

Anharmonic thermodynamic properties and phase boundary across the post-perovskite transition in MgSiO_3



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Method: phonon quasiparticle approach

Mode-projected velocity autocorrelation function:

$$\langle V_{\mathbf{q}_S}(0) \cdot V_{\mathbf{q}_S}(t) \rangle = \lim_{\tau \rightarrow \infty} \frac{1}{\tau} \int_0^\tau V_{\mathbf{q}_S}^*(t') V_{\mathbf{q}_S}(t' + t) dt'$$

$$V_{\mathbf{q}_S}(t) = \sum_{i=1}^N \sqrt{M_i} \mathbf{v}_i(t) e^{i\mathbf{q} \cdot \mathbf{R}_i} \cdot \hat{\mathbf{e}}_{\mathbf{q}_S}$$

Renormalized frequency and phonon linewidth:

$$\langle V_{\mathbf{q}_S}(0) \cdot V_{\mathbf{q}_S}(t) \rangle = A_{\mathbf{q}_S} \cos(\tilde{\omega}_{\mathbf{q}_S} t) e^{-\Gamma_{\mathbf{q}_S} t}$$

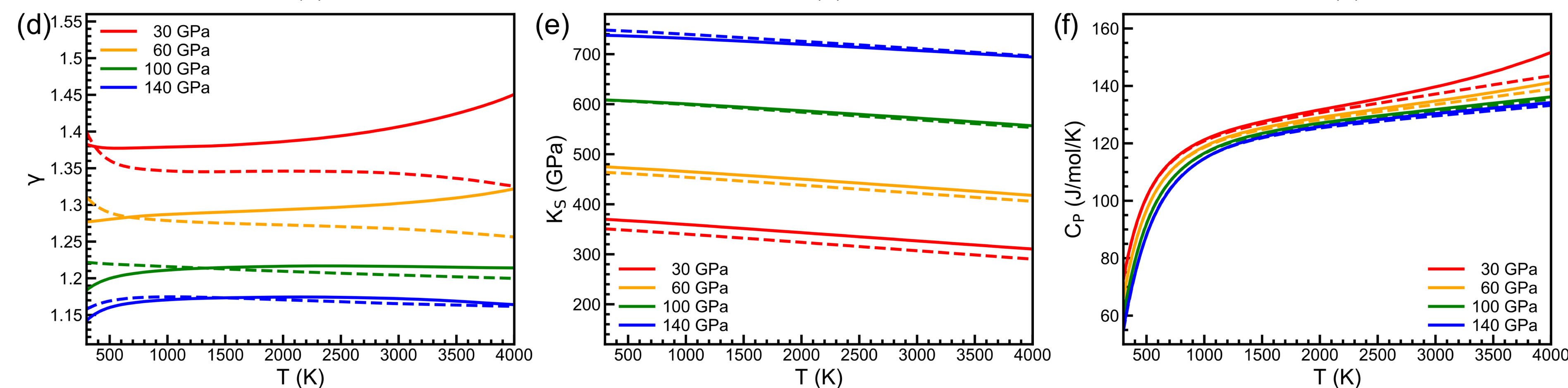
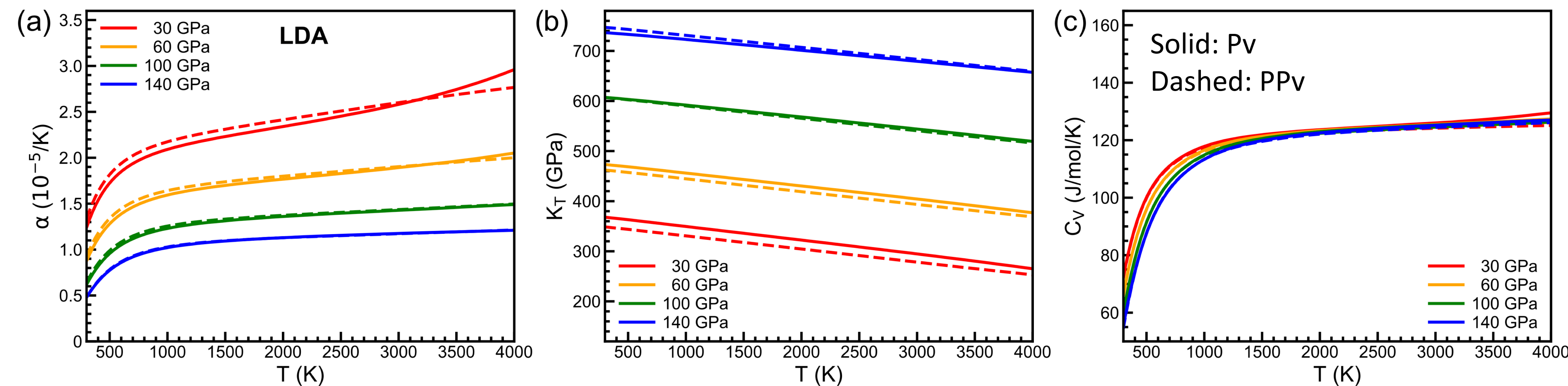
$$G_{\mathbf{q}_S}(\omega) = \left| \int_0^\infty \langle V_{\mathbf{q}_S}(0) \cdot V_{\mathbf{q}_S}(t) \rangle e^{i\omega t} dt \right|^2$$

Vibrational entropy and free energy with the PGM:

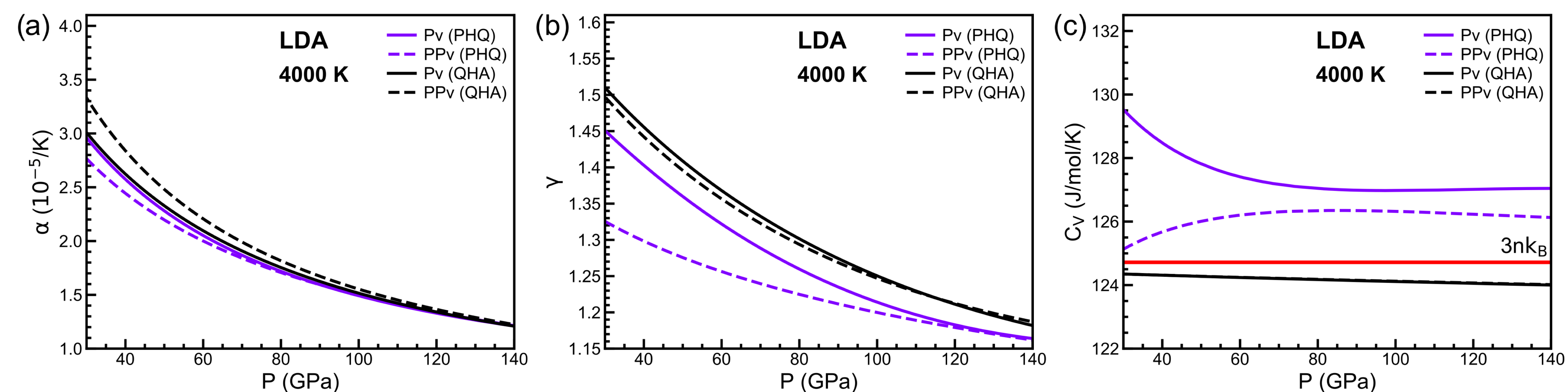
$$S_{\text{vib}}(T) = k_B \sum_{\mathbf{q}_S} [(n_{\mathbf{q}_S} + 1) \ln(n_{\mathbf{q}_S} + 1) - n_{\mathbf{q}_S} \ln n_{\mathbf{q}_S}]$$

$$F(T) = E_0 + \frac{1}{2} \sum_{\mathbf{q}_S} \hbar \omega_{\mathbf{q}_S} - \int_0^T S_{\text{vib}}(T') dT'$$

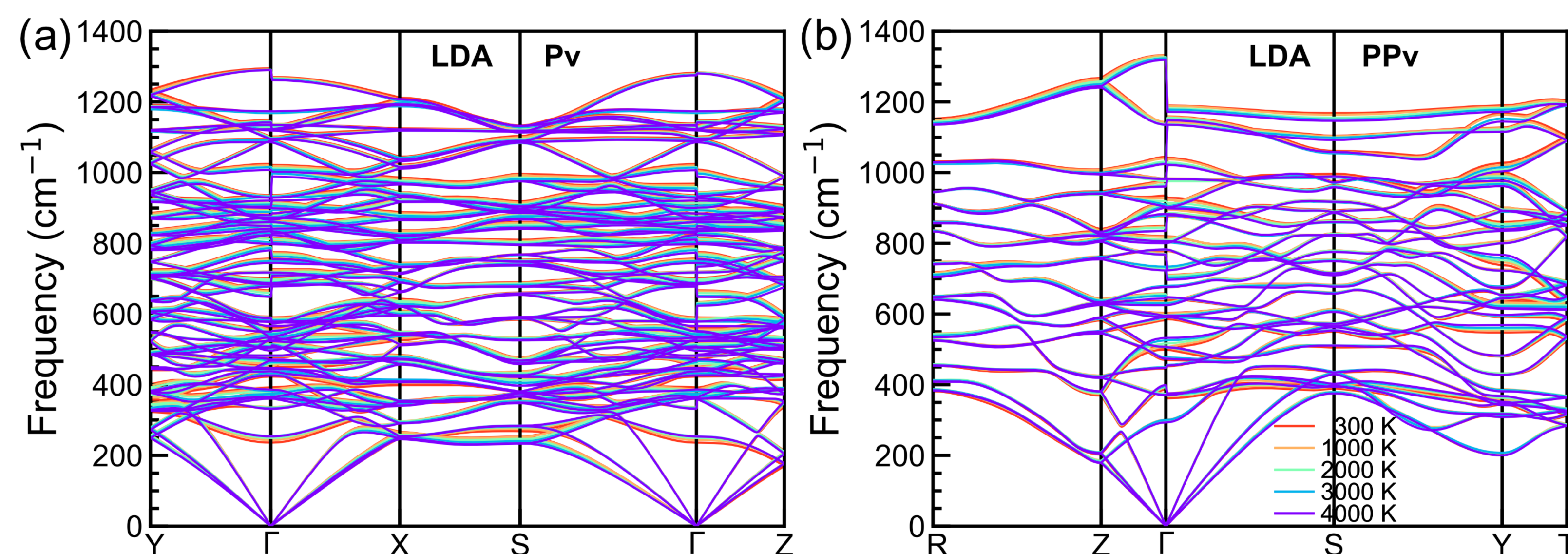
Anharmonic thermodynamic properties



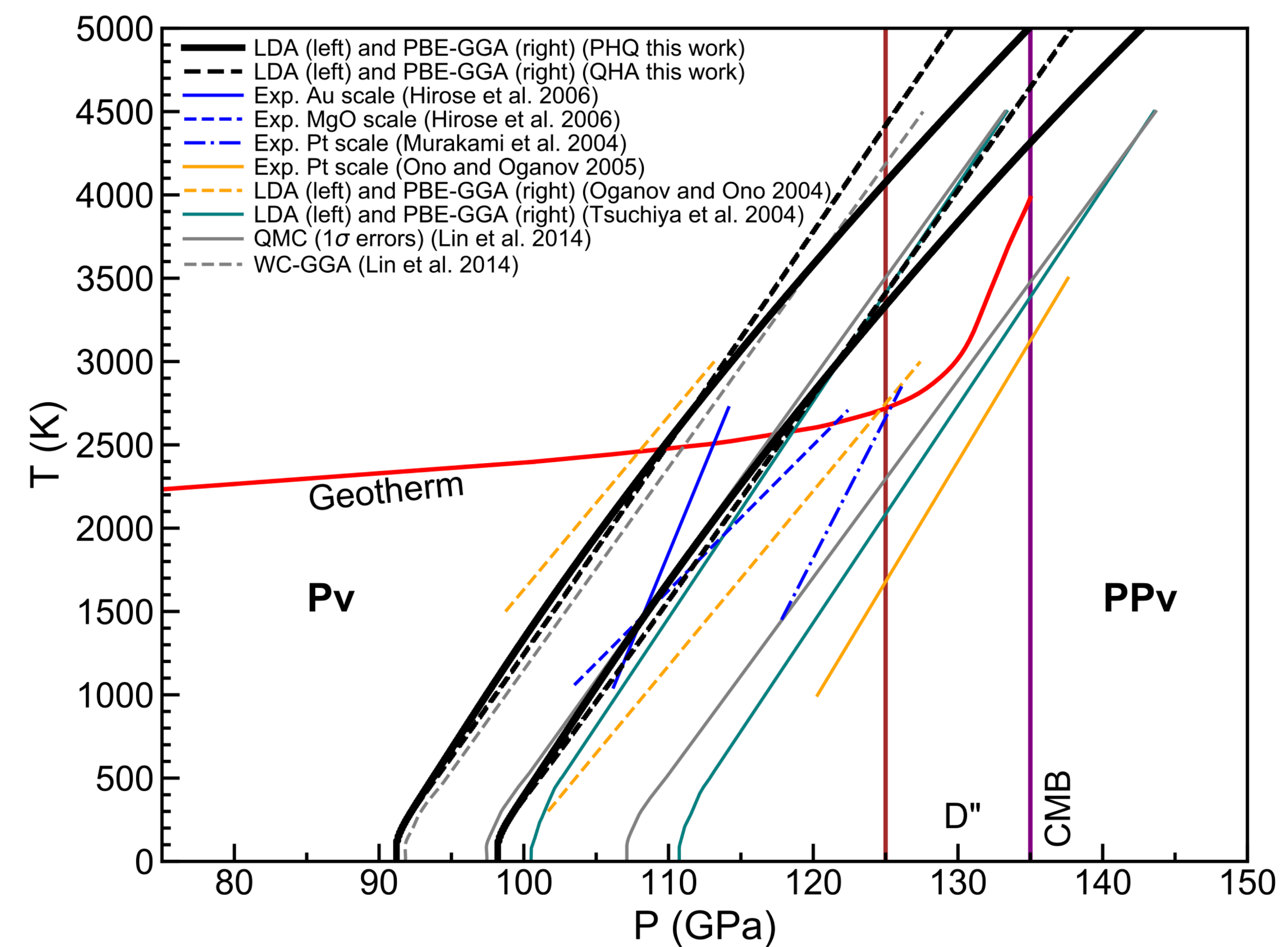
PHQ and QHA comparisons



T-dependent anharmonic phonon dispersions



Pv-PPv phase boundaries



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