



Rensselaer



Emergent spin phenomena in the age of artificial intelligence

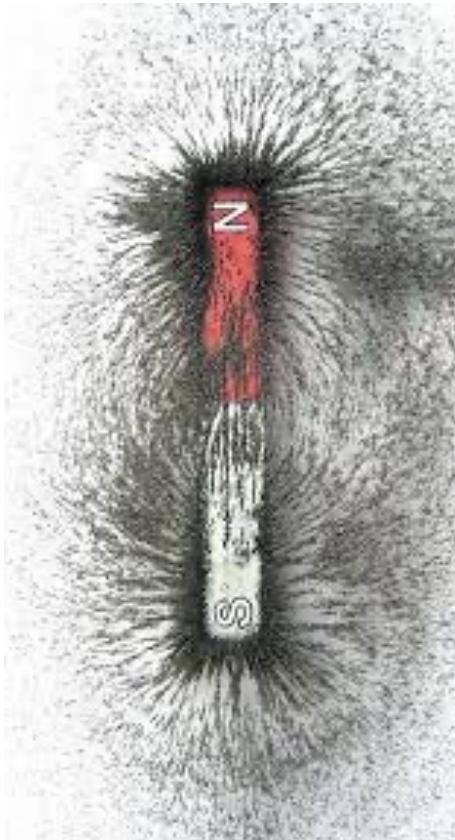
Trevor David Rhone

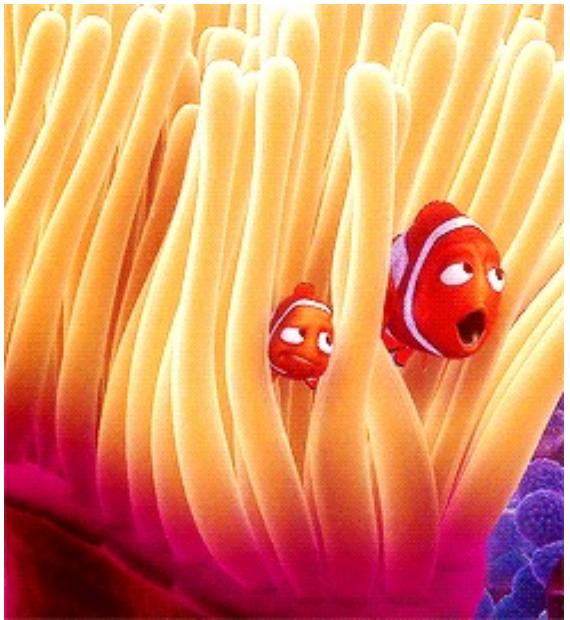
Department of Physics, Applied Physics and Astronomy, Rensselaer Polytechnic Institute

Symposium to Honor the Life and Work of Aron Pinczuk

Aron's Early Influence - Graduate school

Aron's Early Influence - Graduate school





Opportunities and resources!



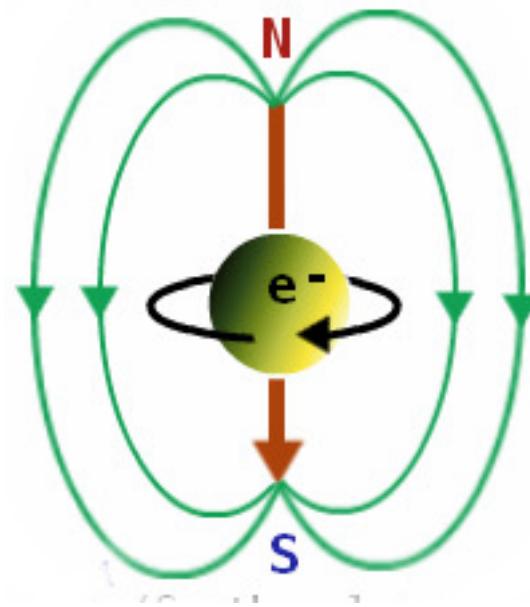
Biggest influence – Research career

- Emergent behavior
 - Low dimensional electron systems
 - Spin degrees of freedom
 - Charge degrees of freedom
- Data analytics and artificial intelligence
 - Molecular beam epitaxy (MBE) of graphene story
 - High-dimensional optimization problem?

More Is Different

Broken symmetry and the nature of the hierarchical structure of science.

P. W. Anderson



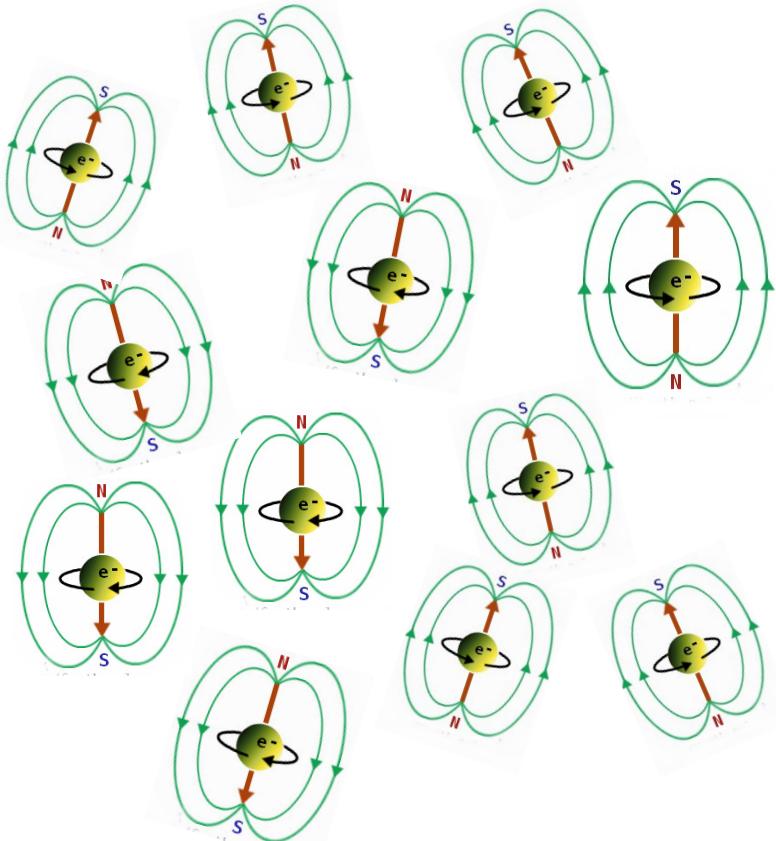
4 August 1972, Volume 177, Number 4047

SCIENCE

More Is Different

Broken symmetry and the nature of
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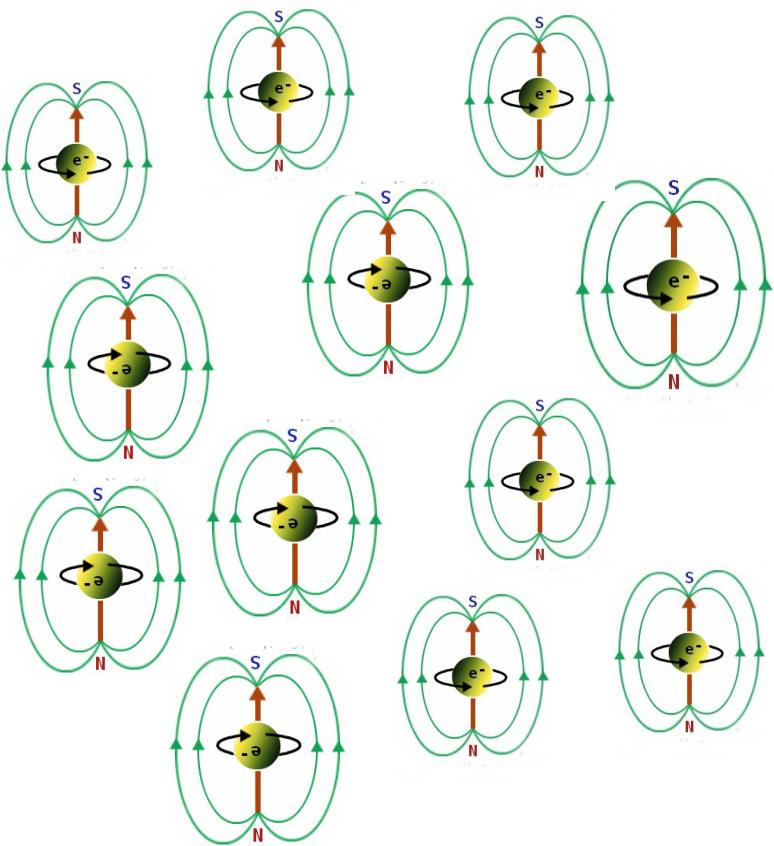
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SCIENCE

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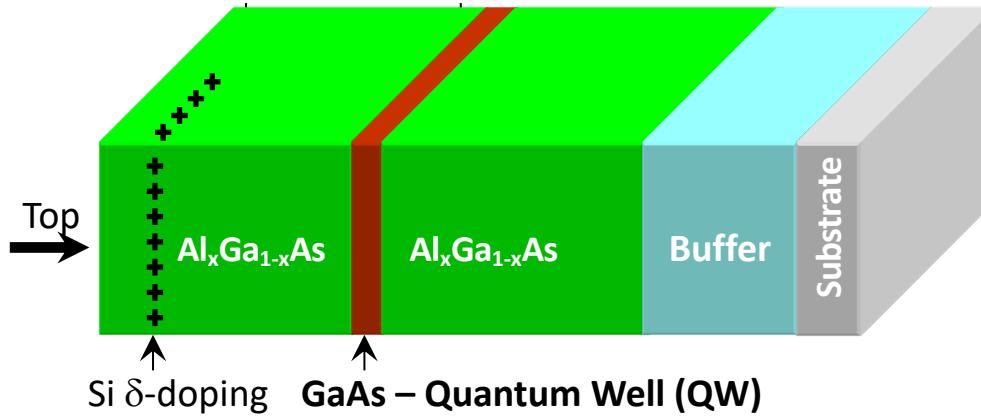
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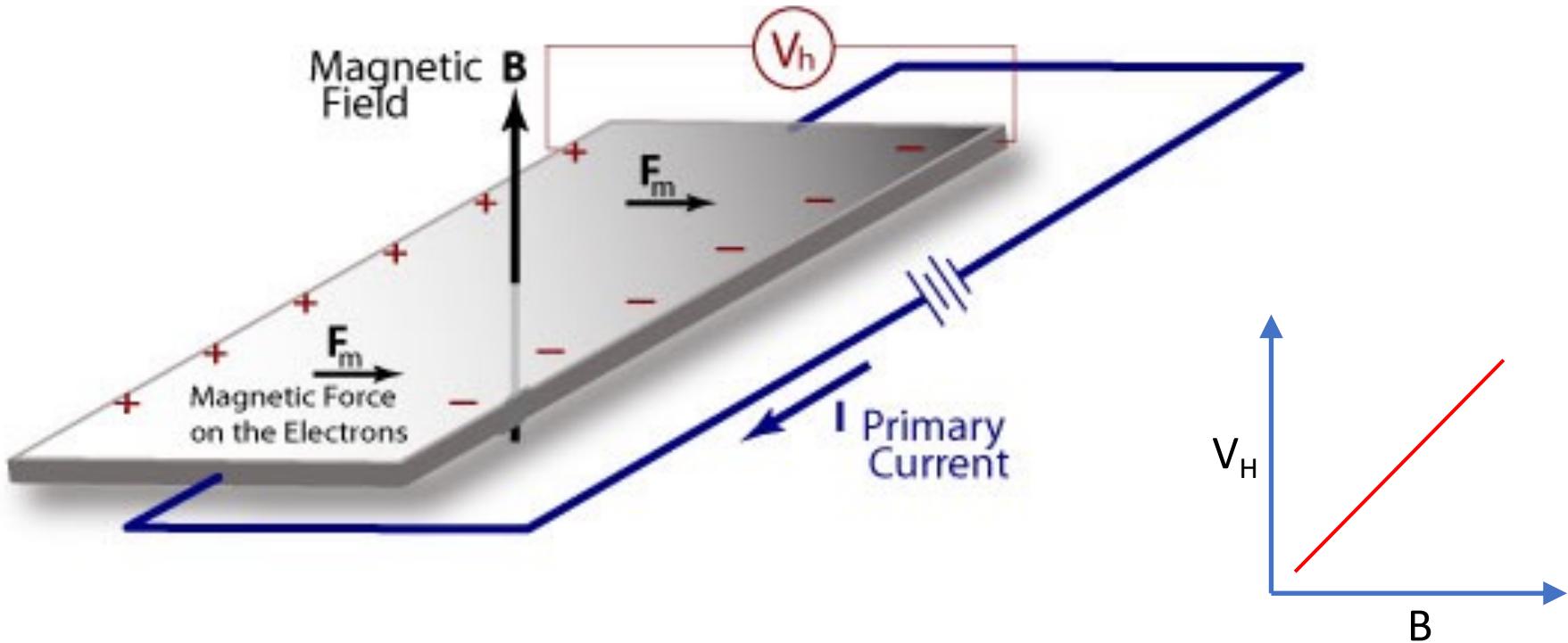
Spin properties in GaAs quantum wells

GaAs Quantum Well



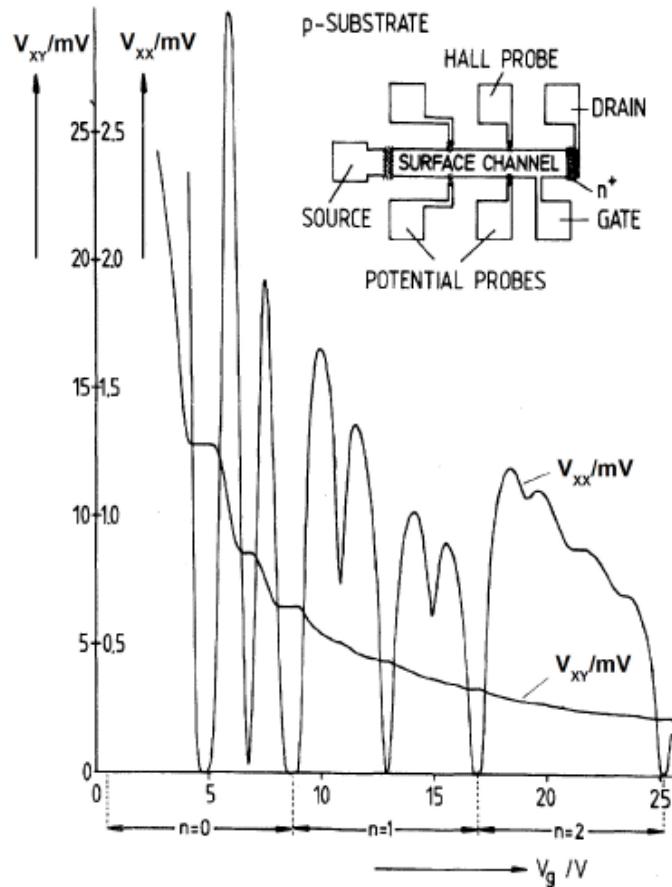
- 270 Angstroms
- $n = [0.5, 4.2] \times 10^{11} \text{ cm}^{-2}$
- **Mobility_{max} = $1.1 \times 10^7 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$**
- V_{gate}

2DES in a magnetic field: Classical Hall Effect



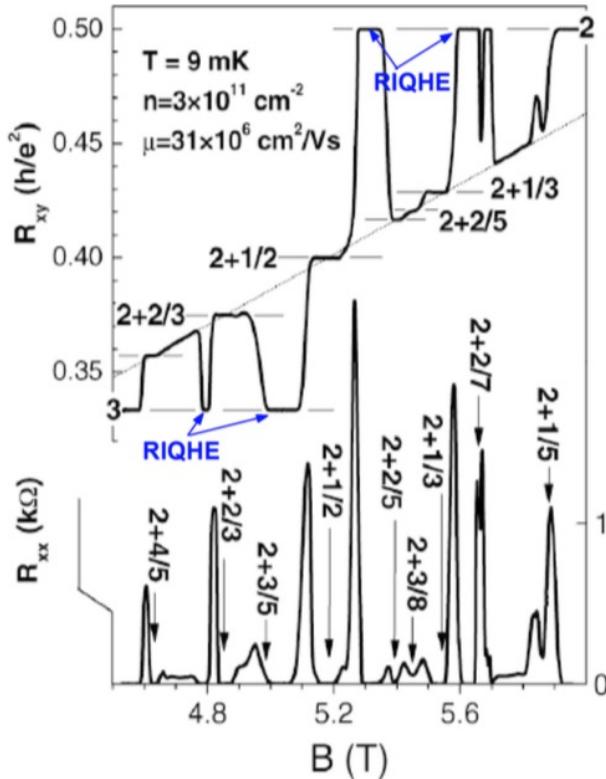
2DES in a magnetic field: Quantum Hall Effect

Integer
Quantum Hall
Effect



I. K. von Klitzing, G. Dorda, and M. Pepper..
Phys. Rev. Lett., 45(494), 1980.

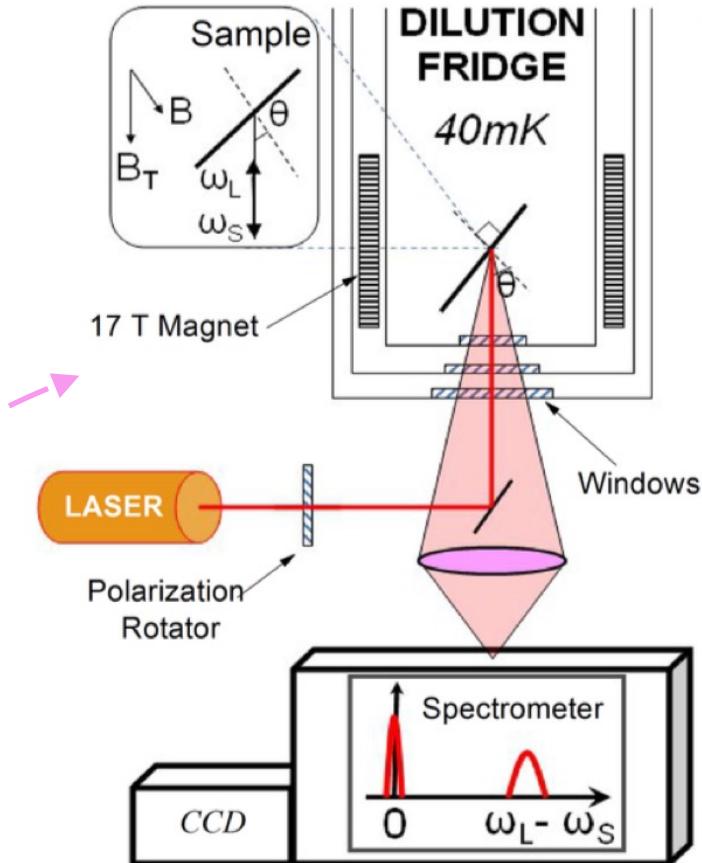
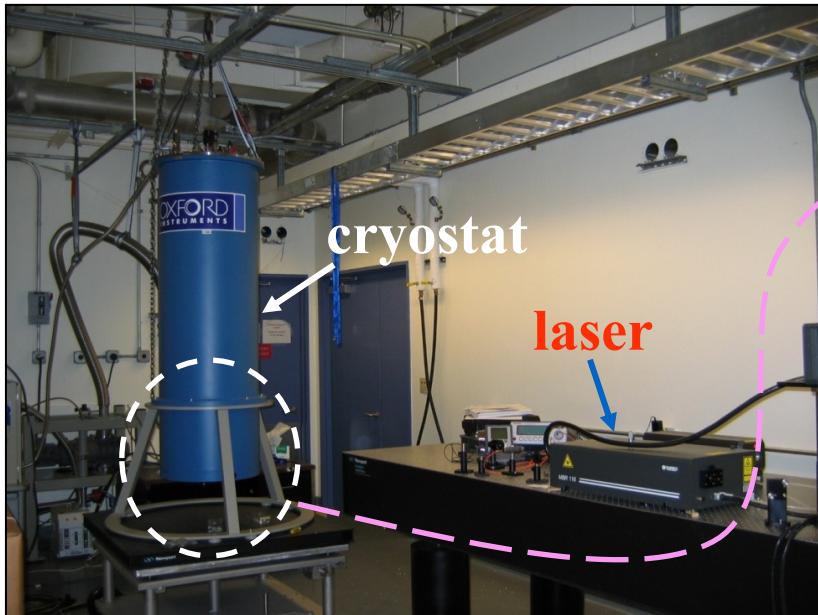
2DES in a magnetic field: Fractional Quantum Hall Effect



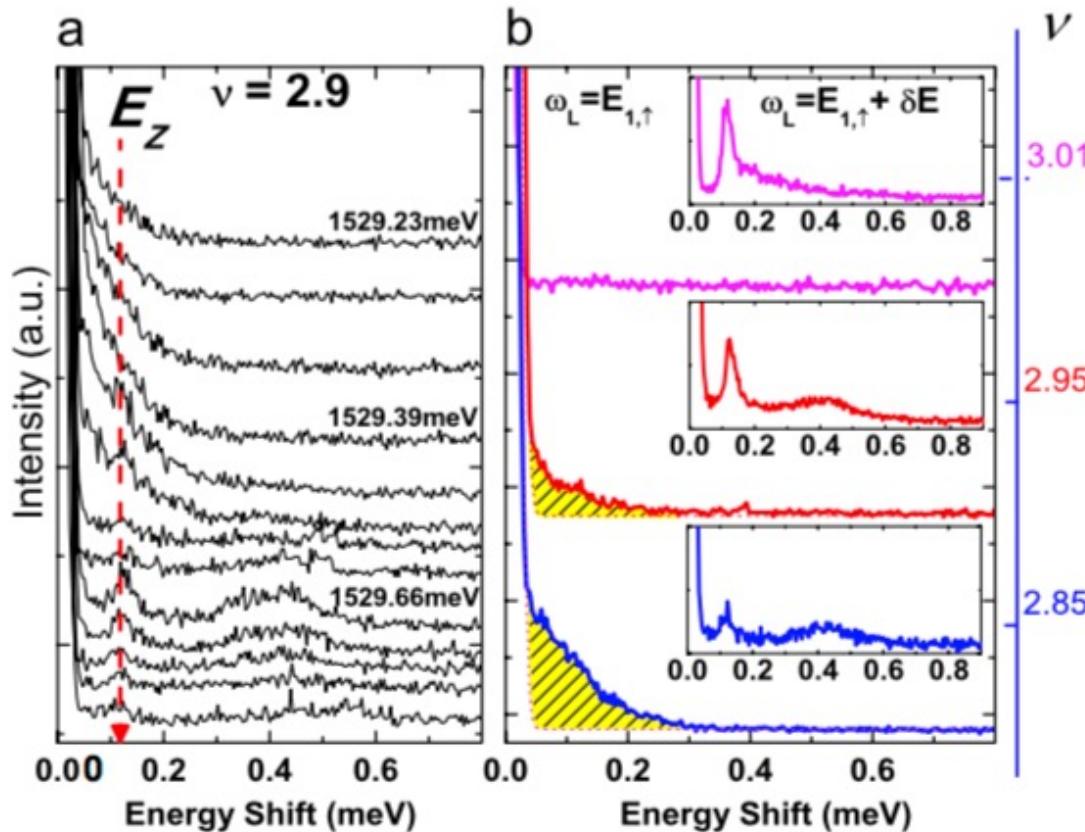
- Exotic even-denominator state at $\nu = 5/2$
- Topologically protected?
- Implement topological quantum computation?

Milli-Kelvin Spectroscopy

- Dilution fridge: $40\text{mK} < T < 2\text{K}$
- Tilt-angle, $\theta = 20$ degrees
- Titanium:Sapphire laser with fine tunability

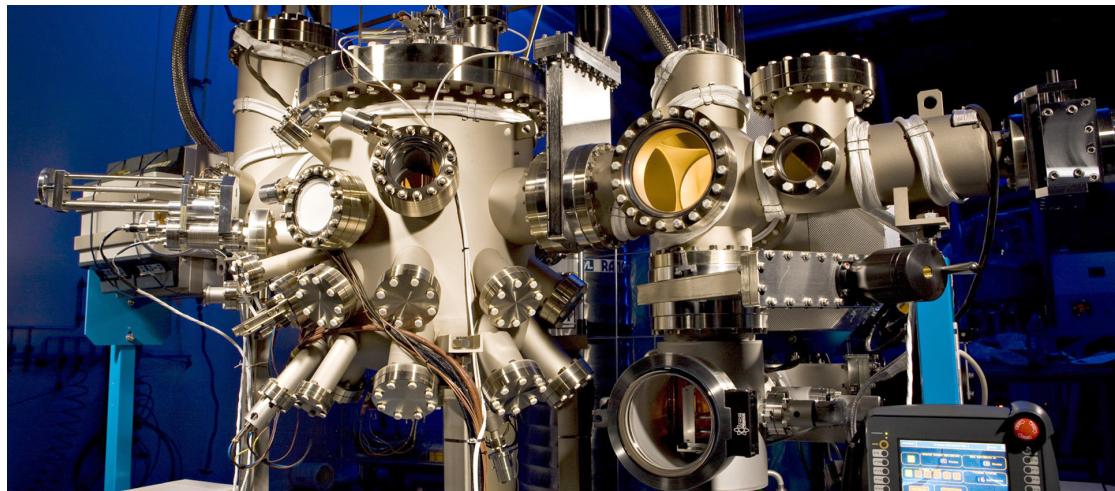
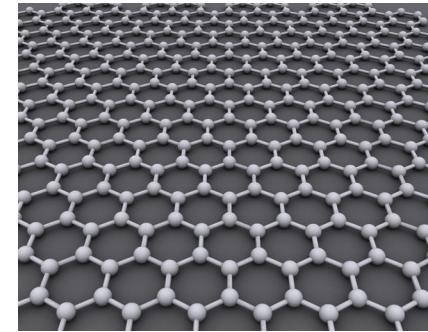


Spin properties of 2DES



Synthesis of graphene by molecular beam epitaxy

- Grow graphene
- High-dimensional parameter space:
 - Substrate temperature
 - Partial pressure of Argon
 - Target temperature
 - Annealing temp.
 - Annealing time
- Measure quality of grown material



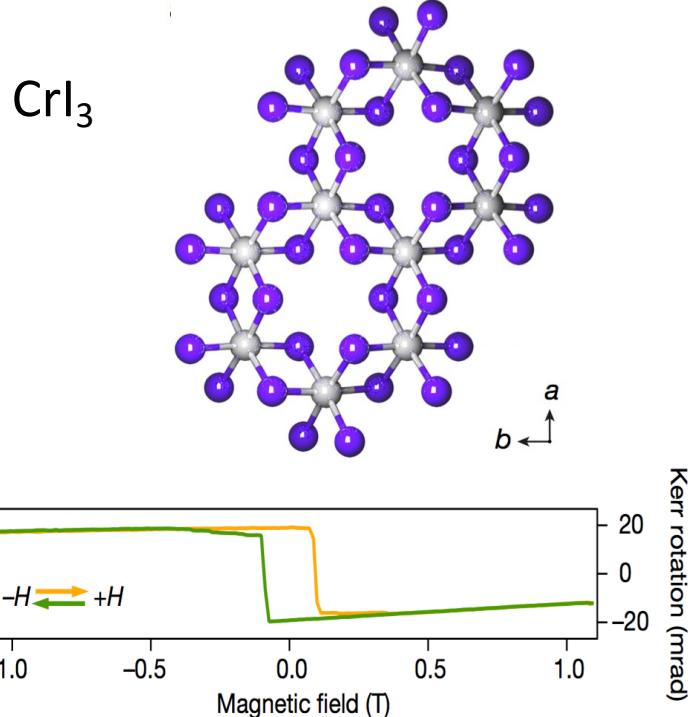
Aron the Influencer – Recently

Harvard University

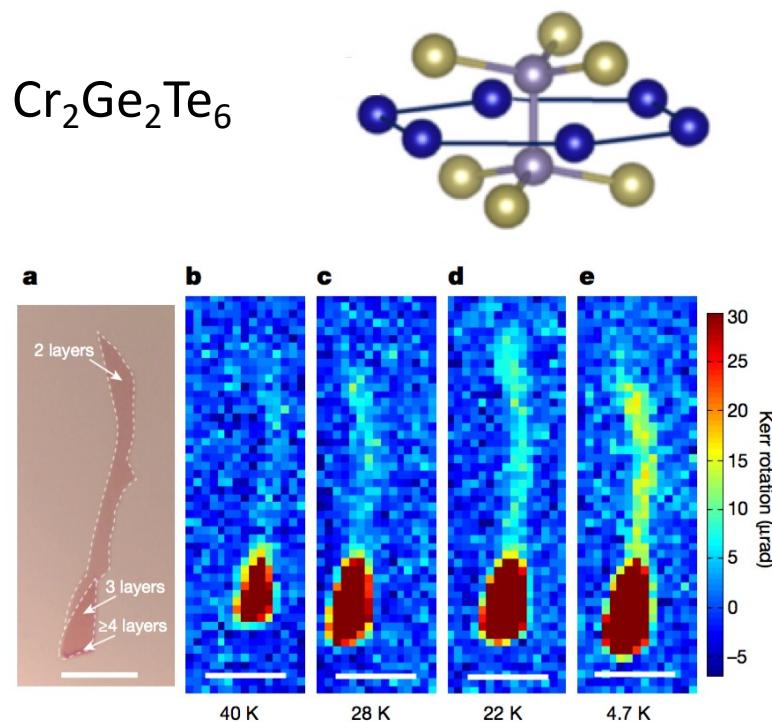


Rensselaer Polytechnic Institute

Two-dimensional Magnetic Materials



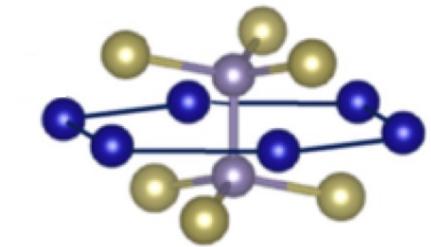
Huang et al., Nature 546, 270 (2017)



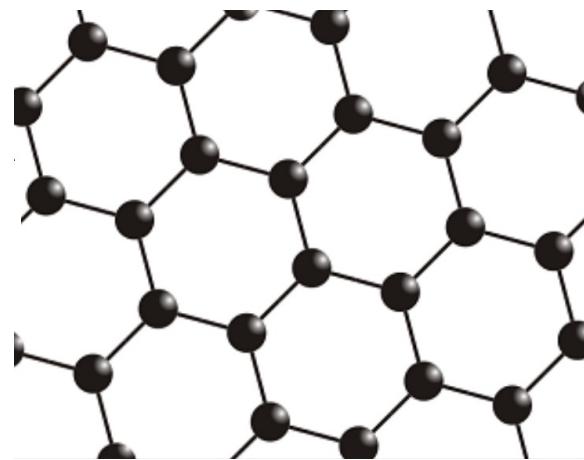
Gong et al., Nature 546, 265 (2017)

Data-driven study of 2D materials?

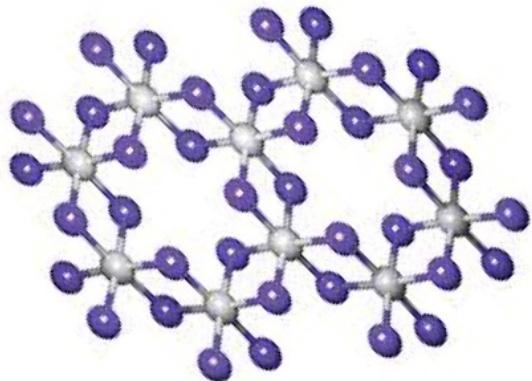
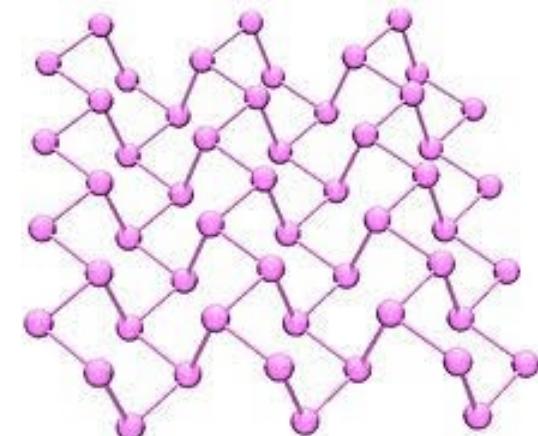
CrGeTe_3



Graphene

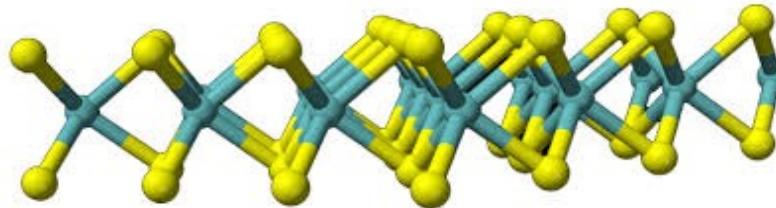


Black phosphorus



CrI_3

MoS_2



Data-driven study of 2D magnetic materials

Motivation:

1. Materials discovery
 - 2D magnetic materials
 - Chemical stability
2. Knowledge discovery
 - Magnetic properties of 2D materials

Discover novel magnetic 2D materials
using materials informatics

Data-driven study of 2D magnetic materials

Materials Informatics

Materials science + Artificial intelligence

$$y = f(x_1, x_2, \dots, x_N)$$

Magnetic moment

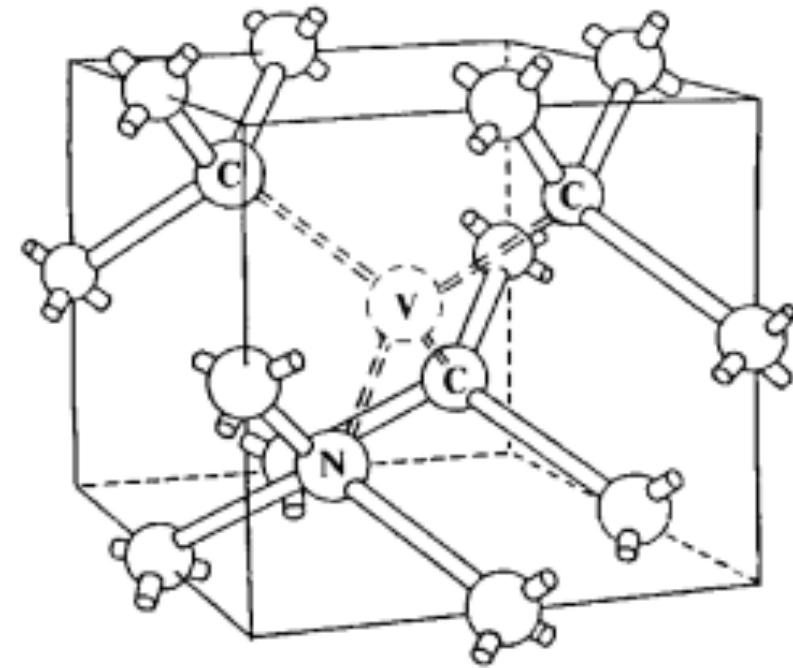
Number of spin up electrons
Number of valence electrons
...
Electronegativity

Why use artificial intelligence to study materials?

- Materials search space is huge
 - ICSD (inorganic crystal structure database)
 - 200,000 inorganic compounds
 - Chemical Abstracts Service
 - 49,037,297 organic/inorganic entries
 - Virtual Chemistry Space¹
 - $\sim 10^{100}$ candidates for materials
- First principles calculations are expensive
- Experiments are slow and expensive

Crystal structure and materials properties

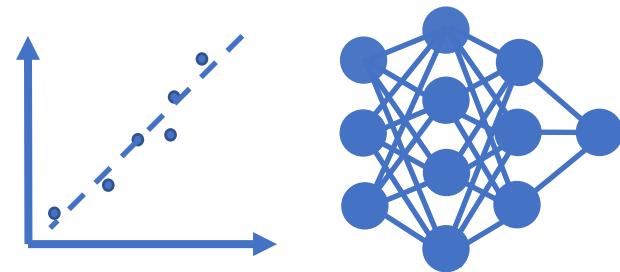
- Structure-property relationships:



Artificial Intelligence for Materials Studies



- The rise of the materials databases
 - Data are accessible
- Chemical space descriptors exist
 - Coulomb Kernel¹, Bag of bonds representation²
- Datascience tools exist
 - Scikit learn, Google's TensorFlow



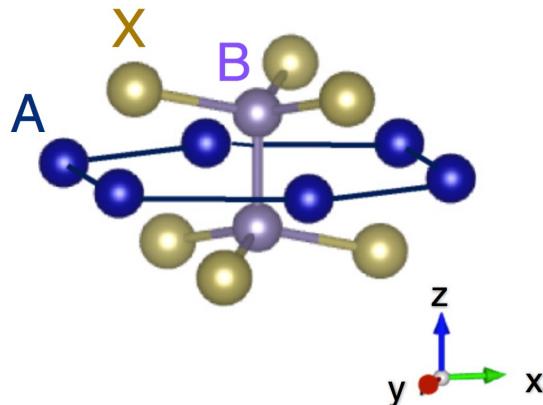
Artificial Intelligence for Materials Studies

Magnetic 2D crystals

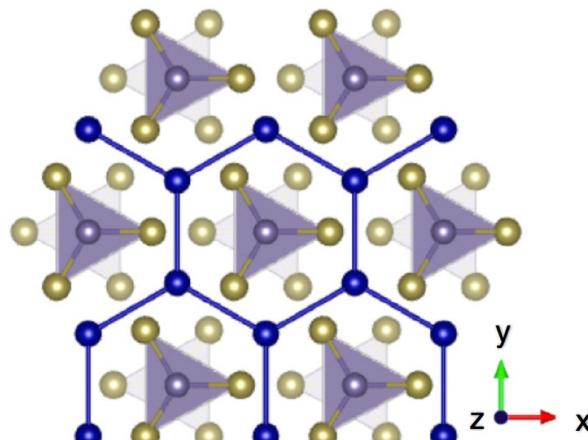
Artificial Intelligence for Materials Studies

Magnetic 2D crystals

Transition metal trichalcogenides are magnetic 2D atomic crystals



$A_2B_2X_6$ crystal structure



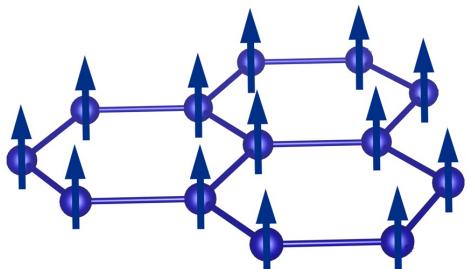
- CrGeTe_3 is a ferromagnet (FM)^{1,2}
- Monolayer CrSiTe_3 is a zigzag antiferromagnet (zigzag-AFM)¹

Artificial Intelligence for Materials Studies

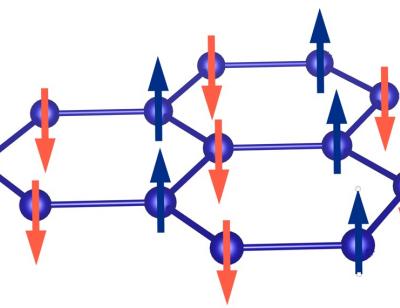
Magnetic 2D crystals

Transition metal trichalcogenides are magnetic 2D atomic crystals

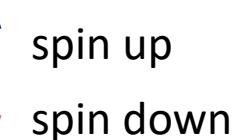
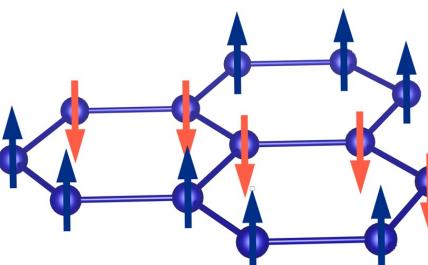
FM



Neel-AFM



zigzag-AFM



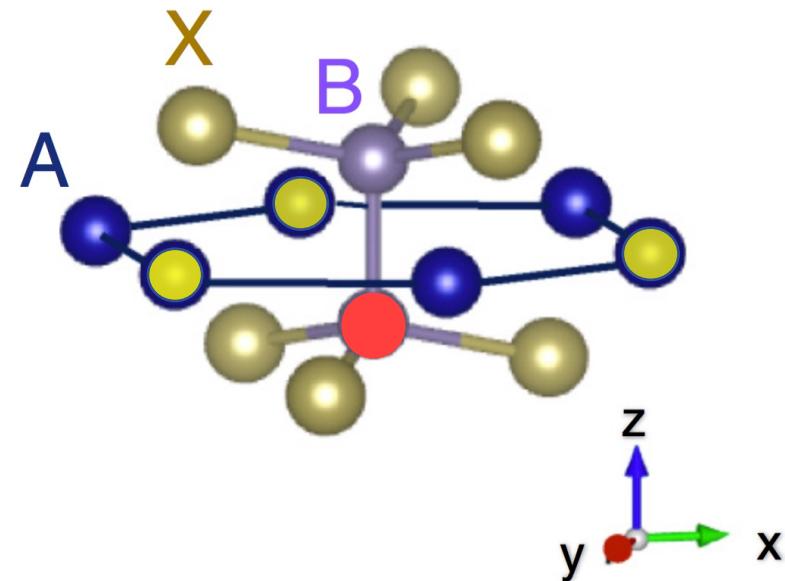
Magnetic structures

- CrGeTe₃ is a ferromagnet (FM)^{1,2}
- Monolayer CrSiTe₃ is a zigzag antiferromagnet (zigzag-AFM)¹

Magnetic van der Waals materials

$A_2B_2X_6$ structures

- Create 198 ABX_3 structures using DFT
 - Total # of structures $\sim 10^4$
 - NM, FM and AFM spin configurations
- Extract data:
 - Formation energy
 - Magnetic order
 - Magnetic moment

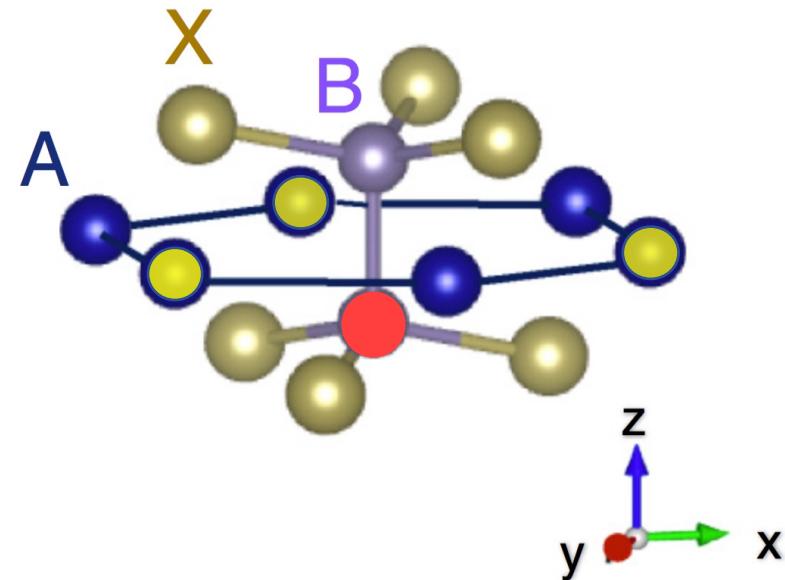


Magnetic van der Waals materials

$A_2B_2X_6$ structures

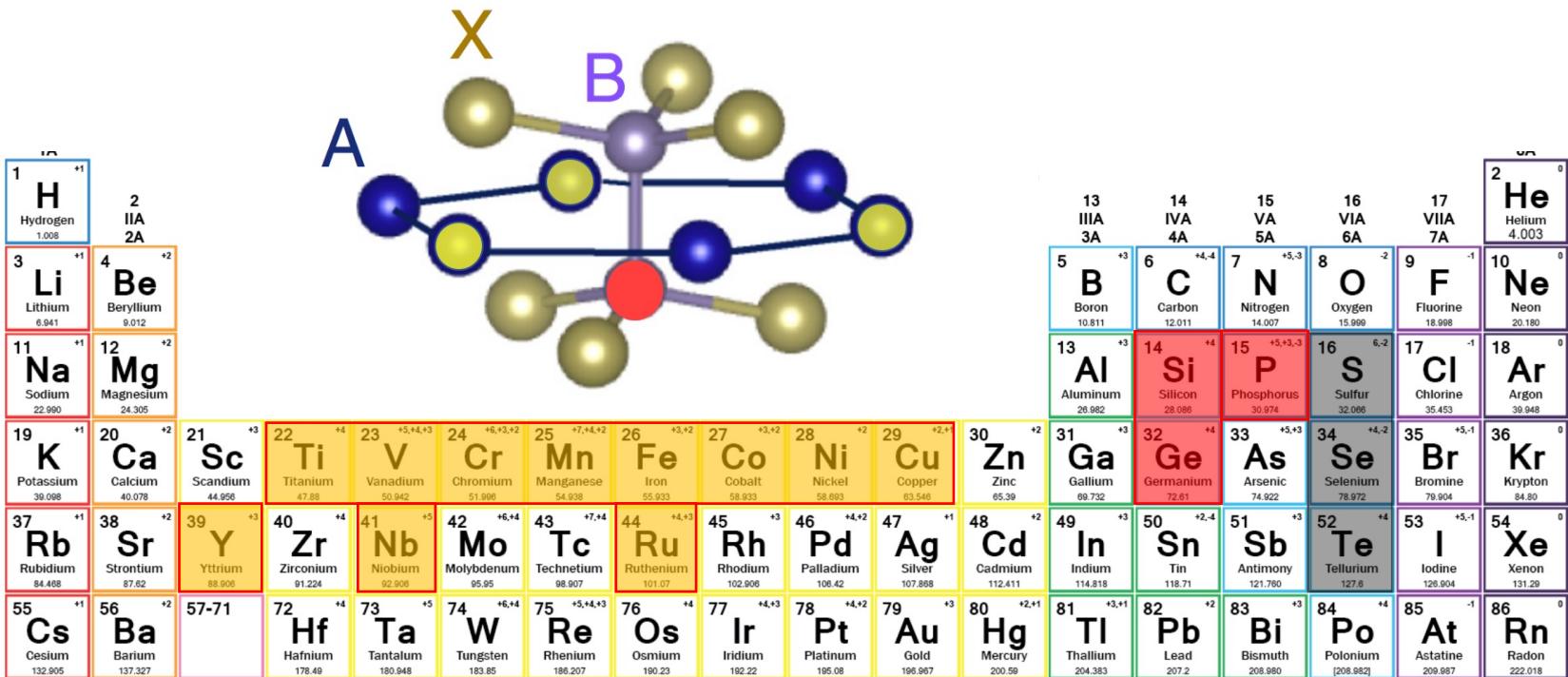
Substitutions:

- A site:
 - $Cr_{0.5}A_{0.5}$
 - A: Ti, V, Cr, Mn, Fe, Co, Ni, Cu, Y, Nb, Ru
- B site:
 - Si, Ge, P combinations
 - B: Si, Ge, P, $Si_{0.5}Ge_{0.5}$, $Si_{0.5}P_{0.5}$, $Ge_{0.5}P_{0.5}$
- X site:
 - S, Se, Te

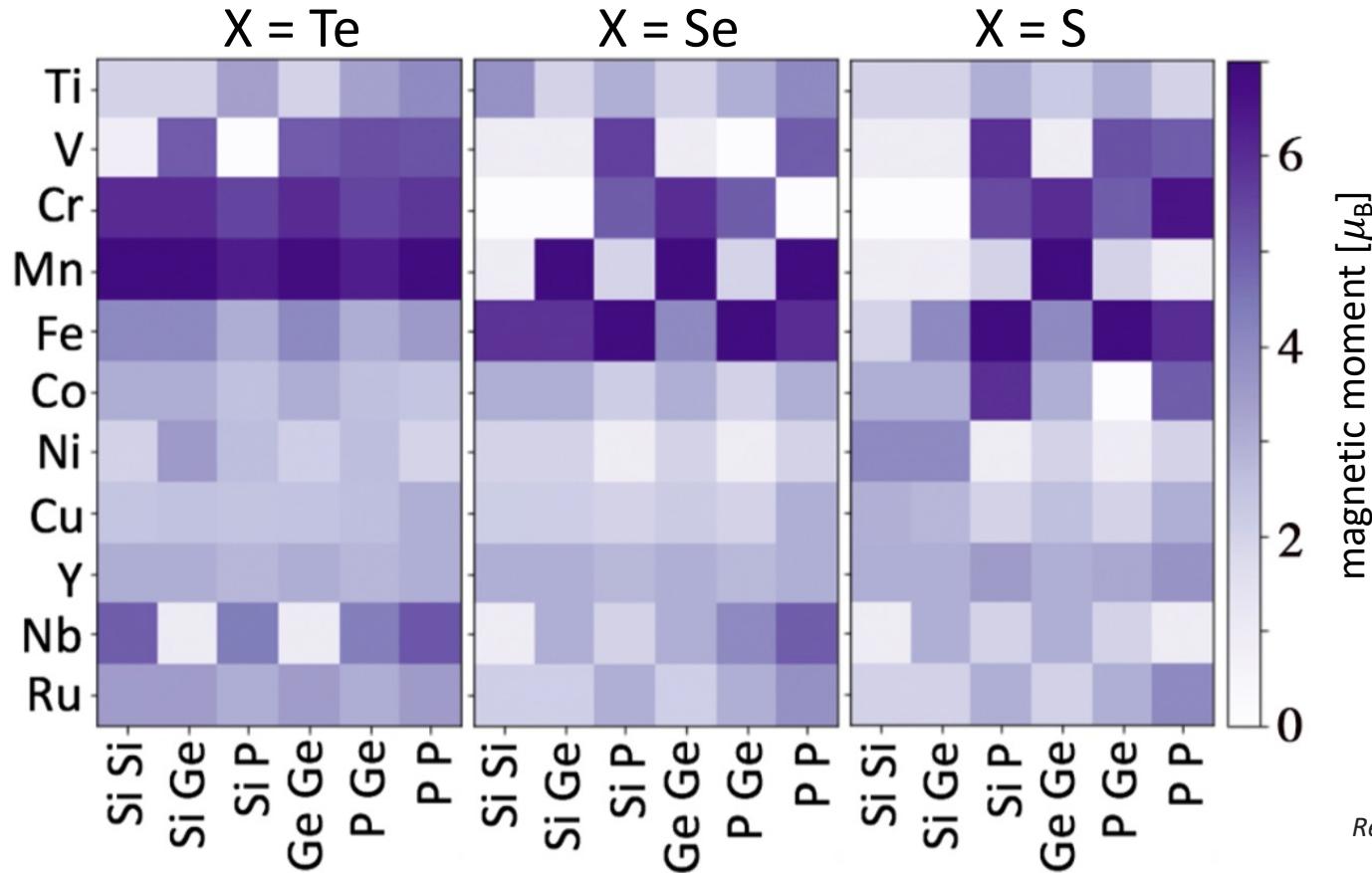


Magnetic van der Waals materials

$A_2B_2X_6$ structures

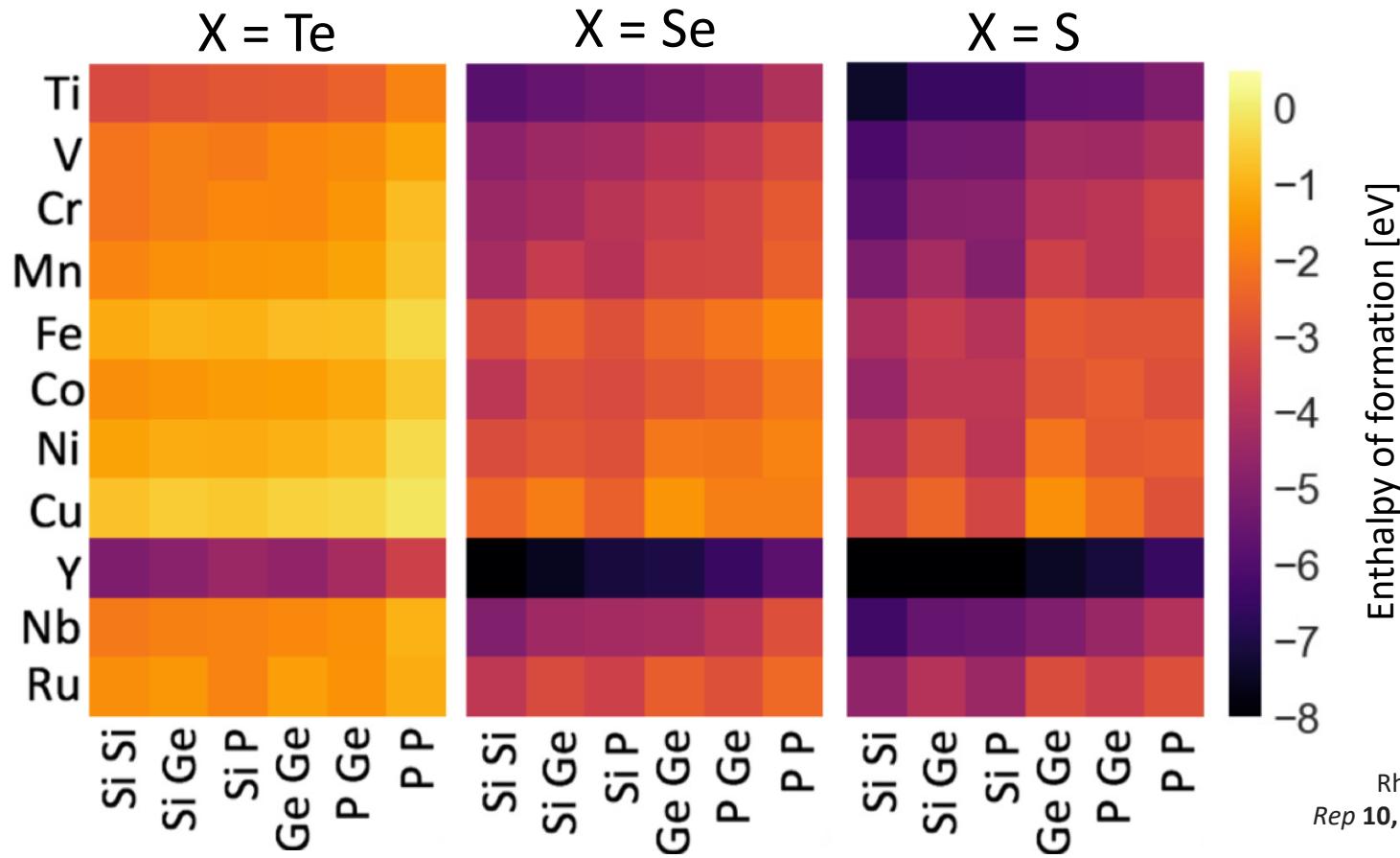


Magnetic moment of $A_2B_2X_6$



Formation energy of $A_2B_2X_6$

Formation energy of $A_2B_2X_6$



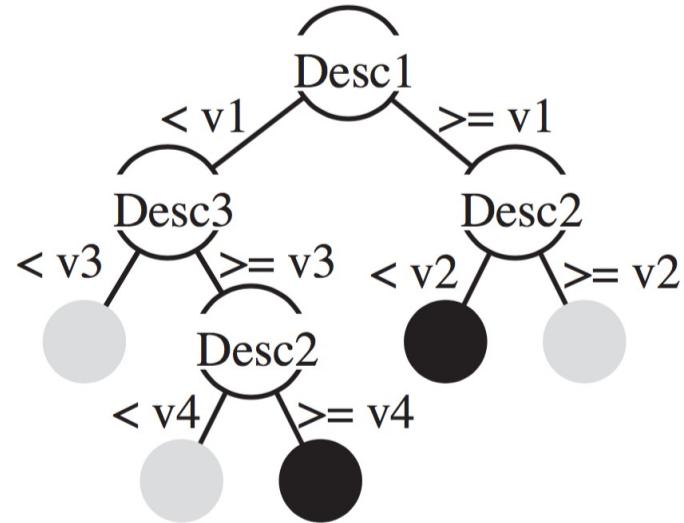
Artificial intelligence in materials science

Materials descriptors

- Describe system using easily attainable components
 - Atomic properties, p
- Compound Property, P
 - $P = \text{mean}(p(A), p(B), p(X))$
 - $P = \text{std. deviation}(p(A), p(B), p(X))$
- Total # of descriptors:
 - 61
- Atomic property, p :
 - Number of spin up e's
 - atomic radius
 - etc.

Machine learning models

- Random forest regression
 - Machine learning model
 - Inputs: X
 - Number of spin up e's
 - Output: Y
 - Magnetic moment
 - Training data
 - Test data
-
- Node m, region R_m , N_m observations
 - Mean Absolute Error
 - minimize L1 error using median values at terminal nodes

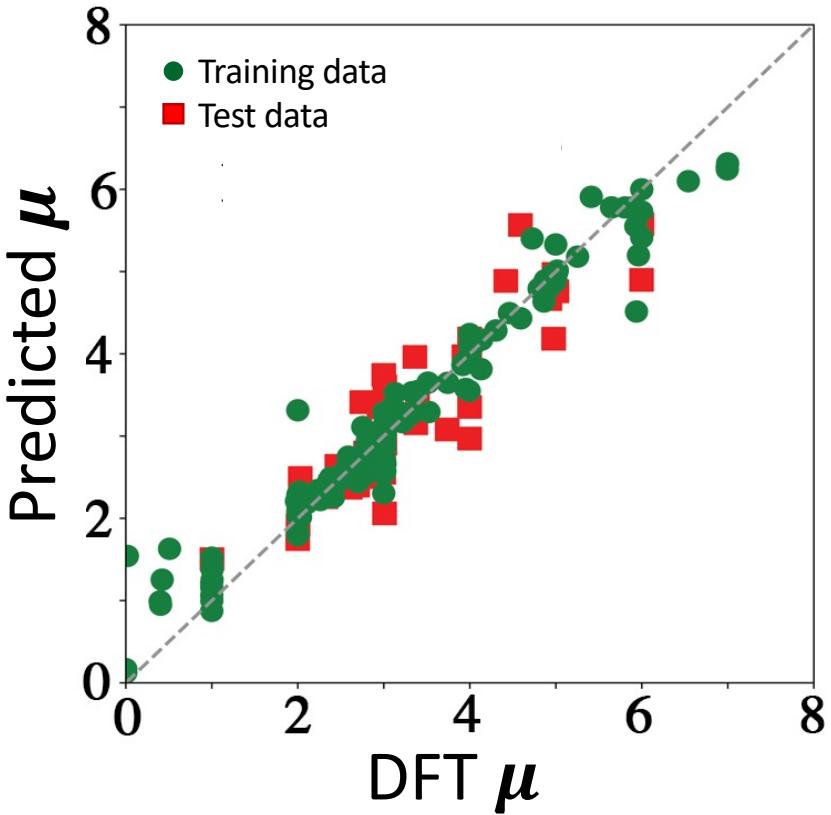


$$L(X_m) = \frac{1}{N_m} \sum_{i \in N_m} |y_i - \bar{y}_m|$$

$$\bar{y}_m = \frac{1}{N_m} \sum_{i \in N_m} y_i$$

Machine learning predictions

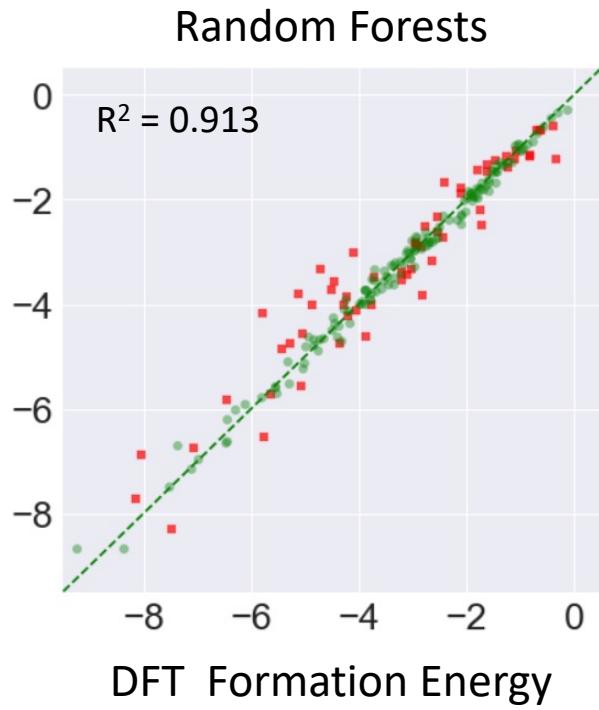
Magnetic moment, X=Te



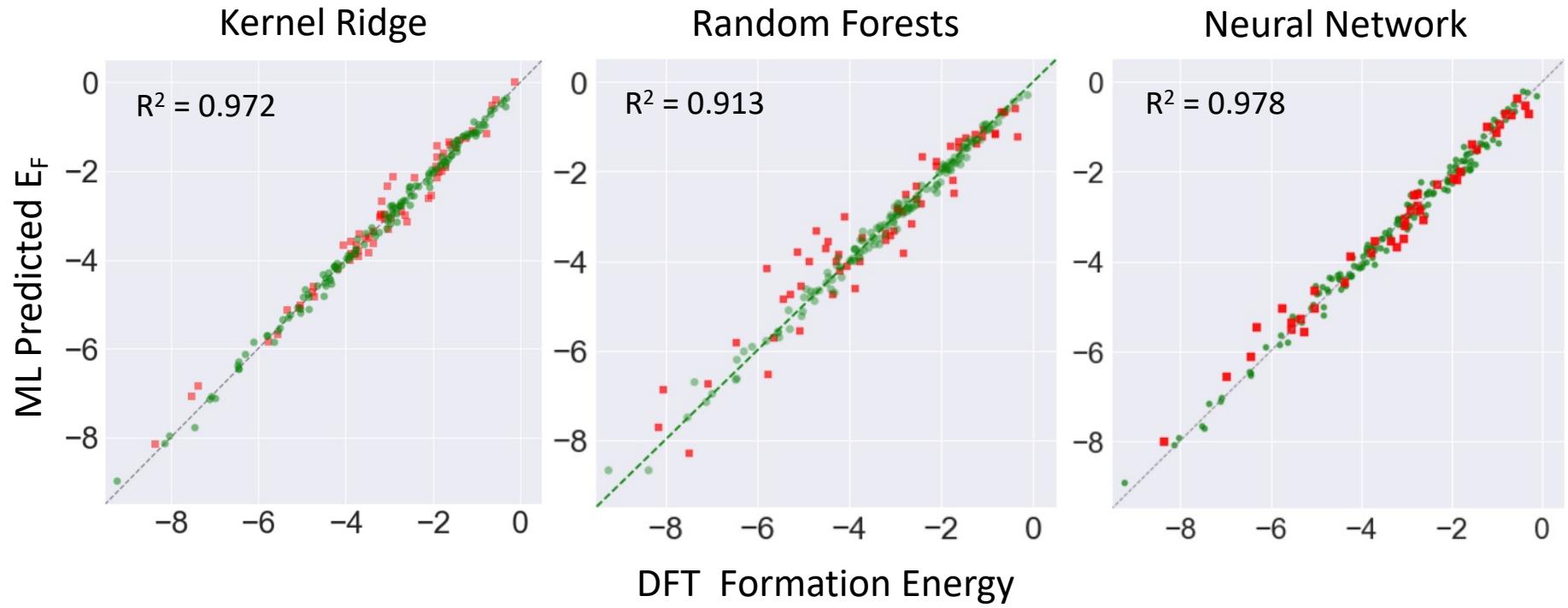
- $N = 262$
- Random forest $R^2 = 0.98$
- Mean absolute error
(MAE) = $0.30 \mu_B$

DFT: first-principles quantum calculations
 μ : magnetic moment \sim magnetization

Machine learning predictions of DFT formation energy

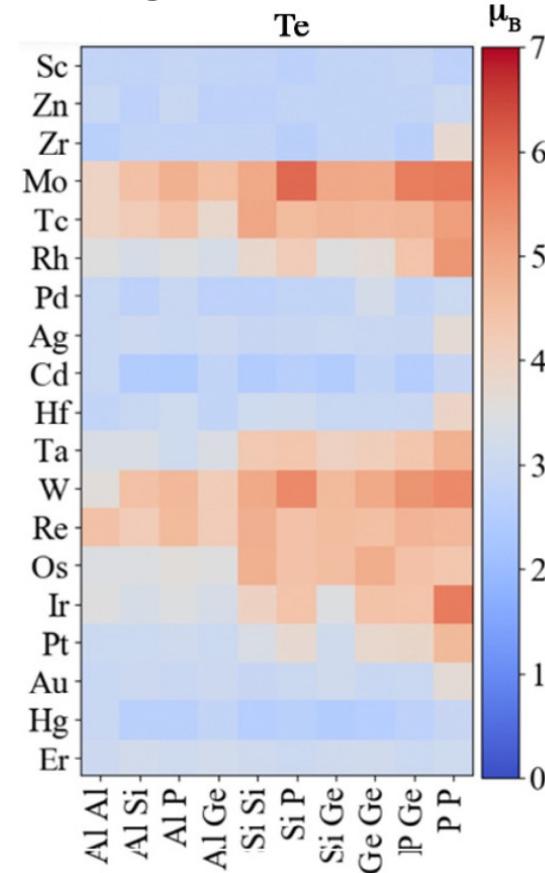


Machine learning predictions of DFT formation energy

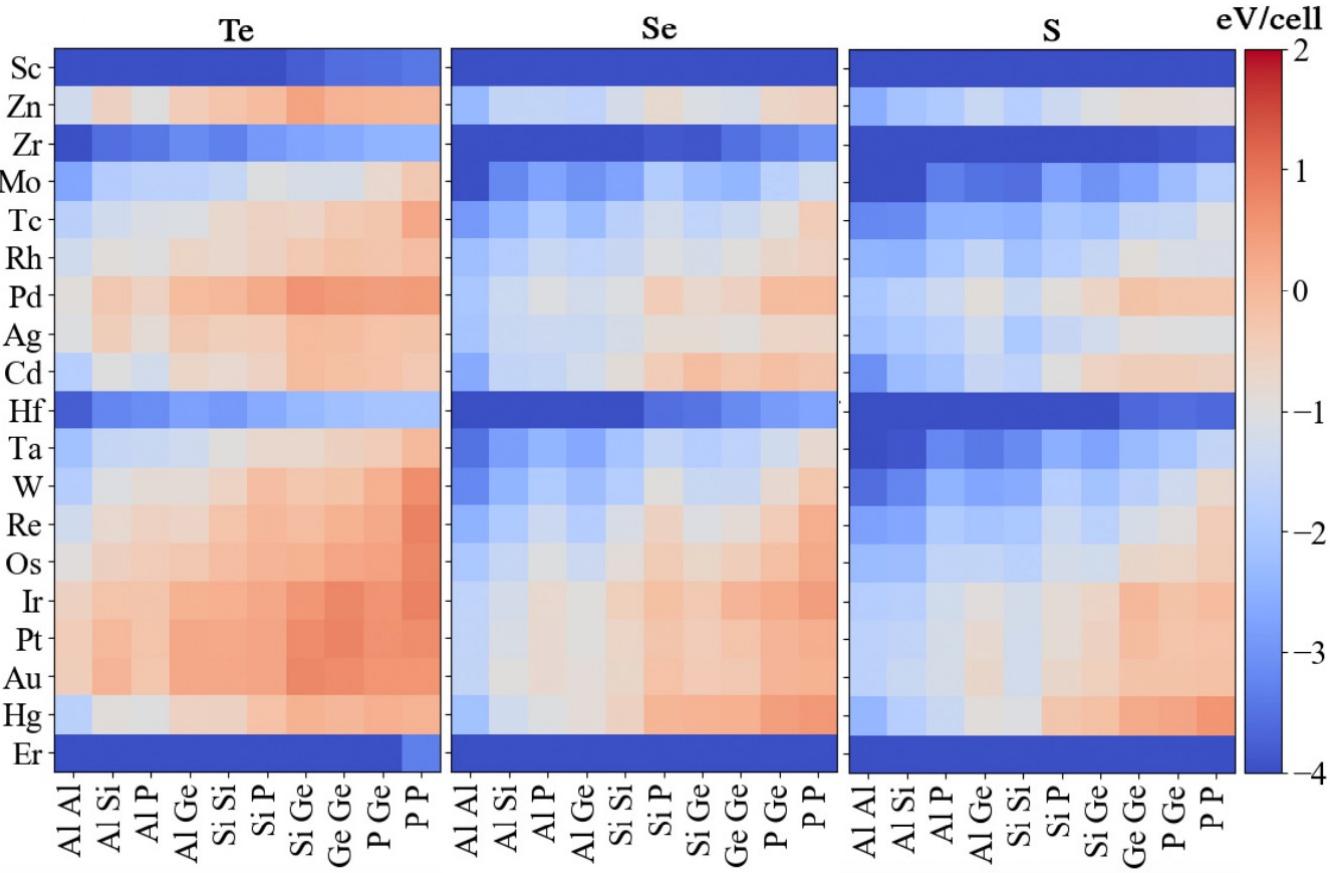


Machine learning results

Magnetic moment



Formation Energy



Candidates for chemically stable 2D ferromagnets

- Initial DFT data (198 structures)
- ML predictions (> 4000 structures)

Large dataset of structures



Stable structures



Large μ & stable

Screening Criteria:

- Magnetic moment $> 5 \mu_B$ & Formation energy $< -1.1\text{eV}$

DFT results:

- $(\text{CrMn})\text{Si}_2\text{Te}_6$
- $(\text{CrMn})\text{Ge}_2\text{Se}_6$
- $(\text{CrFe})(\text{SiP})\text{S}_6$

ML Results:

- $(\text{CrMo})\text{Si}_2\text{Te}_6$
- $(\text{CrW})\text{Si}_2\text{Te}_6$
- $(\text{CrMo})(\text{SiP})\text{Te}_6$

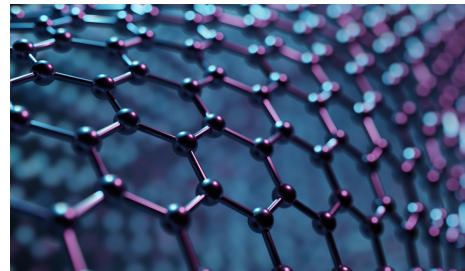
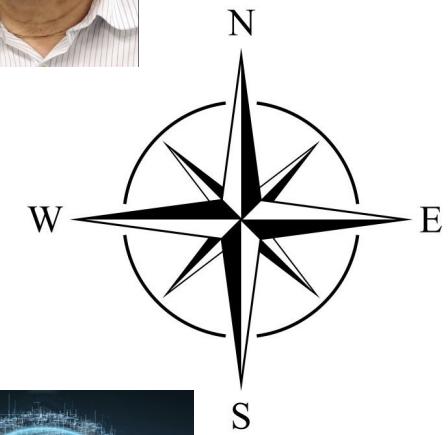
AI-guided materials discovery

Outcomes

- Identified new chemically stable 2D ferromagnets
- AI provides fast estimates of 2D materials' properties
 - $> 4000 A_2B_2X_6$ composites
 - Magnetic properties
 - Chemical stability
- Non-traditional framework for studying emergent spin phenomena in 2D materials

Summary

- Aron's invaluable guidance shaped the lives and careers of many
- A collection of people, under the right conditions, can give rise to 'emergent phenomena'
- AI-guided identification of emergent spin phenomena in materials



Acknowledgements



- This work used the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by National Science Foundation grant number ACI-1548562
- Some of the computations in this paper were run on the Odyssey cluster supported by the FAS Division of Science, Research Computing Group at Harvard University
- This research used resources of the Argonne Leadership Computing Facility, which is a DOE Office of Science User Facility supported under Contract DE-AC02-06CH11357.
- This material is based upon work supported by the National Science Foundation CAREER award under Grant No 2044842

TANGOMA



Aron's Early Influence – Postdoctoral studies

Postdoc at NTT, Japan

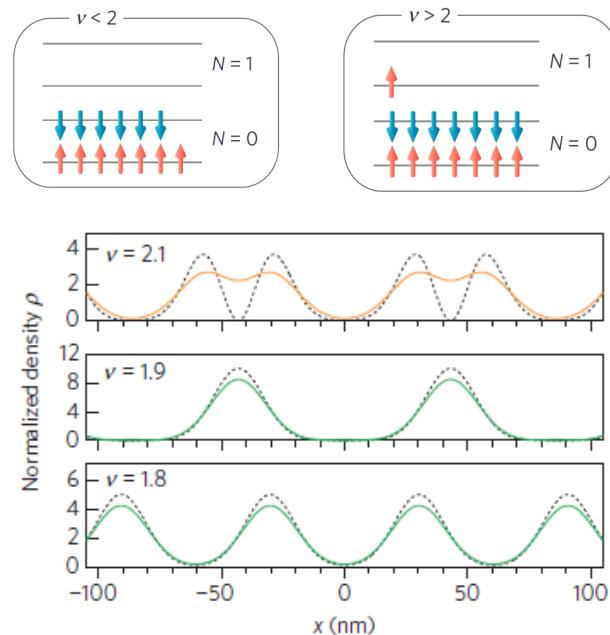
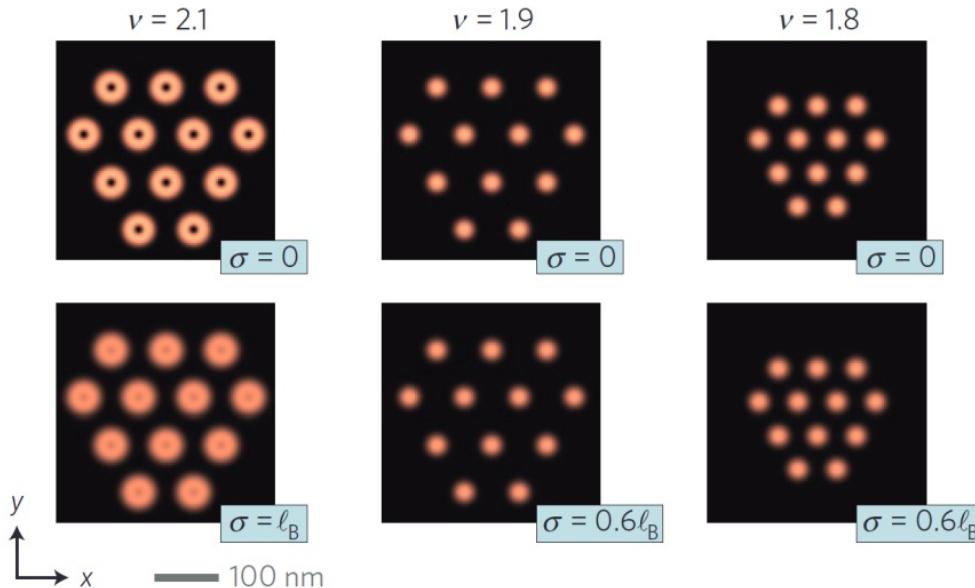


Charge properties of electrons in GaAs quantum wells

NMR probes Wigner Solids: *In-plane local density variations at $v \sim 2$*

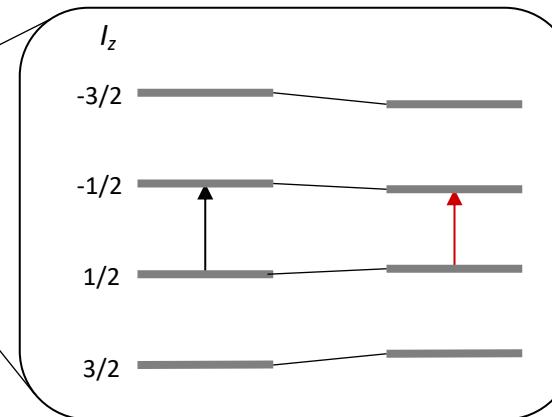
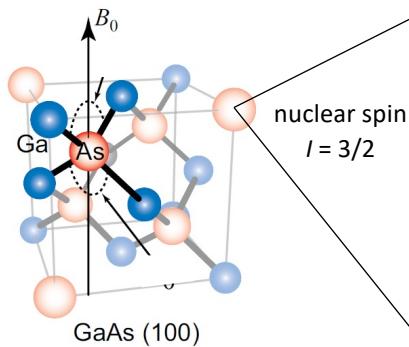
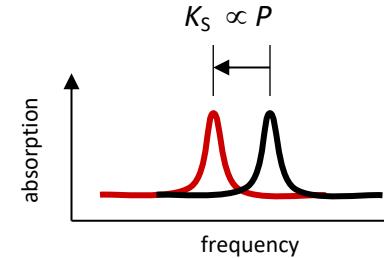
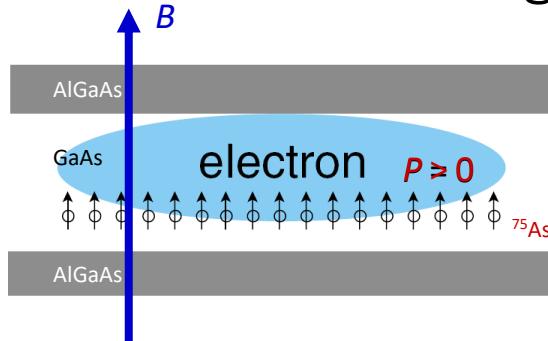
NMR profiling of quantum electron solids in high magnetic fields

a



- 1) L. Tiemann^(*), T.D. Rhone^(*), N. Shibata, K. Muraki, Nature Physics, doi:10.1038/nphys3031
(^{*}: equal contribution)

Nuclear Magnetic Resonance (NMR) Knight Shift

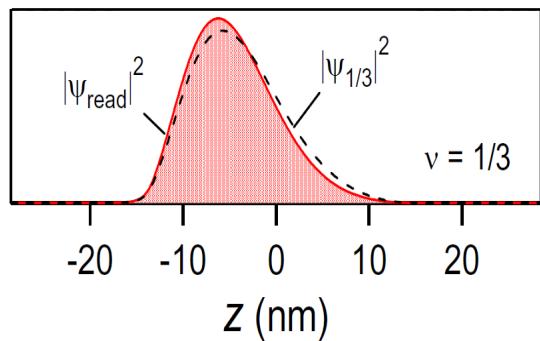


electron spin

$P = 0$

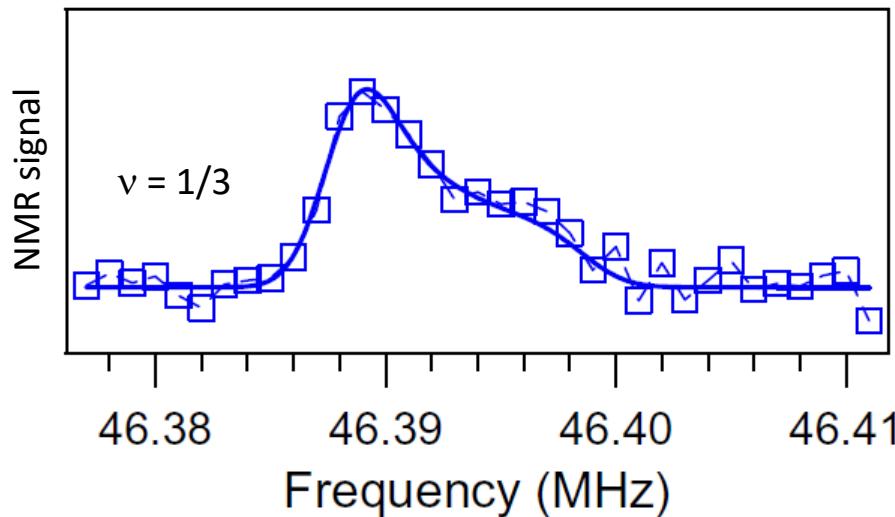
$P > 0$

Simulating RD-NMR Spectra

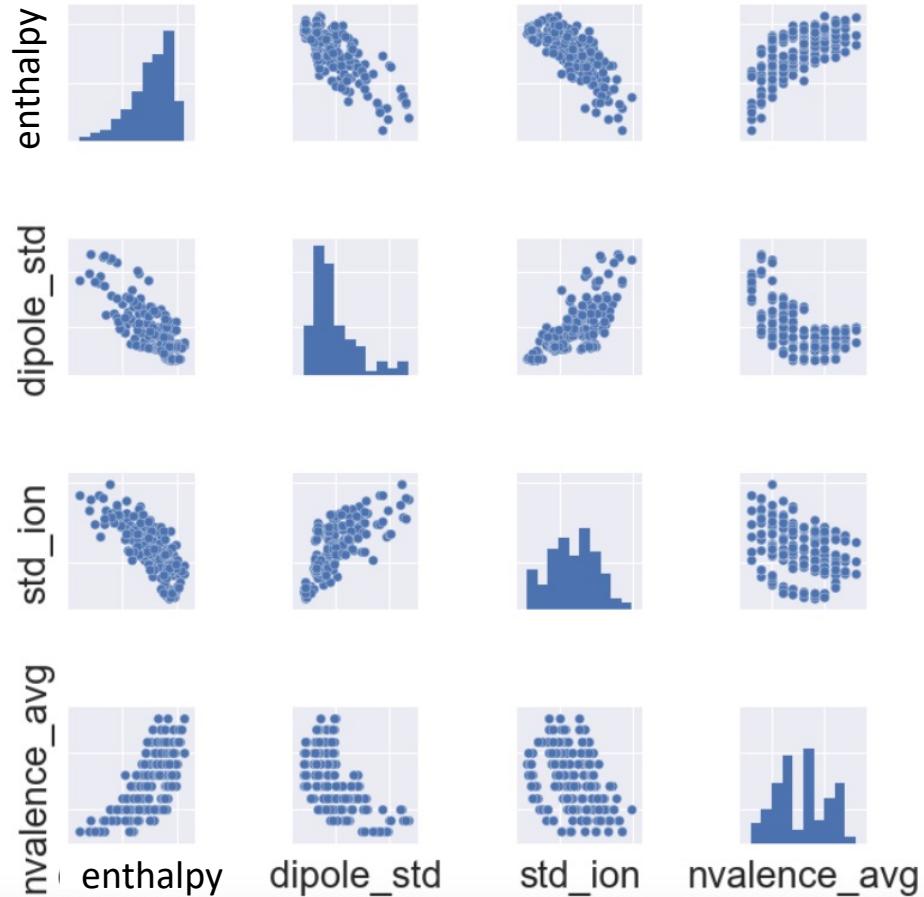


$$I_v(f - f_0) = \int_{-w/2}^{w/2} g(f - f_0 + \underbrace{\alpha_v |\psi_v(z)|^2}_{\text{(spin polarization)}}) \underbrace{|\psi_{\text{read}}(z)|^2 dz}_{\text{(electron density)}}$$

(spin polarization) x (electron density)

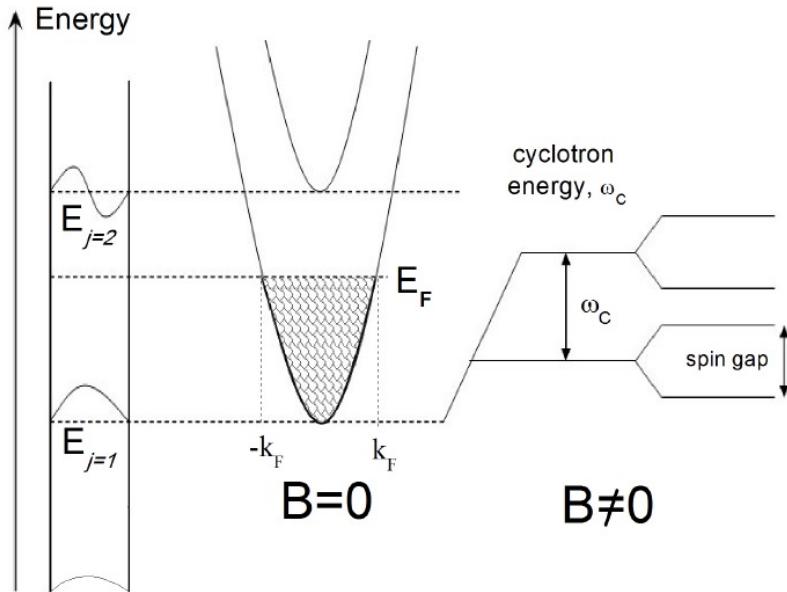


Materials descriptors: data visualization



- Compound Property, P
 - $P = f(p(A), p(B), p(X))$
- p:
 - Enthalpy
 - Polarizability (dipole_std)
 - Ionization energy (std_ion)
 - # valence electrons (nvalence_avg)

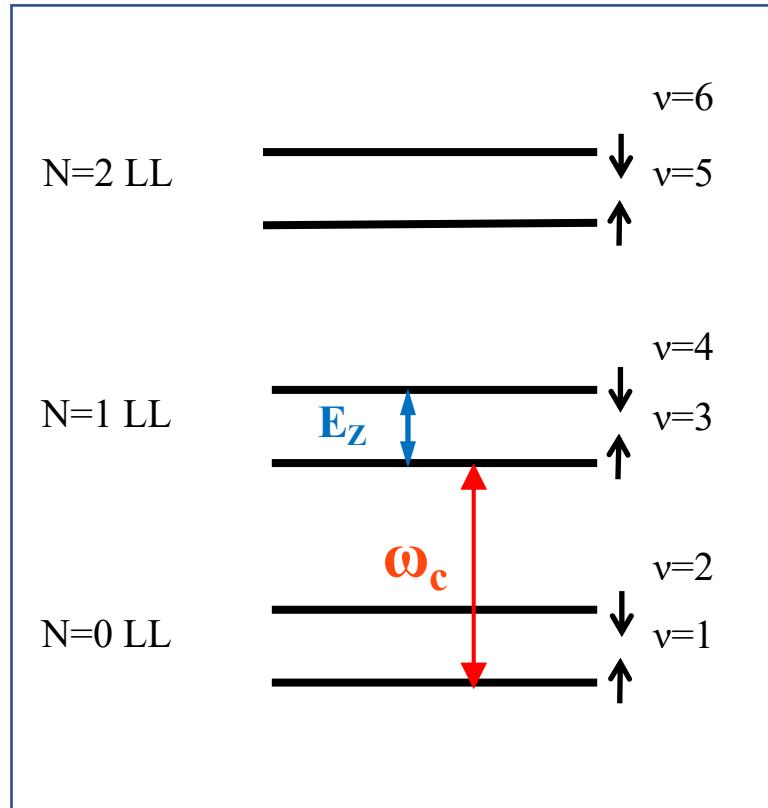
Quantum Well



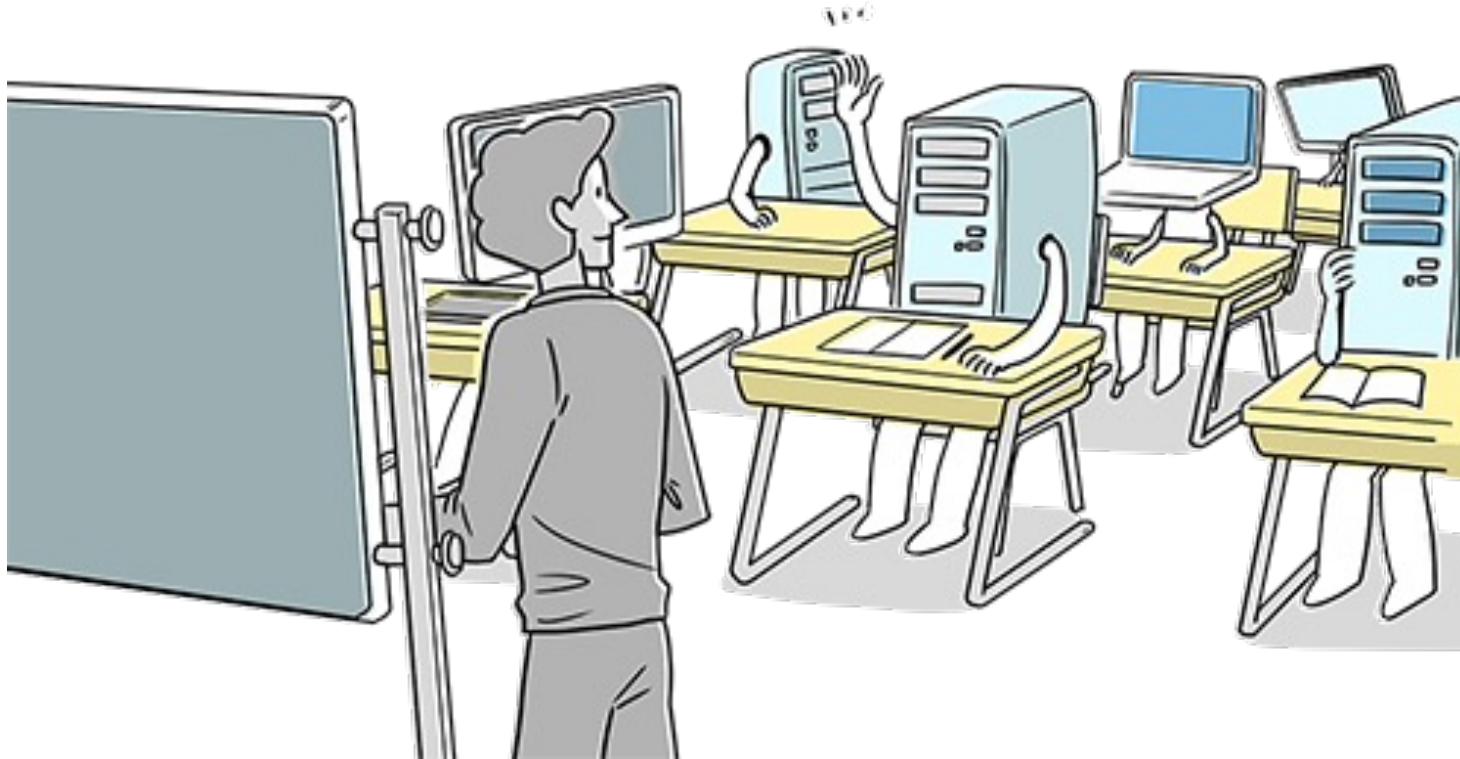
$$\omega_c = eB/m^*c$$

$$\nu = n/(B/\phi_0)$$

Spin gap is the
Zeeman energy



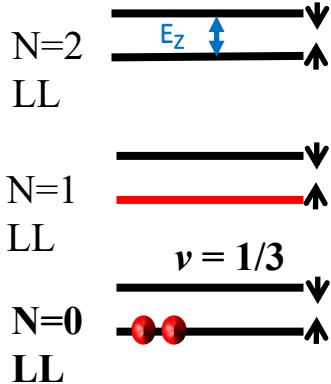
What is Materials Informatics?



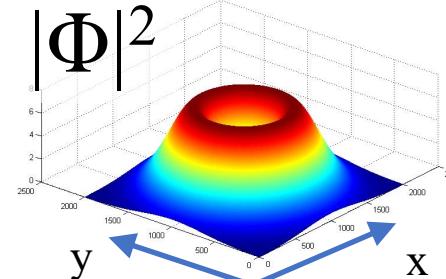
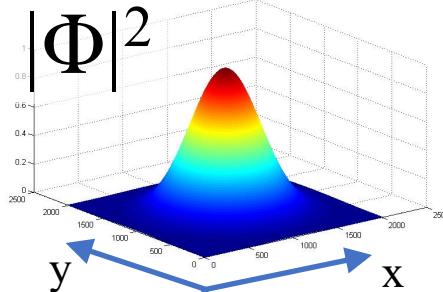
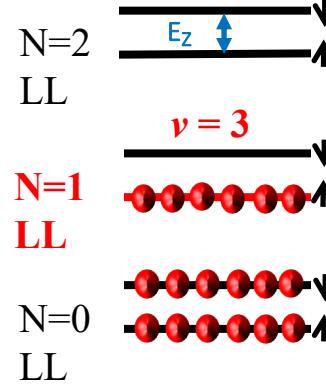
Teaching computers materials science using machine learning!

2DES in varying LL regimes

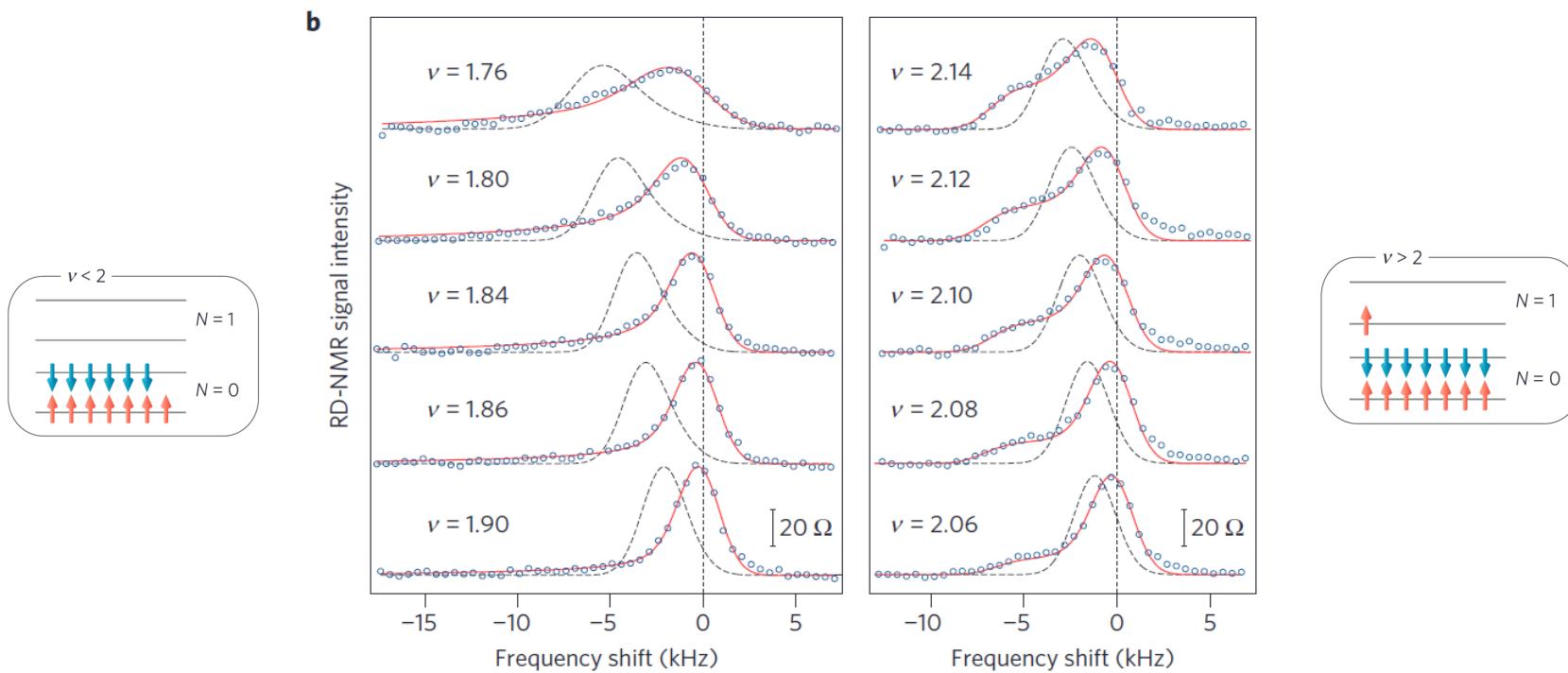
$N = 0 \text{ LL}, \nu = 1/3$



$N = 1 \text{ LL}, \nu = 3$

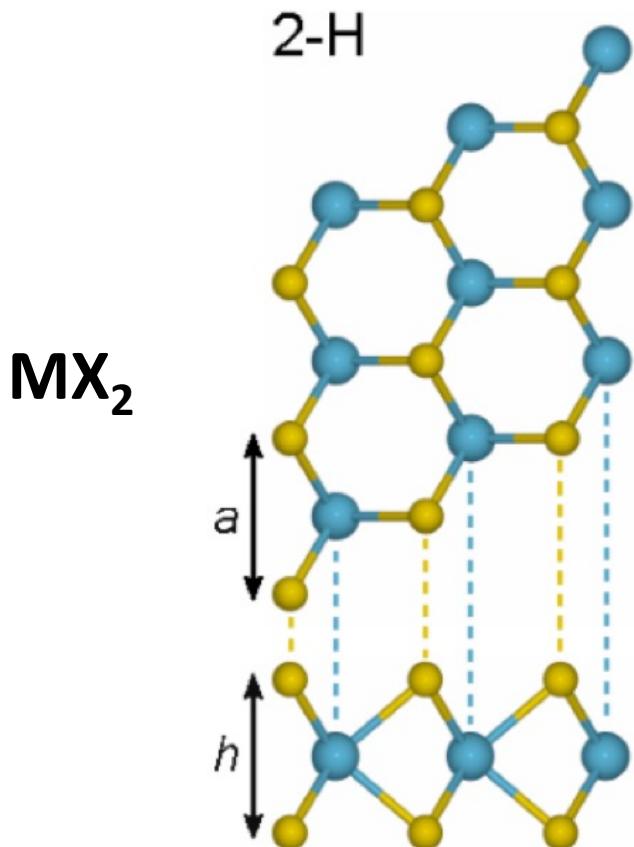


NMR probes Wigner Solids: *In-plane local density variations at $\nu \sim 2$*



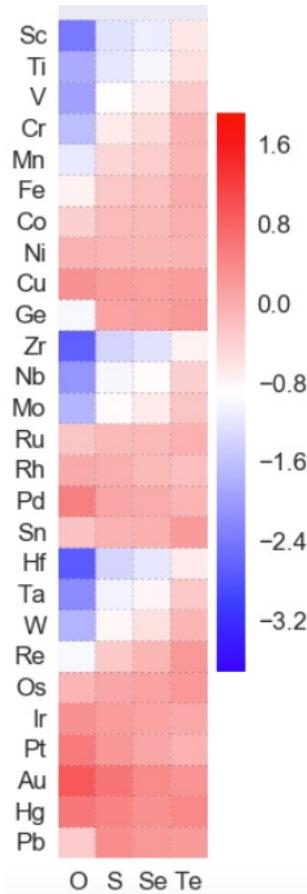
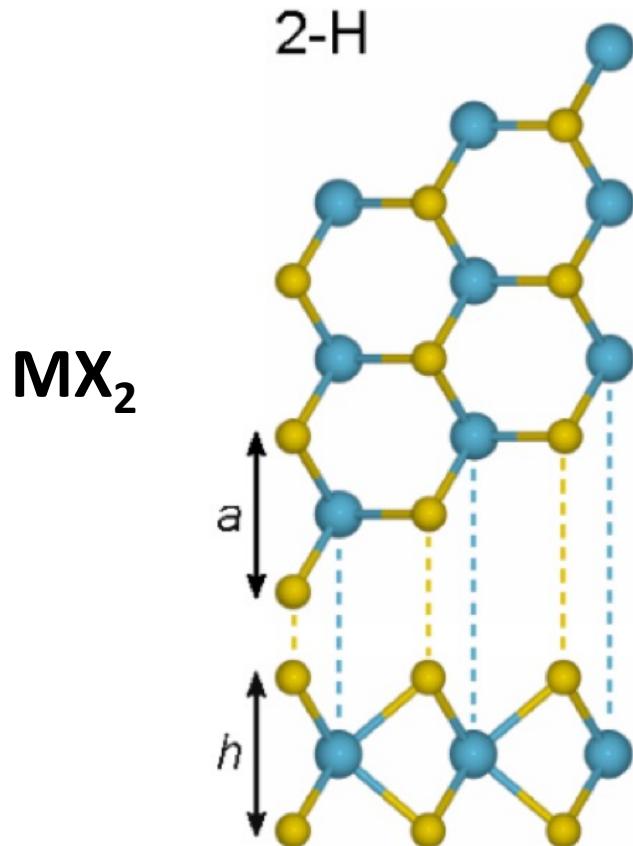
- 1) L. Tiemann^(*), T.D. Rhone^(*), N. Shibata, K. Muraki, Nature Physics, doi:10.1038/nphys3031
(*: equal contribution)

Dataset: Transition Metal Dichalcogenides (TMDs)



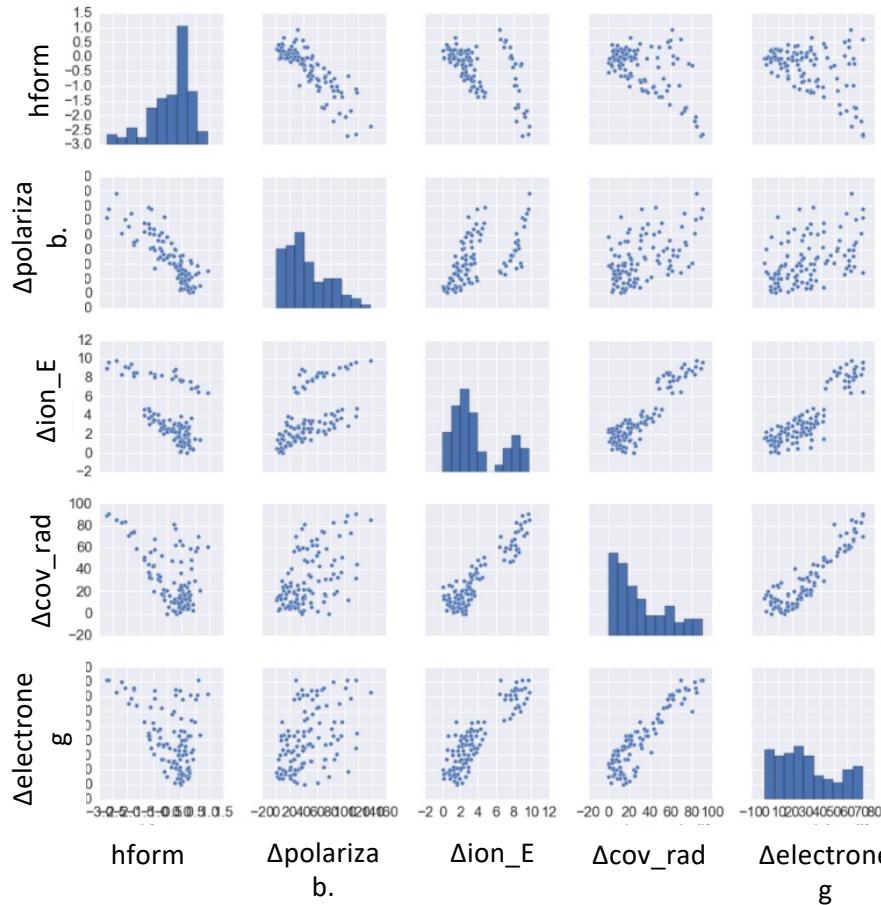
1 H																		2 He
3 Li	4 Be																	10 Ne
11 Na	12 Mg																	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
55 Cs	56 Ba	*	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	
87 Fr	88 Ra	**	104 Rf	105 Db	106 Sg	10d7 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Uut	114 Fl	115 Uup	116 Lv	117 Uus	118 Uuo	
*	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu			
**	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr			

Dataset: Transition Metal Dichalcogenides (TMDs)



Heat of Formation
of TMDs

Data visualization: TMDs

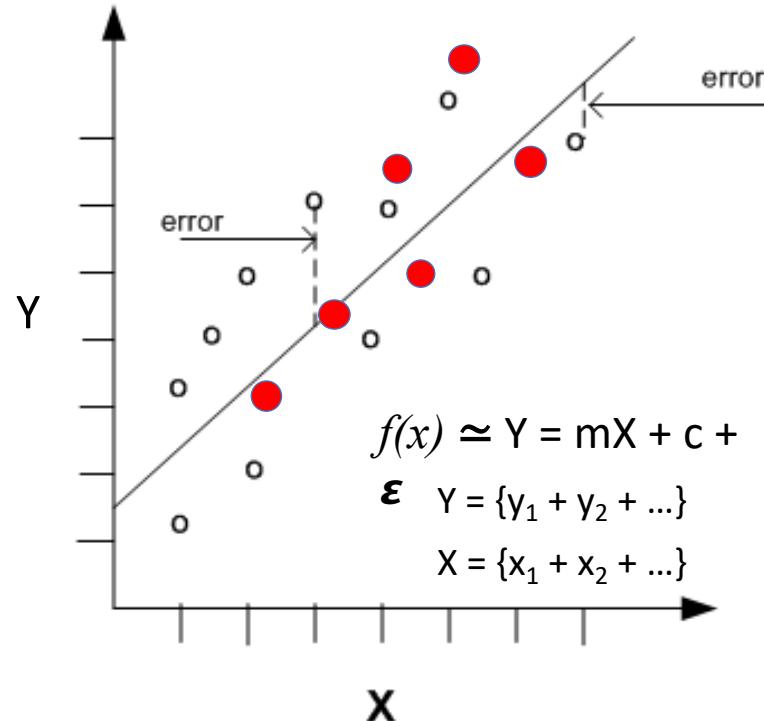


MX₂ materials ‘features’

- Atomic properties:
 - $\Delta x = x(M) - x(X)$
- x:
 - Polarizability
 - Ionization energy
 - Covalent radius
 - electronegativity

Machine Learning models

- Linear regression is a type of machine learning model
- Inputs: X
 - Dipole polarizability of A, B
- Output: Y
 - Heat of formation
- Training data
- Test data
- Algorithm estimates m & c
 - Reduce test error
 - $\min\{\sum_i(y_i - \hat{y}_i)^2\}$



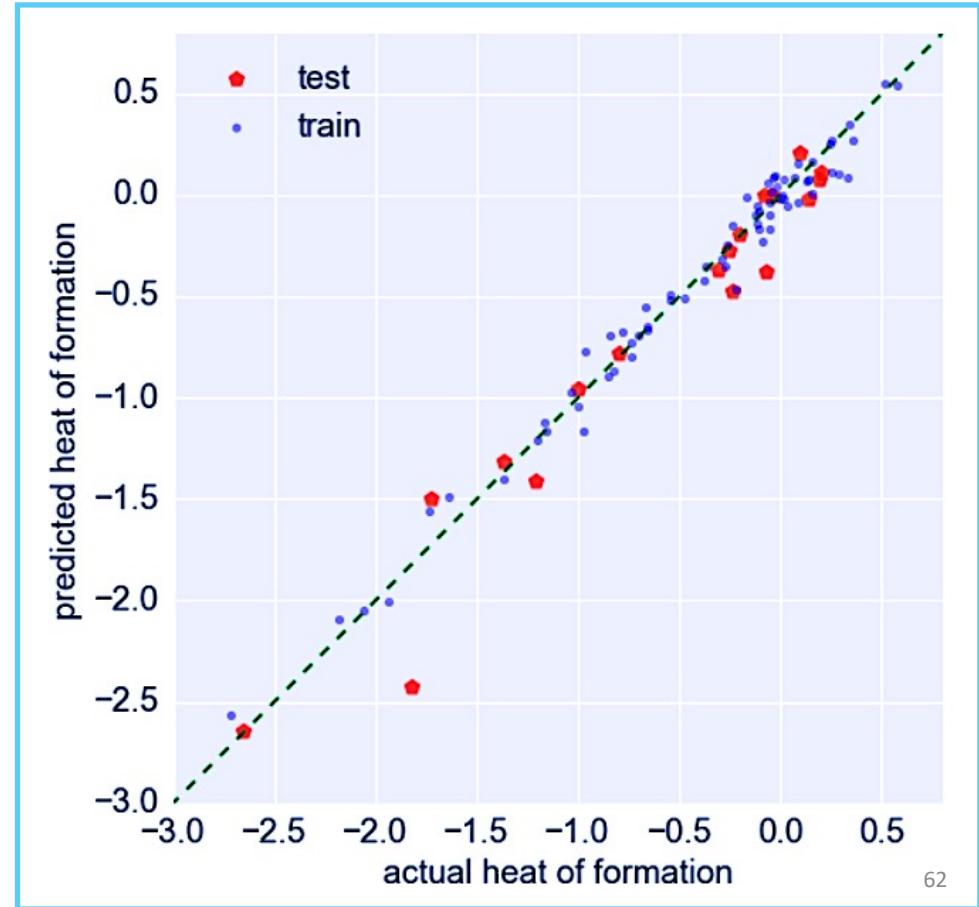
Machine learning TMD data to predict stability

Machine learning models

$$y = f(x_1, x_2, \dots, x_N)$$

Heat of formation

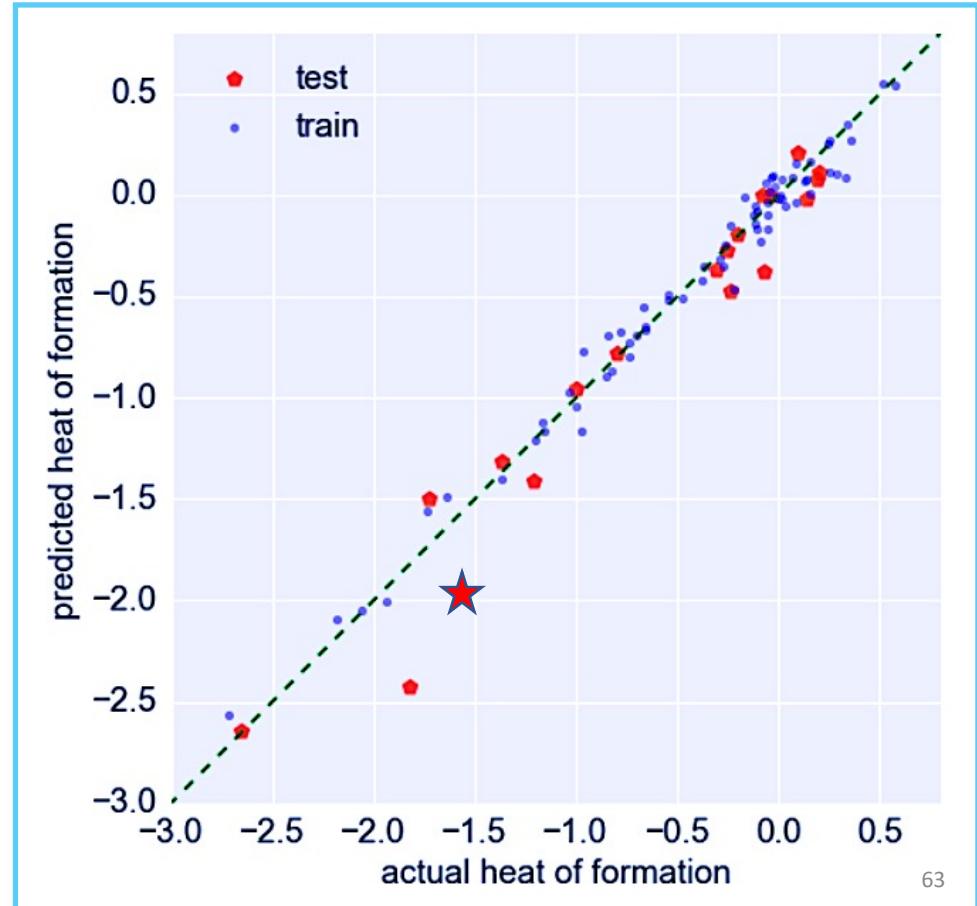
dipole polarizability difference
valence electrons difference
...
Electronegativity difference



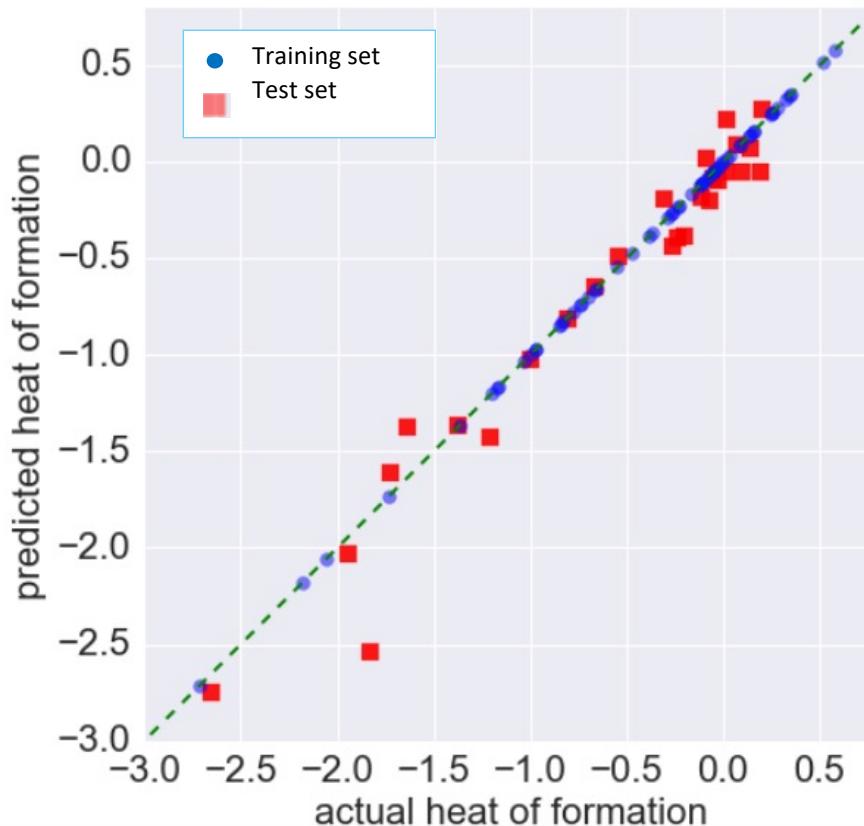
Machine learning TMD data to predict stability

Heat of formation of
Boron Nitride

- Predicted value: $-2eV$
- Expected value: $-1.56eV$



Machine Learning models: Kernel ridge regression



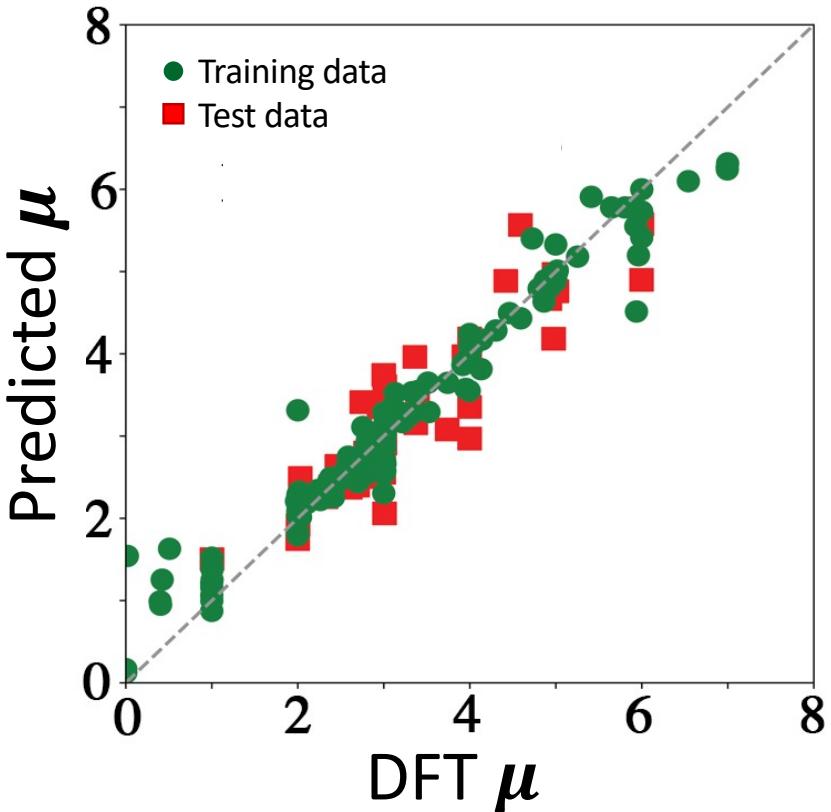
- # data points = 89
- # features = 30

$$C = \frac{1}{2} \sum_i (y_i - \mathbf{w}^T \mathbf{x}_i)^2 + \frac{1}{2} \lambda \|\mathbf{w}\|^2$$

Test score , $R^2 = 0.94$
Train score, $R^2 = 0.99$

Machine learning predictions

Magnetic moment, X=Te

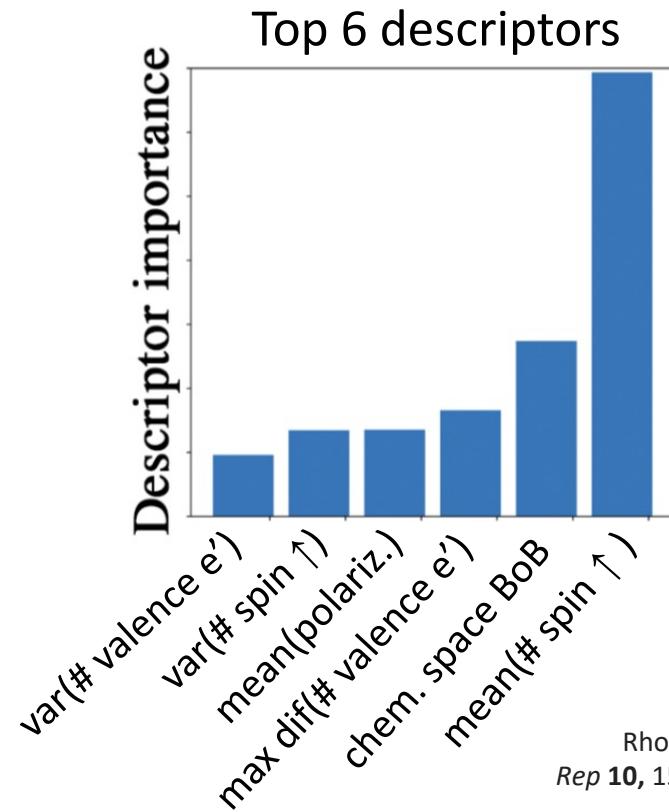
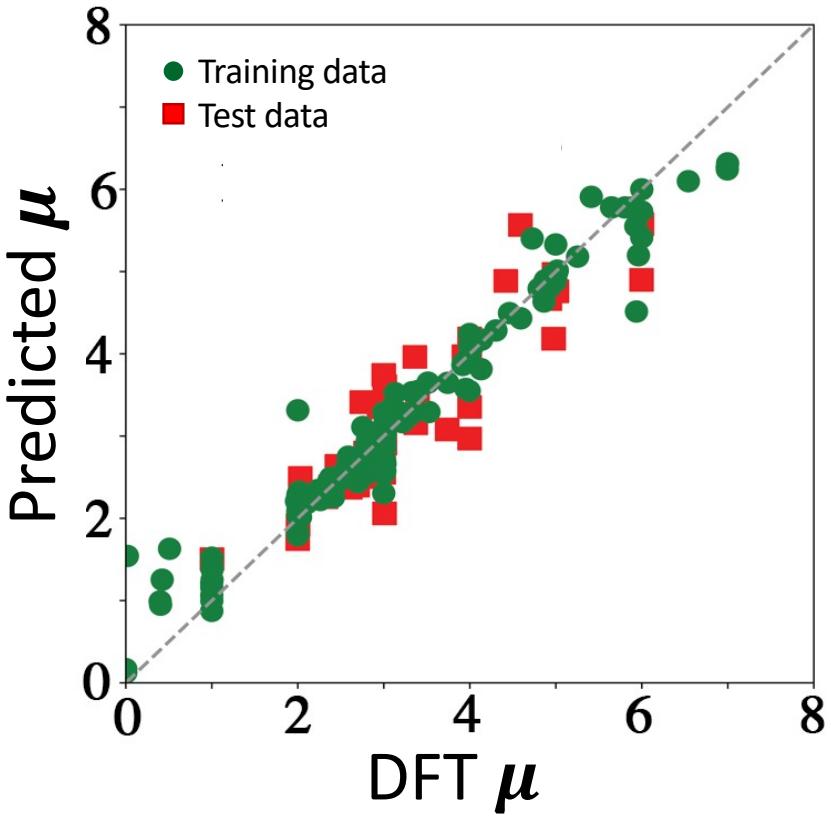


- $N = 262$
- Random forest $R^2 = 0.98$
- Mean absolute error
(MAE) = $0.30 \mu_B$

DFT: first-principles quantum calculations
 μ : magnetic moment \sim magnetization

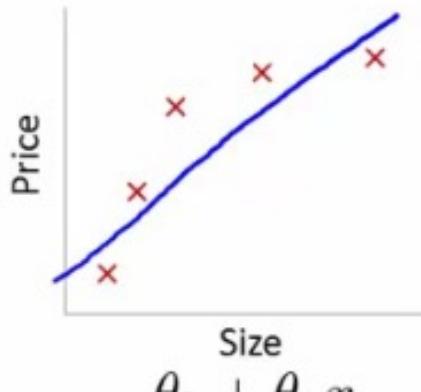
Machine learning predictions

Magnetic moment, X=Te

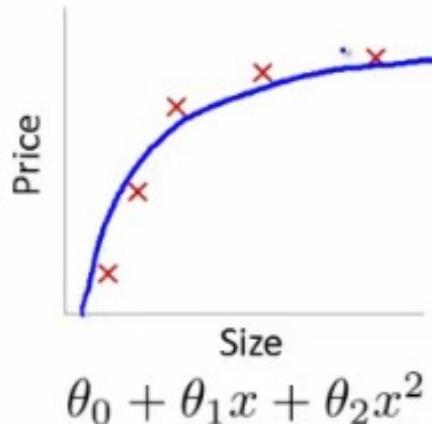


Machine Learning models: Kernel ridge regression

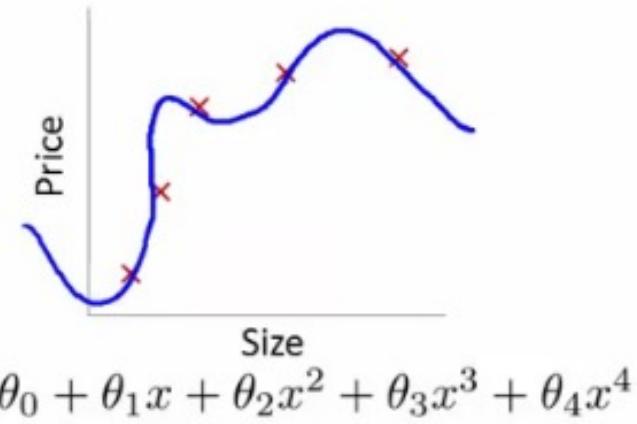
Overfitting



High bias
(underfit)

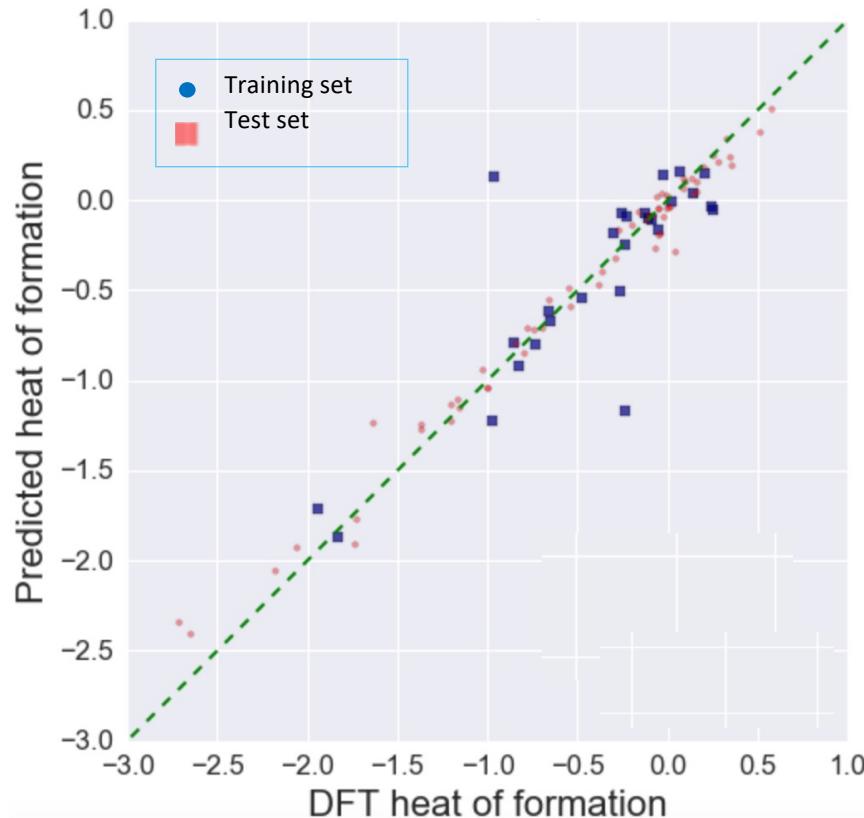


"Just right"



High variance
(overfit)

Machine Learning models: Random forest regression



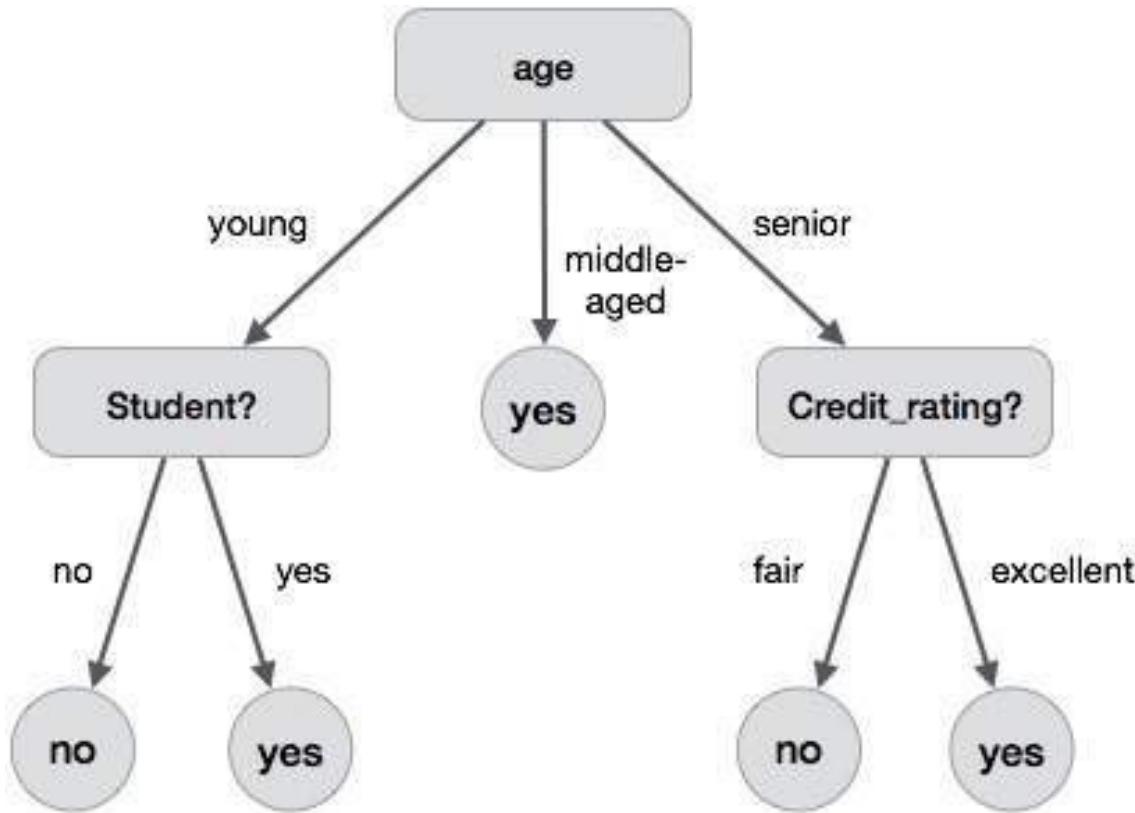
Random forest
regression is based on
decision trees

- # data points = 89
- # features = 39

Test score, MSE = 0.095

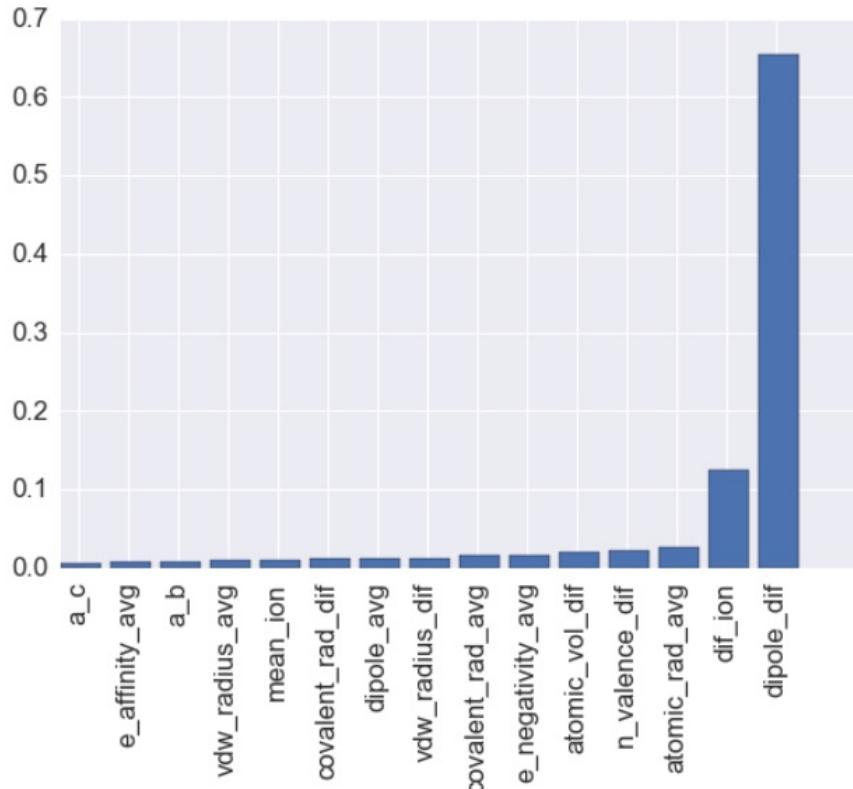
Random Forest model and Decision Trees

Is a customer at a company likely to buy a computer or not?



Machine Learning models: Random forest regression

Feature Importances



Top ten descriptors

- 1 Dipole dif
- 2 Dif in ionization E
- 3 atomic radius avg
- . num valence dif
- . atomic vol dif
- . e_negativity avg
- covalent rad avg
- vdw radius dif
- dipole avg
- 10 covalent rad dif

Machine Learning models

Challenges

1. Can our ML models generalize to other 2D materials?
2. Are our descriptors sufficient?
3. Develop descriptors to describe crystal structure?

Top ten descriptors

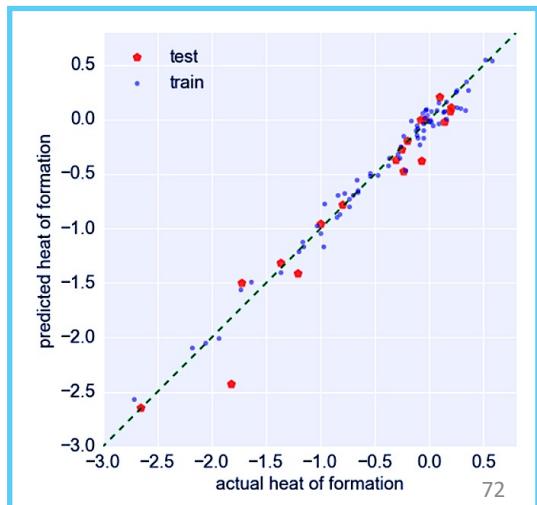
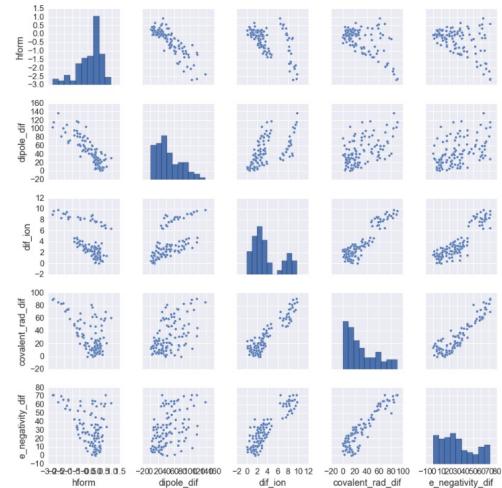
- | | |
|----|---------------------|
| 1 | Dipole dif |
| 2 | Dif in ionization E |
| 3 | atomic radius avg |
| . | num valence dif |
| . | atomic vol dif |
| . | e_negativity avg |
| | covalent rad avg |
| | vdw radius dif |
| | dipole avg |
| 10 | covalent rad dif |

Summary

- Materials informatics

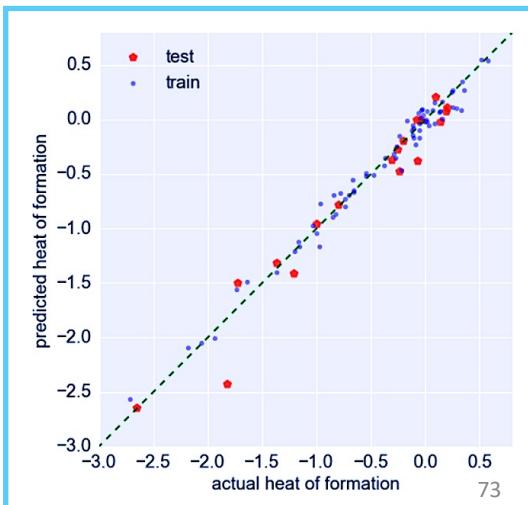
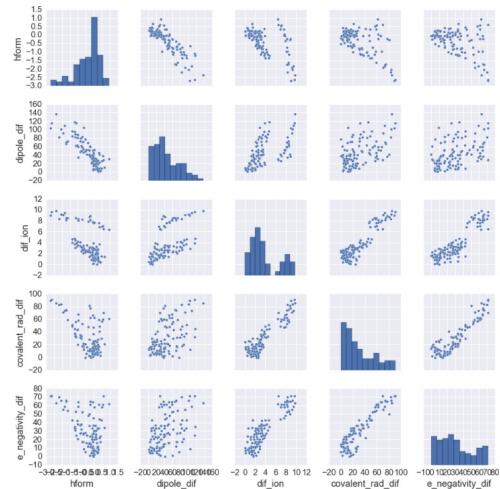
- Identified and exploited trends in materials' properties data for vdW materials
- Predicted heat of formation of TMDs

- Materials databases + access to machine learning tools makes materials informatics possible



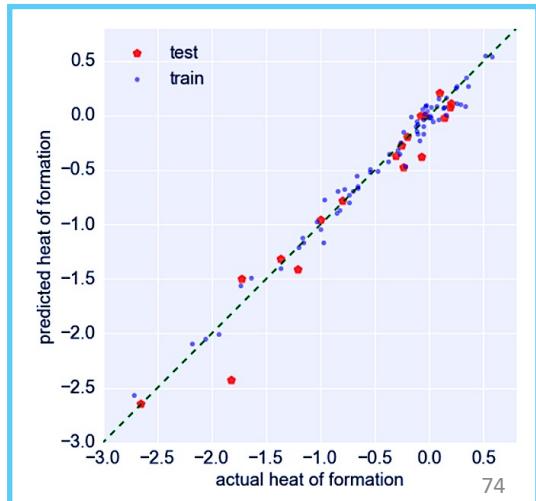
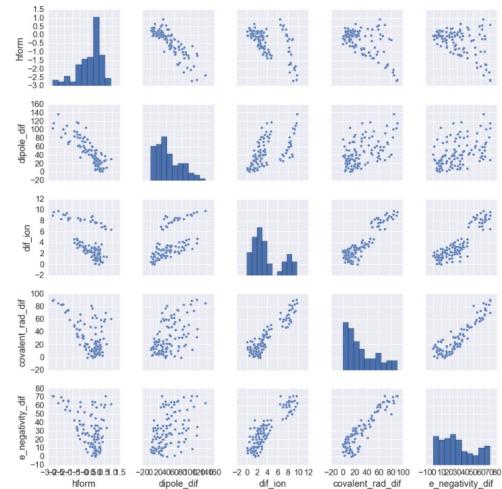
Outlook

- Discovery of new 2D materials?
- Tailor 2D materials to have desired properties?
- Use statistical inference to guide the discovery of new physics?



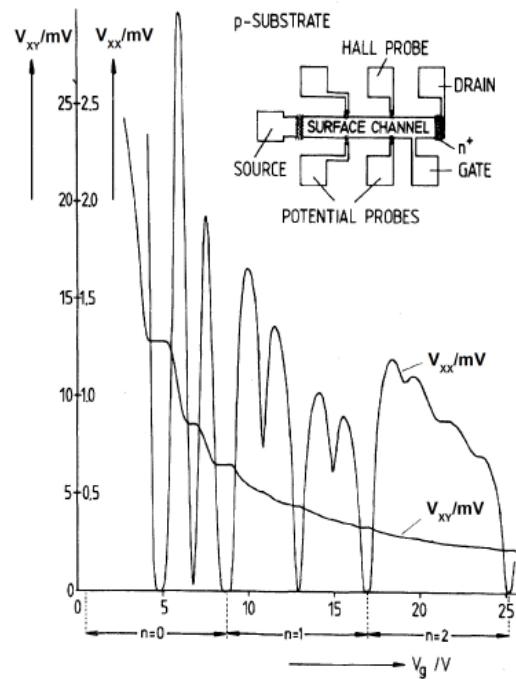
Outlook

- Academic research
 - Universities
 - Materials Project (Materials Genome Initiative)
 - NIMS
- Industry
 - Citrine
 - Google
 - Applications:
 - ❖ Photovoltaics
 - ❖ Thermoelectrics
 - ❖ Organic LEDs
 - ❖ Magnetocalorics



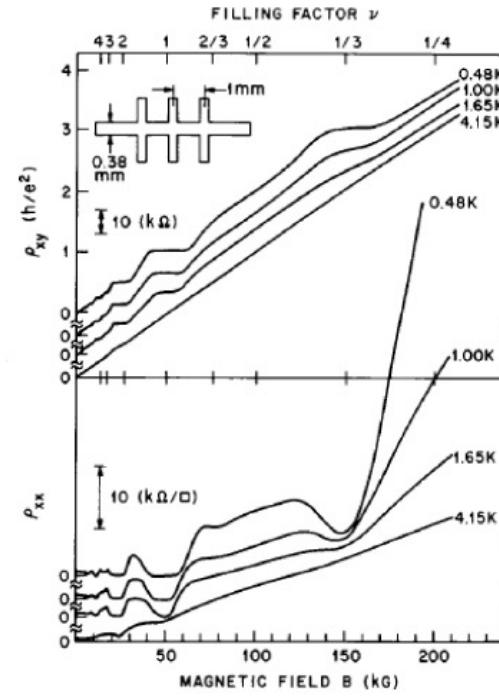
2DES in a magnetic field: Integer Quantum Hall Effect

Integer Quantum Hall Effect



1. K. von Klitzing, G. Dorda, and M. Pepper. New method for high-accuracy determination of the fine-structure constant based on quantized Hall resistance. Phys. Rev. Lett., 45(494), 1980.

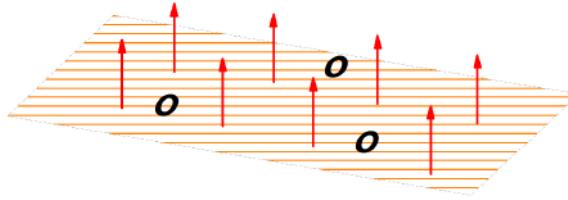
Fractional Quantum Hall Effect



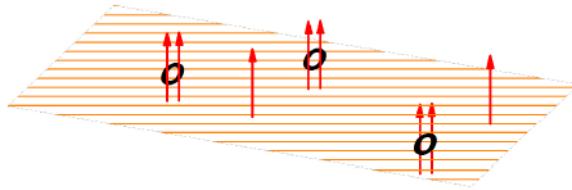
2. D.C. Tsui, H.L. Stormer, and A.C. Gossard. Two-dimensional magnetotransport in the extreme quantum limit. Phys. Rev. Lett., 48 (1559), 1982.

Emergent Quasiparticles: Composite Fermions

Electrons in a
strong B field



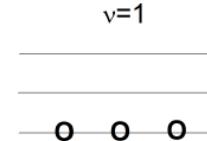
Composite Fermions
in a weak B^* field



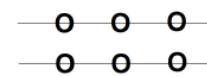
$$\text{IQHE} \quad \Psi_{\nu=1} = \prod_{j < k} (z_j - z_k) \exp \left[\frac{-1}{4l_o^2} \sum_l |z_l|^2 \right]$$

$$\text{FQHE} \quad \Psi_{p/(\phi p+1)} = \hat{P}_{LLL} \prod_{j < k} (z_j - z_k)^{\phi} \Psi_{\nu=p}$$

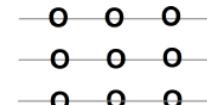
IQHE



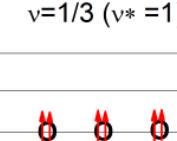
$\nu=2$



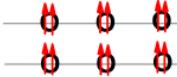
$\nu=3$



FQHE



$\nu=2/5 (\nu^* = 2)$

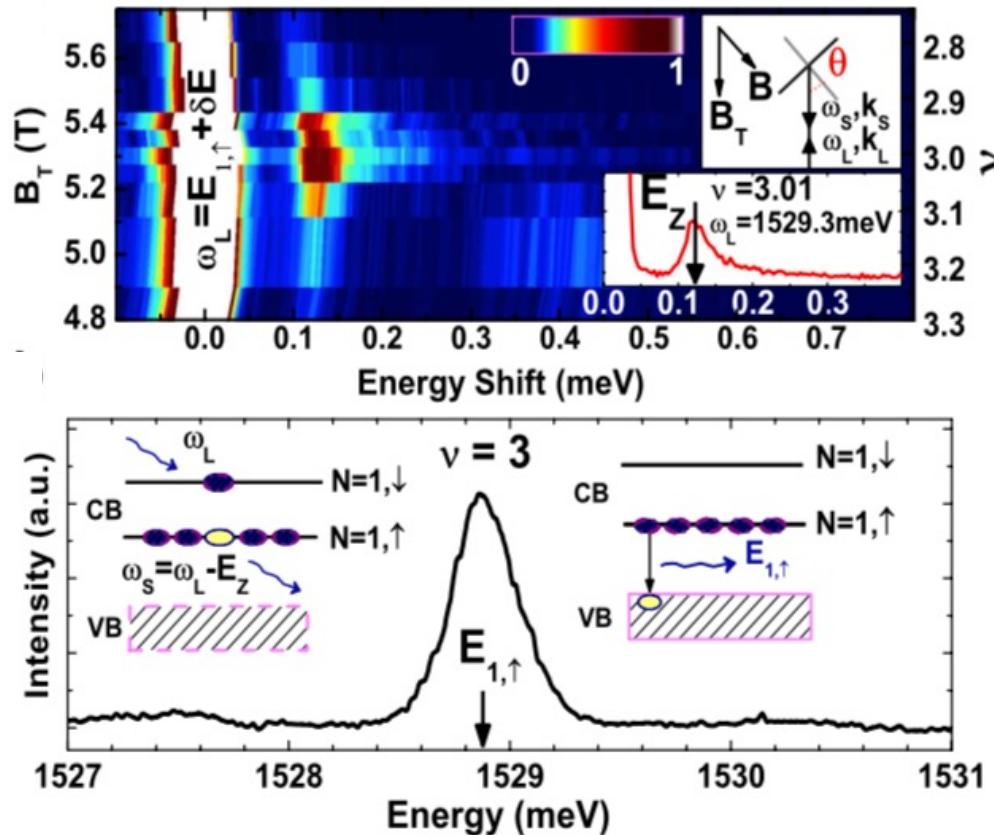


$\nu=3/7 (\nu^* = 3)$

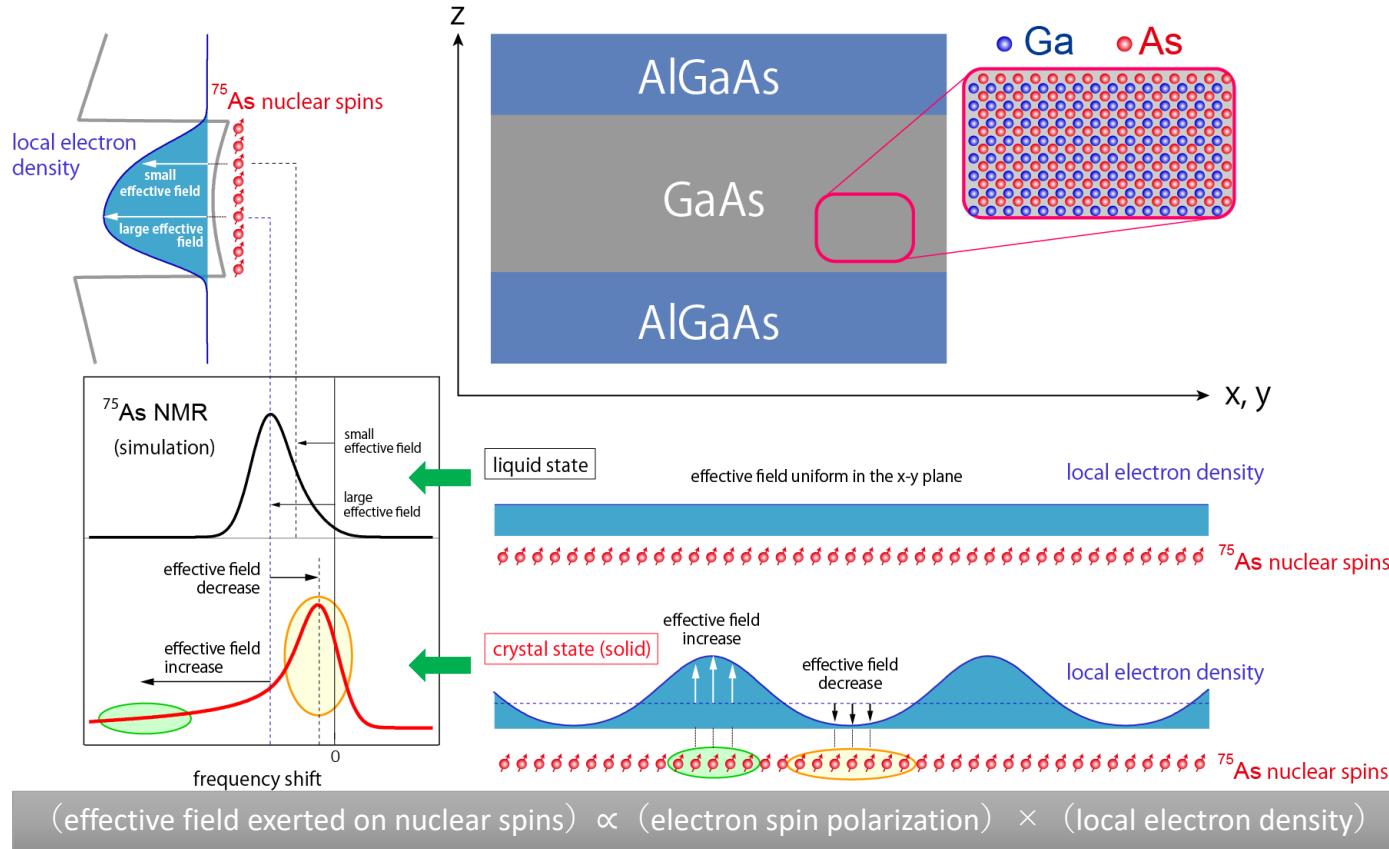


$$\nu^* = n\phi_o / |B^*| \quad \nu = \frac{\nu^*}{\phi\nu^* \pm 1}.$$

Spin properties of 2DES



Resistively detected NMR (RDNMR) as a Local Density Probe



Resistively Detected NMR (RD-NMR)

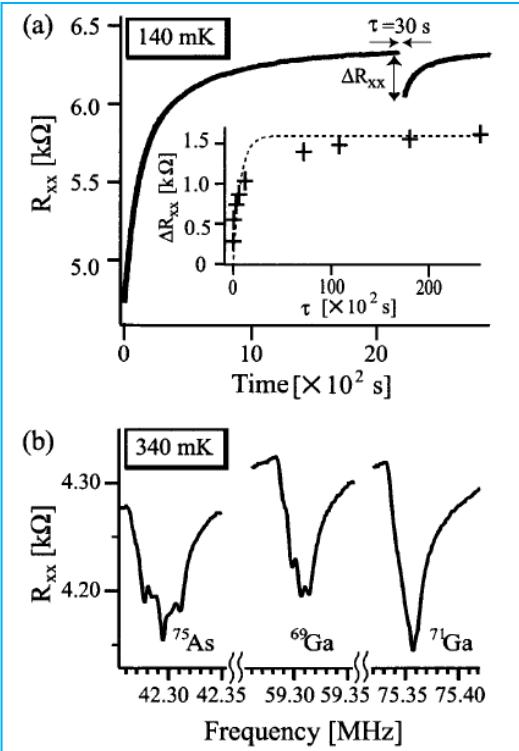
VOLUME 88, NUMBER 17

PHYSICAL REVIEW LETTERS

29 APRIL 2002

Electrically Controlled Nuclear Spin Polarization and Relaxation by Quantum-Hall States

K. Hashimoto,^{1,2,*} K. Muraki,¹ T. Saku,¹ and Y. Hirayama^{1,2}



$$E_z = g\mu_B(B_0 + b_n \langle I_z \rangle)$$

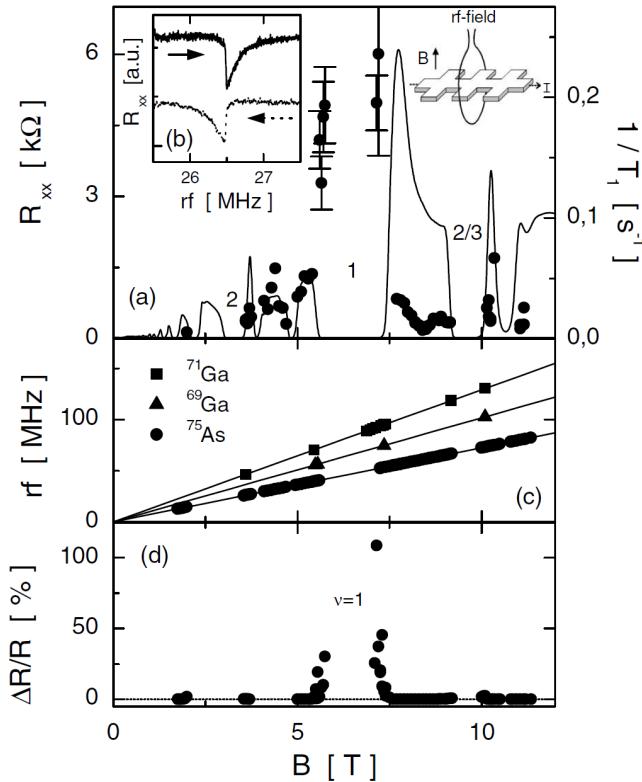
$$\Delta E_z \propto \Delta \langle I_z \rangle$$

if $\Delta R_{xx} \propto \Delta E_z$, then $\Delta R_{xx} \propto \Delta \langle I_z \rangle$

only applicable to those states with:

- sensitivity to ΔE_z
- finite R_{xx}

Resistively Detected NMR (RD-NMR)



$$E_z = g\mu_B(B_0 + b_n \langle I_z \rangle)$$

$$\Delta E_z \propto \Delta \langle I_z \rangle$$

if $\Delta R_{xx} \propto \Delta E_z$, then $\Delta R_{xx} \propto \Delta \langle I_z \rangle$

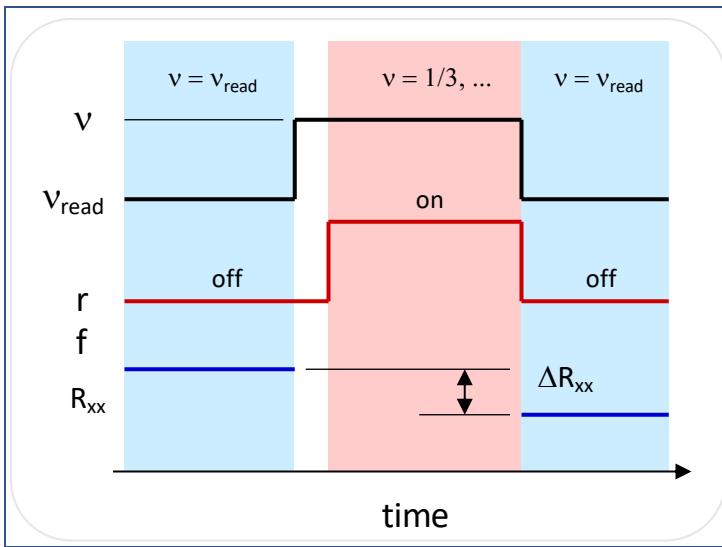
only applicable to those states with:

- sensitivity to ΔE_z
- finite R_{xx}

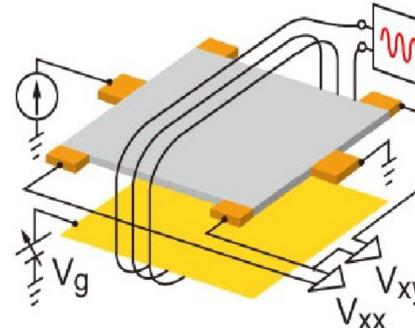
Our Method: Modified RD-NMR

Key idea:

Use gate voltage to go to a different filling factor ν_{read} for the readout



Detect resonant rf absorption at ν as a change in R_{xx} at ν_{read}

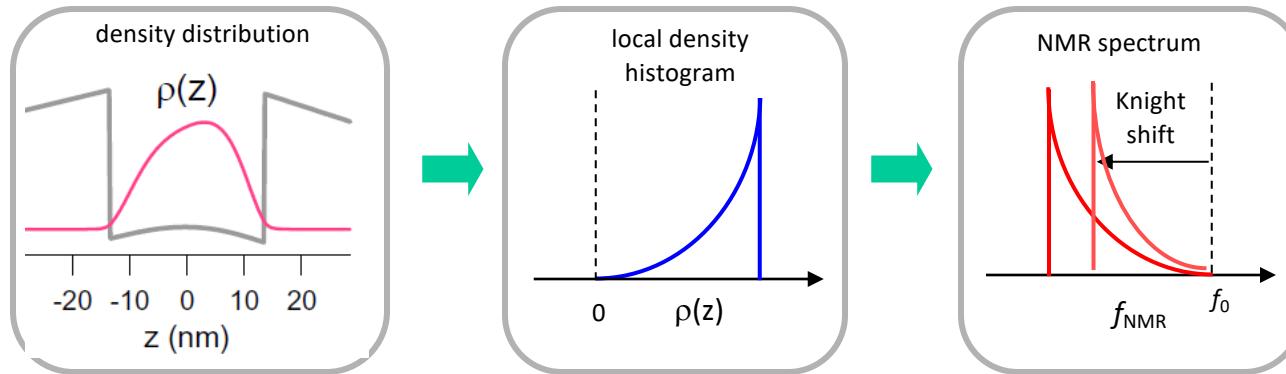


- Nuclear spins interact with electron spins at $\nu_{\text{read}}=2/3$
- R_{xx} at ν_{read} can be used to measure spin degrees of freedom

NMR Line Shape

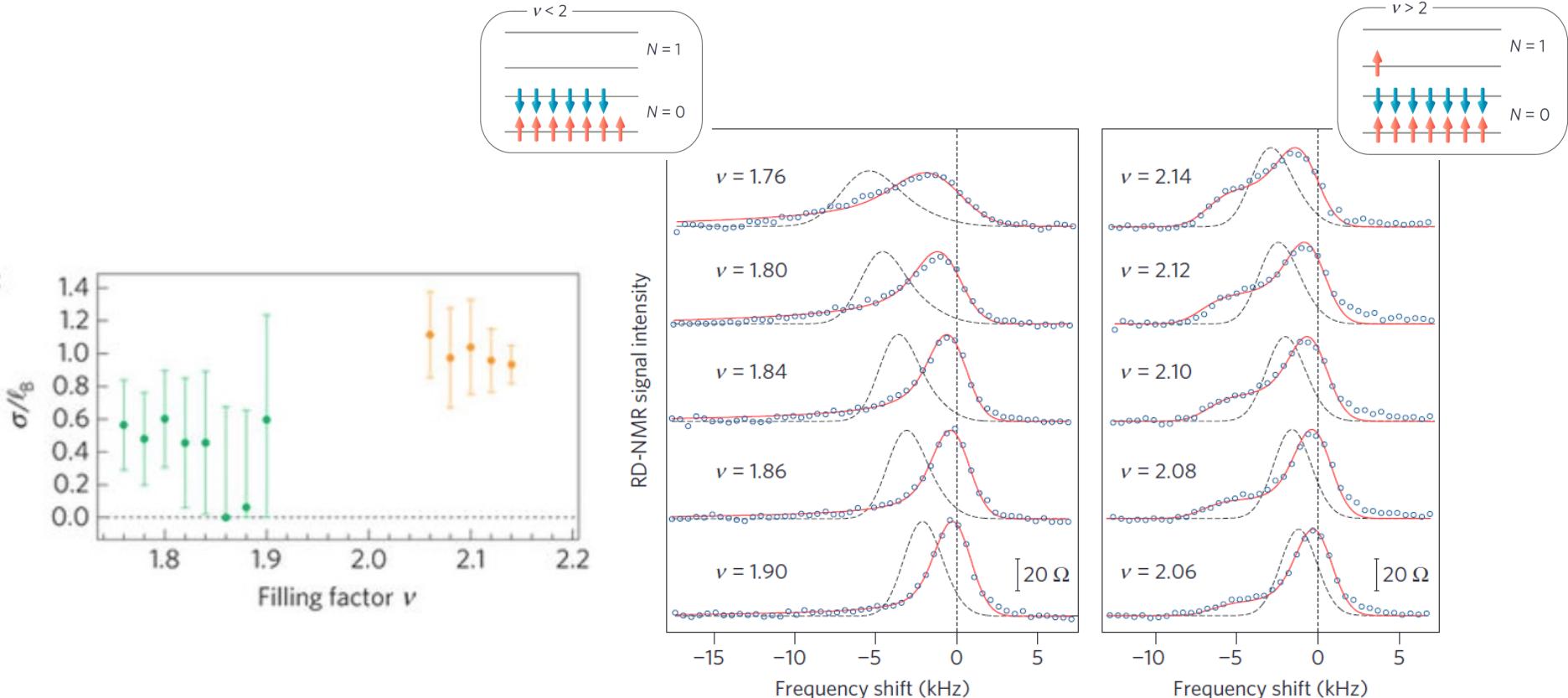
$$K_s(\mathbf{r}) \text{ (Knight shift of nucleus at position } \mathbf{r} \text{)} = \alpha_v \text{ (spin polarization * n)} \times \rho(\mathbf{r}) \text{ (local probability density)}$$

$$P = \alpha_v / \alpha_{\max,v}$$



- For $P > 0$, NMR line shape \cong mirror image of local density histogram
- spectral mapping of subband wavefunction

NMR probes Wigner Solids: *In-plane local density variations at $v \sim 2$*



- 1) L. Tiemann^(*), T.D. Rhone^(*), N. Shibata, K. Muraki, Nature Physics, doi:10.1038/nphys3031
(*: equal contribution)

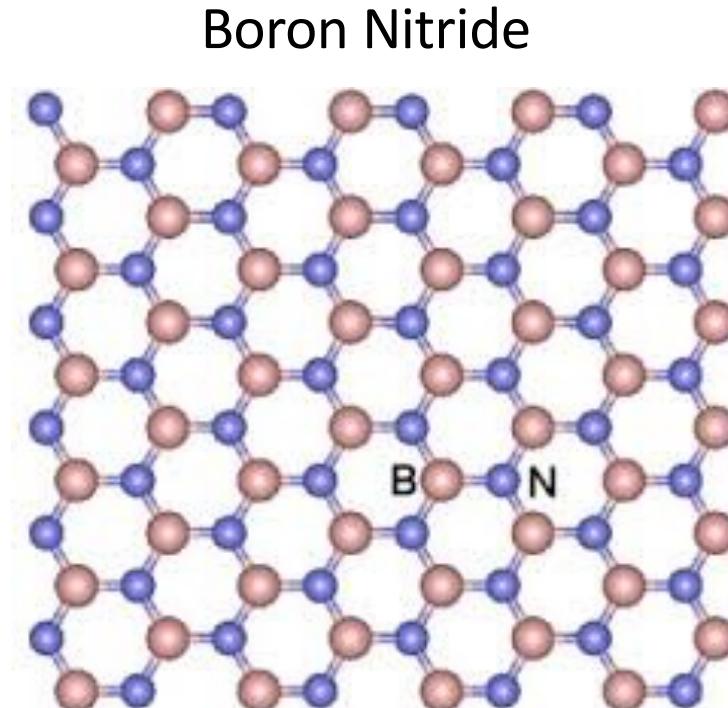
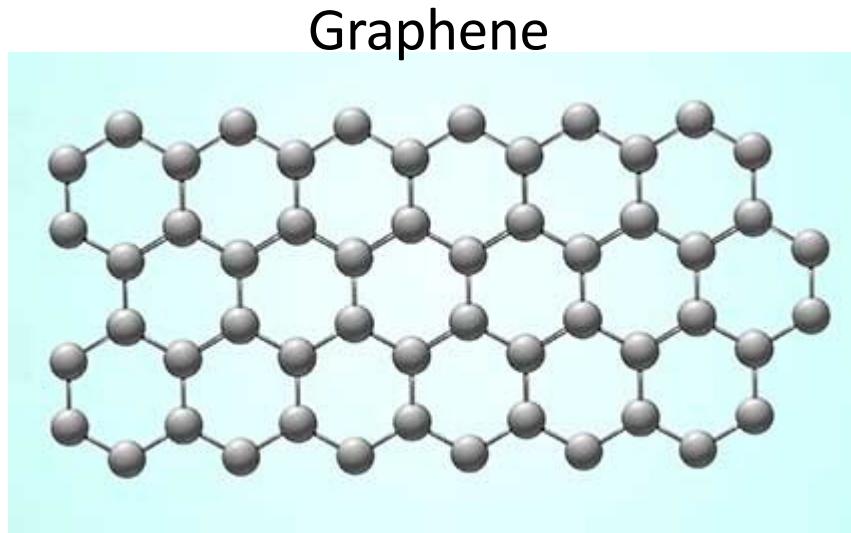
"I Keep Six Honest Serving Men ..."

I keep six honest serving-men
(They taught me all I knew);
Their names are What and Why and When
And How and Where and Who...

by Rudyard Kipling

Crystal structure and materials properties

- Structure-property relationships:



Total set of descriptors

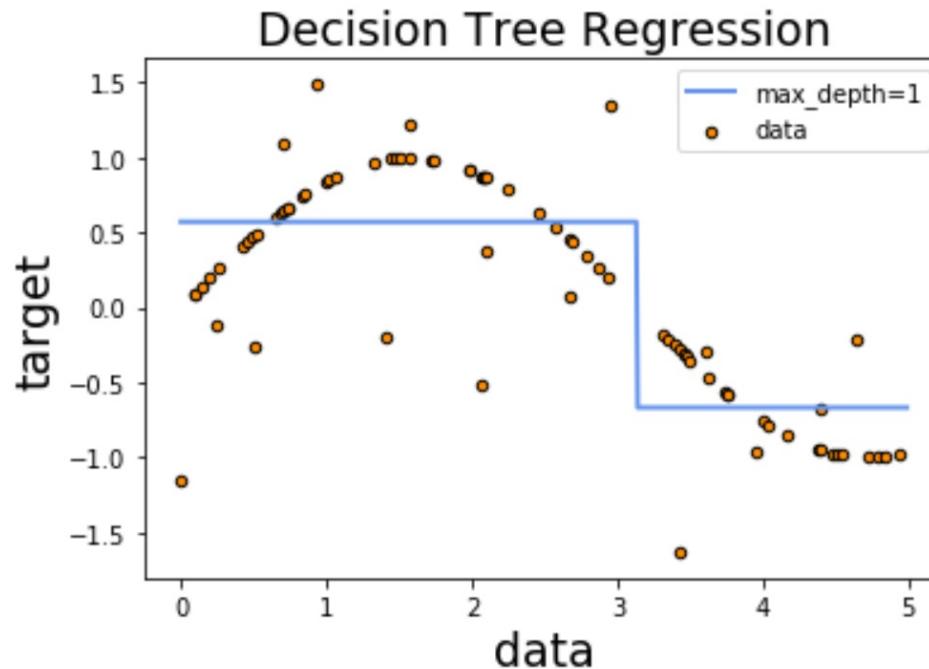
1 num_p	21 covalentrad_max_dif	41 e_negativity_max_dif	55 atomE_AB
2 num_d	22 covalentrad_sum_dif	42 e_negativity_sum_dif	56 frac_f
3 num_f	23 covalentrad_std_dif	43 e_negativity_std_dif	57 std_ion
4 atomic_rad	24 covalentrad_std	44 e_negativity_std	58 cmpd_sigma_d
5 atomic_vol	25 dipole_avg	45 nvalence_avg	59 cmpd_sigma_f
6 covalent_rad	26 dipole_max_dif	46 nvalence_max_dif	60 sum_ion
7 dipole	27 dipole_sum_dif	47 nvalence_sum_dif	61 mean_ion
8 eaffinity	28 dipole_std_dif	48 nvalence_std_dif	
9 num_electrons	29 dipole_std	49 nvalence_std	
10 atomic_rad_avg	30 numelectron_avg	50 lastsubshell_avg	
11 atomic_rad_max_dif	31 numelectron_max_dif	51 cmpd_skew_p	
12 atomic_rad_sum_dif	32 numelectron_sum_dif	52 cmpd_skew_d	
13 atomic_rad_std_dif	33 numelectron_std_dif	53 cmpd_skew_f	
14 atomic_rad_std	34 numelectron_std	54 cmpd_sigma_p	
15 atomic_vol_avg	35 vdwradius_avg		
16 atomic_vol_max_dif	36 vdwradius_max_dif		
17 atomic_vol_sum_dif	37 vdwradius_sum_dif		
18 atomic_vol_std_dif	38 vdwradius_std_dif		
19 atomic_vol_std	39 vdwradius_std		
20 covalentrad_avg	40 e_negativity_avg		

Reduced set of descriptors

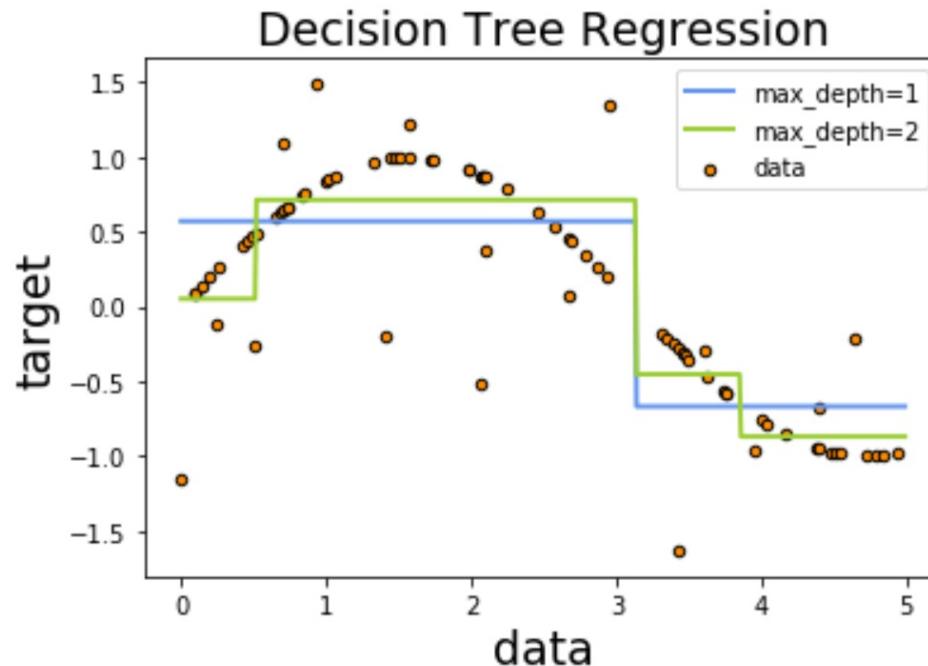
1 covalentrad_max_dif
2 hardness_var
3 hardness_mean
4 covalentrad_avg
5 sum_ion
6 Nup_mean
7 Nup_var
8 atomic_rad_std_dif
9 atomic_vol_avg
10 atomic_vol_max_dif

11 nvalence_std_dif
12 dipole_std
13 covalentrad_std_dif
14 dipole_max_dif
15 nvalence_sum_dif
16 atomic_vol_std_dif
17 nvalence_max_dif
18 atomic_vol_sum_dif
19 nvalence_std
20 nvalence_avg

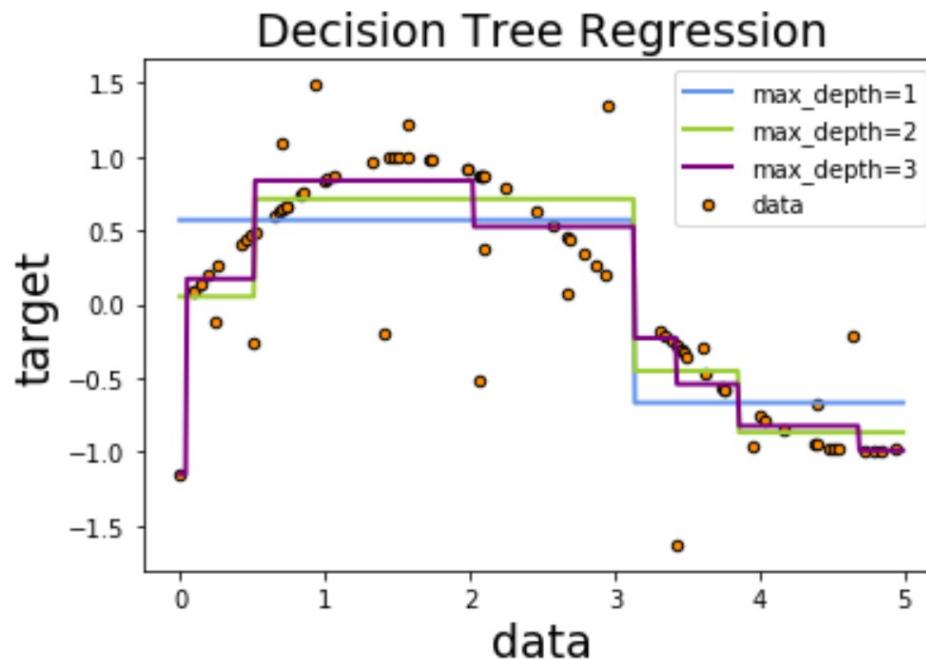
Random Forests Regression



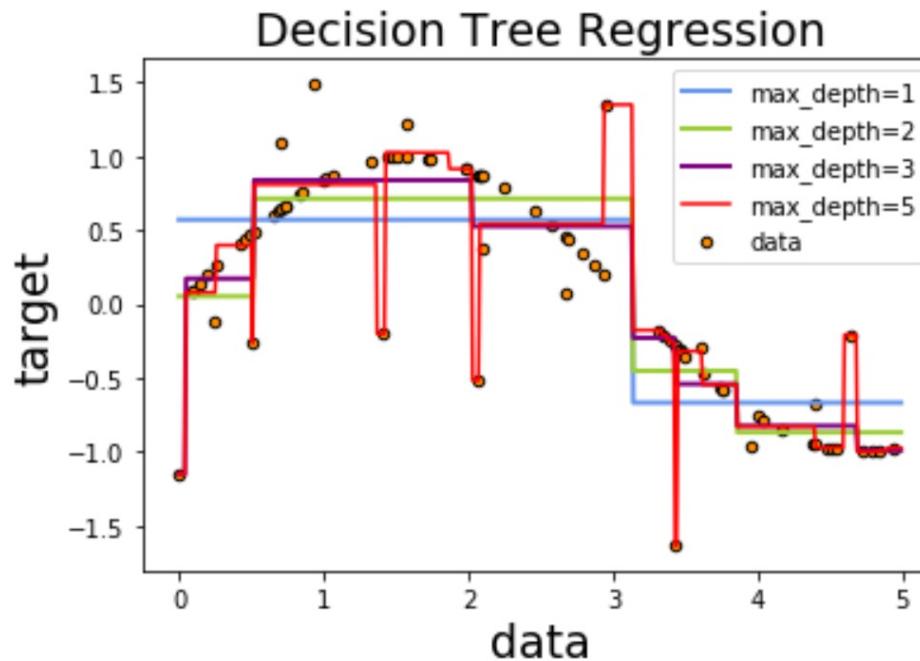
Random Forests Regression



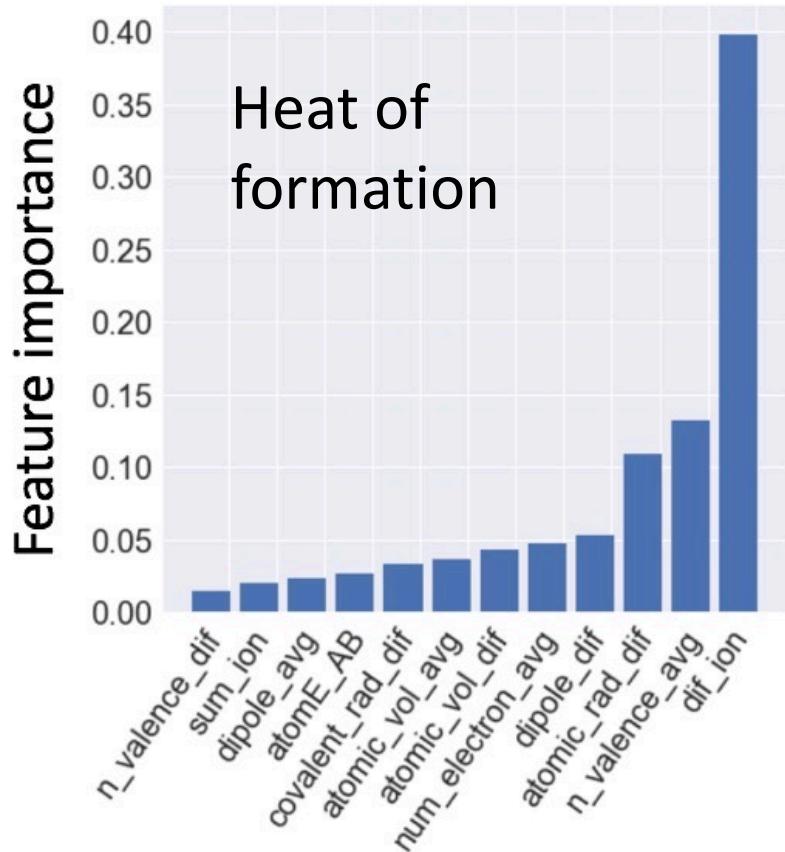
Random Forests Regression



Random Forests Regression



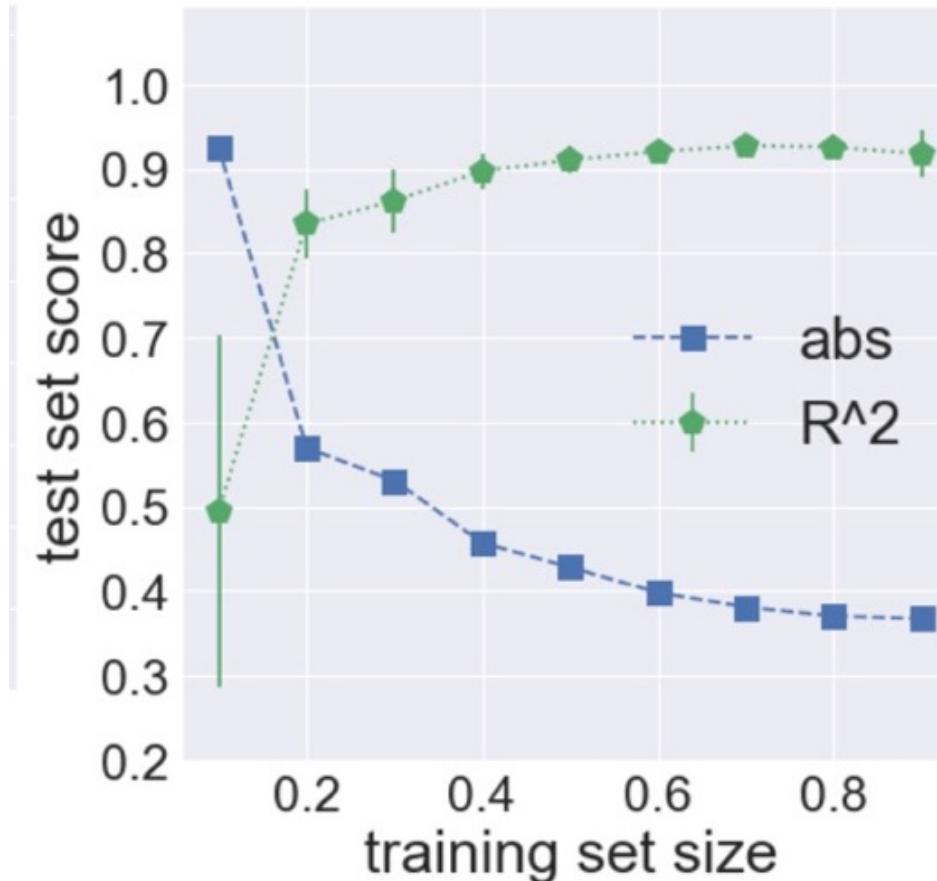
Extra forest regression: Feature extraction



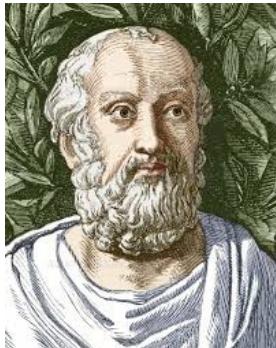
Feature Importance Ranking:

1. Ionization energy dif.
2. # valence electrons avg.
3. Atomic radius dif.
4. Dipole polarizability dif
5. Num of electrons avg.
6. Atomic volume avg
7. Covalent radius dif
8. Atom E_AB
9. Dipole poarizability avg
10. Ionization energy sum
11. # of valence electrons dif

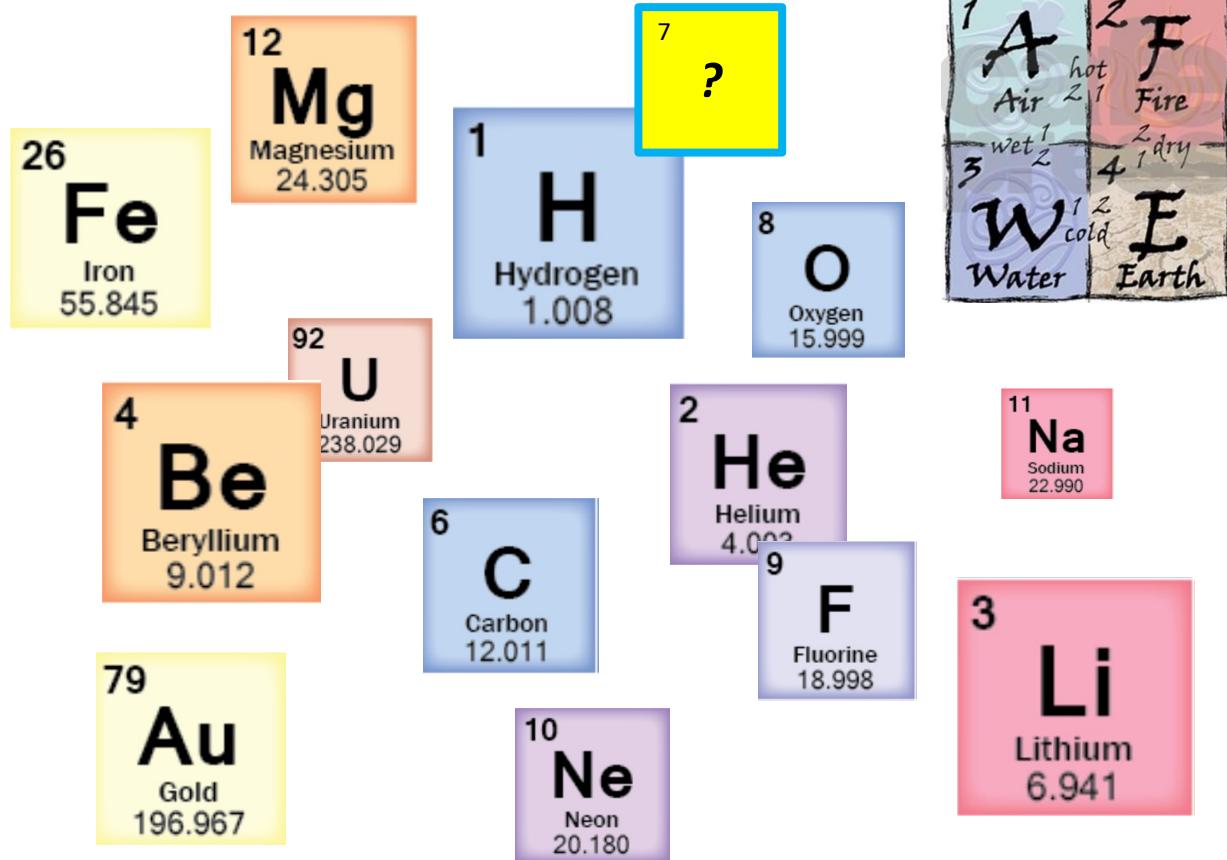
Test score vs training set size



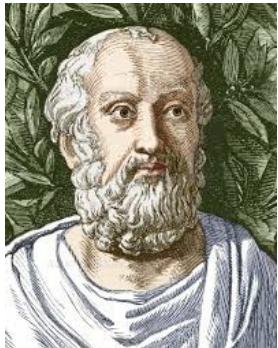
Where and who of Materials Informatics



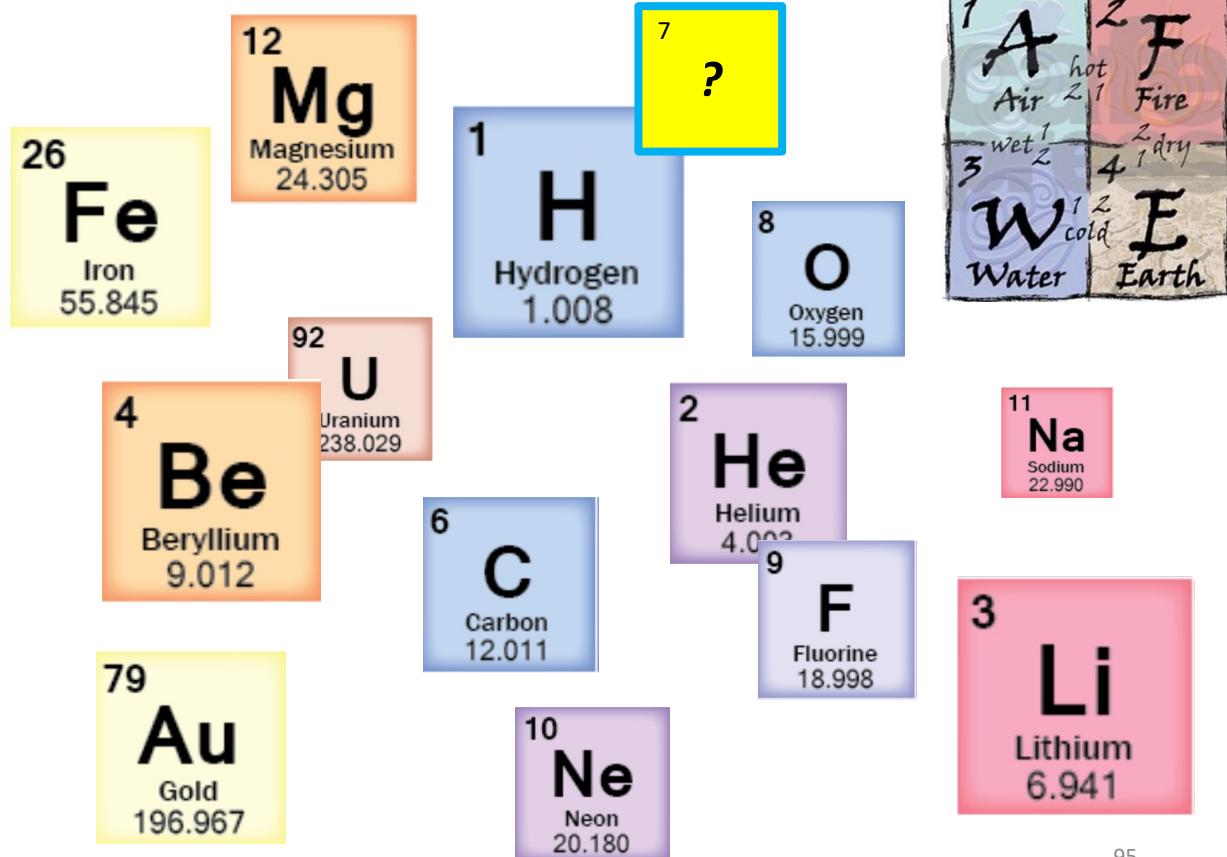
- You are an alchemist living in ancient Greece
- You have a small random set of elements



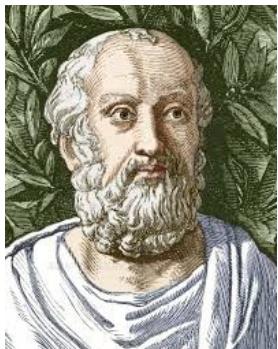
Where and who of Materials Informatics



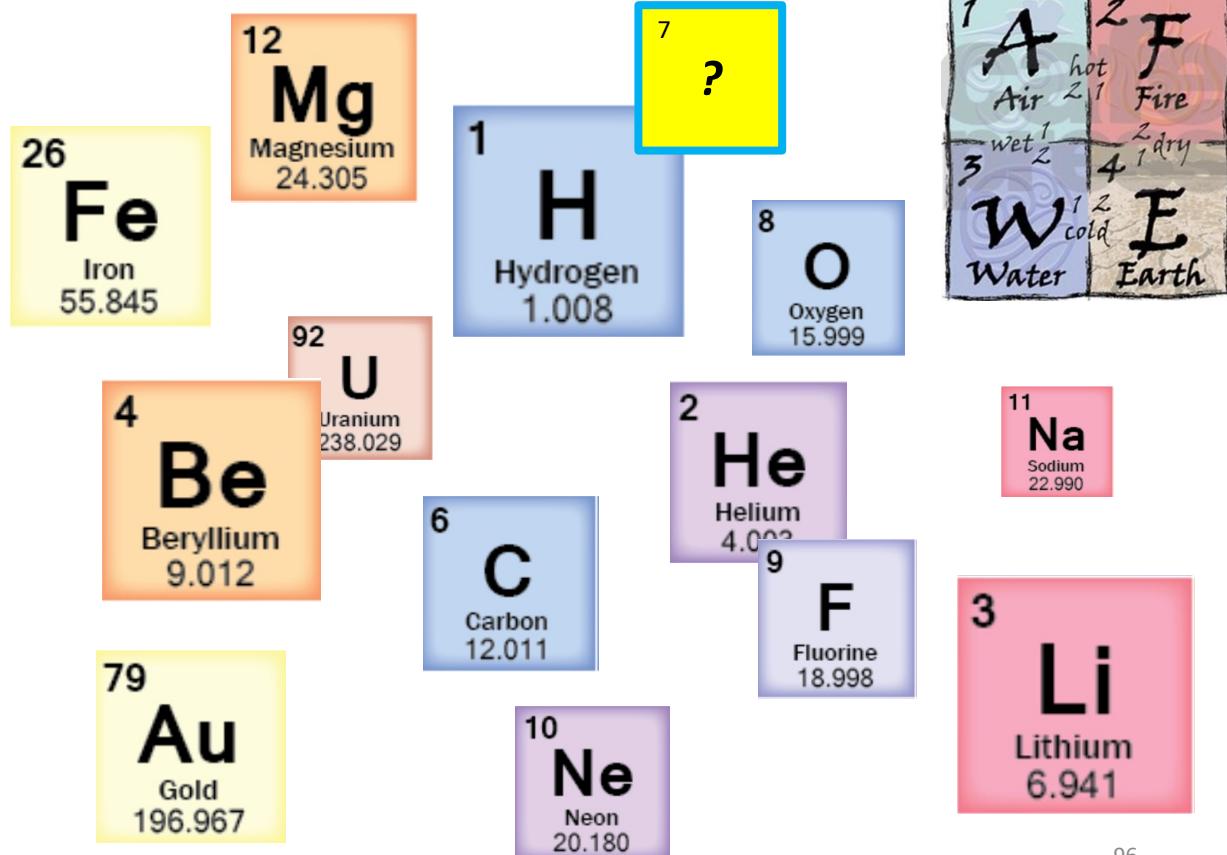
- What is a good descriptor?
- What are trends in the data?



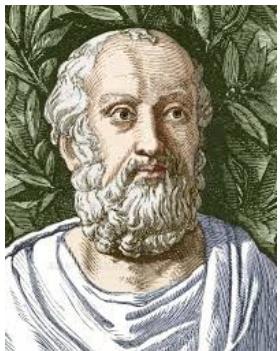
Where and who of Materials Informatics



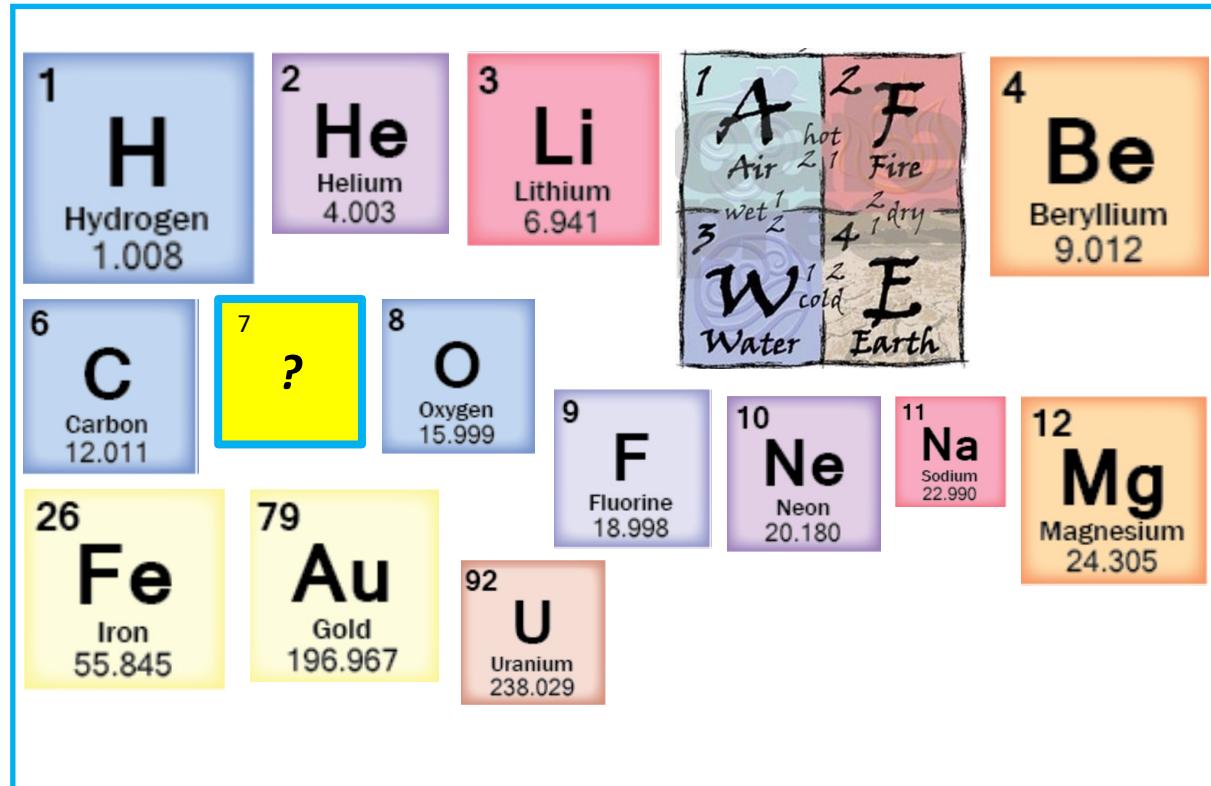
- Descriptor:
 - Atomic number
- Apply a model:
 - Sort atomic numbers



Where and who of Materials Informatics



- Descriptor:
 - Atomic number
- Apply a model:
 - Sort atomic numbers



Where and who of Materials Informatics

- Descriptor:

- Atomic number

- Apply a model:

- Sort atomic numbers

Periodic Table of the Elements

The Periodic Table of the Elements displays 103 elements arranged in 18 groups. The groups are color-coded: IA (blue), IIA (orange), IIIA (light blue), IVA (yellow), VA (green), VIA (purple), VIIA (pink), and VIIIA (light purple). The table includes the following series:

- Lanthanide Series:** Elements 57 (La) through 71 (Lu).
- Actinide Series:** Elements 89 (Ac) through 103 (Lr).

Each element cell contains its symbol, name, atomic number, and atomic mass.

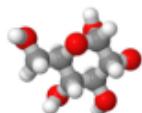
Group	Element	Symbol	Name	Atomic Number	Atomic Mass
1 IA	Hydrogen	H	Hydrogen	1	1.008
2 IIA	Boron	B	Boron	13	10.811
3 IIIB	Silicon	Si	Silicon	14	28.086
4 IVB	Phosphorus	P	Phosphorus	15	30.974
5 VIB	Sulfur	S	Sulfur	16	32.066
6 VIIB	Chlorine	Cl	Chlorine	17	35.453
7 VIIIB	Argon	Ar	Argon	18	39.948
8 VIIIA	Neon	He	Neon	10	4.003
9	Oxygen	O	Oxygen	8	15.999
10	Nitrogen	N	Nitrogen	7	14.007
11	Carbon	C	Carbon	6	12.011
12	Boron	B	Boron	5	10.811
13	Aluminum	Al	Aluminum	13	26.982
14	Magnesium	Mg	Magnesium	12	24.305
15	Sodium	Na	Sodium	11	22.990
16	Lithium	Li	Lithium	3	6.941
17	Beryllium	Be	Beryllium	4	9.012
18	Hydrogen	H	Hydrogen	1	1.008
19	K	K	Potassium	19	39.098
20	Ca	Ca	Calcium	20	40.078
21	Sc	Sc	Scandium	21	44.956
22	Ti	Ti	Titanium	22	47.867
23	V	V	Vanadium	23	50.942
24	Cr	Cr	Chromium	24	51.996
25	Mn	Mn	Manganese	25	54.938
26	Fe	Fe	Iron	26	55.845
27	Co	Co	Cobalt	27	58.933
28	Ni	Ni	Nickel	28	58.693
29	Cu	Cu	Copper	29	63.546
30	Zn	Zn	Zinc	30	65.38
31	Ga	Ga	Gallium	31	69.723
32	Ge	Ge	Germanium	32	72.631
33	As	As	Arsenic	33	74.922
34	Se	Se	Selenium	34	78.971
35	Br	Br	Bromine	35	79.904
36	Kr	Kr	Krypton	36	84.798
37	Rb	Rb	Rubidium	37	84.468
38	Sr	Sr	Strontrium	38	87.62
39	Y	Y	Yttrium	39	88.906
40	Zr	Zr	Zirconium	40	91.224
41	Nb	Nb	Niobium	41	92.905
42	Mo	Mo	Molybdenum	42	95.95
43	Tc	Tc	Technetium	43	98.907
44	Ru	Ru	Ruthenium	44	101.07
45	Rh	Rh	Rhodium	45	102.906
46	Pd	Pd	Palladium	46	106.42
47	Ag	Ag	Silver	47	107.888
48	Cd	Cd	Cadmium	48	112.411
49	In	In	Indium	49	114.818
50	Sn	Sn	Tin	50	118.711
51	Sb	Sb	Antimony	51	121.760
52	Te	Te	Tellurium	52	127.5
53	I	I	Iodine	53	126.904
54	Xe	Xe	Xenon	54	131.294
55	Cs	Cs	Cesium	55	132.905
56	Ba	Ba	Barium	56	137.328
57-71				57-71	
72	Hf	Hf	Hafnium	72	178.49
73	Ta	Ta	Tantalum	73	180.948
74	W	W	Tungsten	74	183.84
75	Re	Re	Rhenium	75	186.207
76	Os	Os	Osmium	76	190.23
77	Ir	Ir	Iridium	77	192.217
78	Pt	Pt	Platinum	78	195.085
79	Au	Au	Gold	79	196.957
80	Hg	Hg	Mercury	80	200.592
81	Tl	Tl	Thallium	81	204.383
82	Pb	Pb	Lead	82	207.2
83	Bi	Bi	Bismuth	83	208.980
84	Po	Po	Polonium	84	[208.982]
85	At	At	Astatine	85	209.987
86	Rn	Rn	Radon	86	222.018
87	Fr	Fr	Franium	87	223.020
88	Ra	Ra	Radium	88	226.025
89-103				89-103	
104	Rf	Rf	Rutherfordium	104	[261]
105	Db	Db	Dubnium	105	[262]
106	Sg	Sg	Seaborgium	106	[265]
107	Bh	Bh	Berthium	107	[264]
108	Hs	Hs	Hessium	108	[269]
109	Mt	Mt	Metternium	109	[268]
110	Ds	Ds	Domestaniium	110	[269]
111	Rg	Rg	Roentgenium	111	[272]
112	Cn	Cn	Copernicium	112	[277]
113	Uut	Uut	Ununtrium	113	[289]
114	Fl	Fl	Florivium	114	[289]
115	Uup	Uup	Ununpentium	115	[289]
116	Lv	Lv	Livermorium	116	[298]
117	Uus	Uus	Ununseptium	117	[298]
118	Uuo	Uuo	Ununoctium	118	[298]
103	Lr	Lr	Lutetium	103	174.967

Machine Learning for Materials studies

Data



Materials Project



Inorganic Crystal Structure Database

Machine Learning for Materials studies



- Kitchen sink method:
 - Use statistical analysis to learn relevant descriptors
- Domain knowledge:
 - Construct features that are important for describing a system
- Example:
 - Ionic compounds have atoms in different columns of periodic table
 - Descriptor: column # of the periodic table

Machine Learning for Materials studies

Datascience
tools

Statistical
models

