

Spin state and structural stability of ferropericlyase up to 30 Mbar

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INTRODUCTION

• As a solid solution of MgO and FeO [(Mg_{1-x},Fe_x)O] ferropericlyase(fp) might be a major mantle forming phase terrestrial type exoplanets.

• The properties of fp are well characterized within the range of condition typical of the Earth's interior but they need to be investigated also in a much broader pressure/temperature range achieved in the interior of larger planets.

• The interplay between a structural change and the spin-state change in iron makes it a non-trivial task.

METHODS

• LDA+U: treat the strong on-site Coulomb interaction of localized electrons in iron oxides, which is not correctly described by standard (LDA or GGA) DFT calculations.

$$E = E_{LDA} + \frac{U}{2} \sum_{l,\sigma} Tr[\mathbf{n}^{l,\sigma}(1 - \mathbf{n}^{l,\sigma})]$$

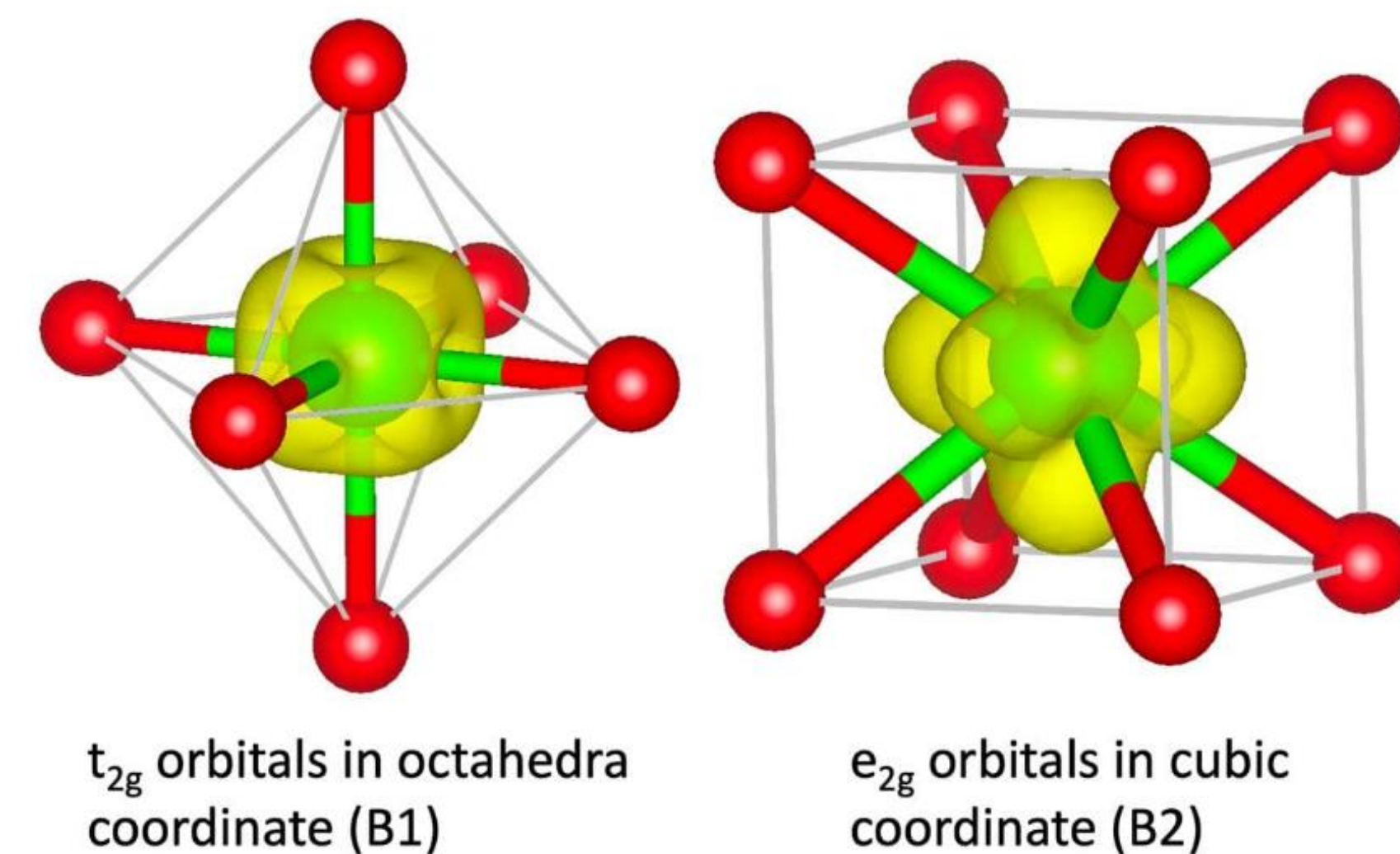
• Phonon calculations were performed using the finite-displacement method implemented in the Phonopy code¹ with the LDA+U calculations from Quantum ESPRESSO. The electronic entropy at high temperatures was obtained using the Mermin functional^{2,3}. The final Gibbs free energy computed with the quasi-harmonic approximation calculations, i.e.

$$G(P, T) = G^{QHA}(P, T) = H(P, T) - T(S_{elec} + S_{vib} + S_{mag})$$

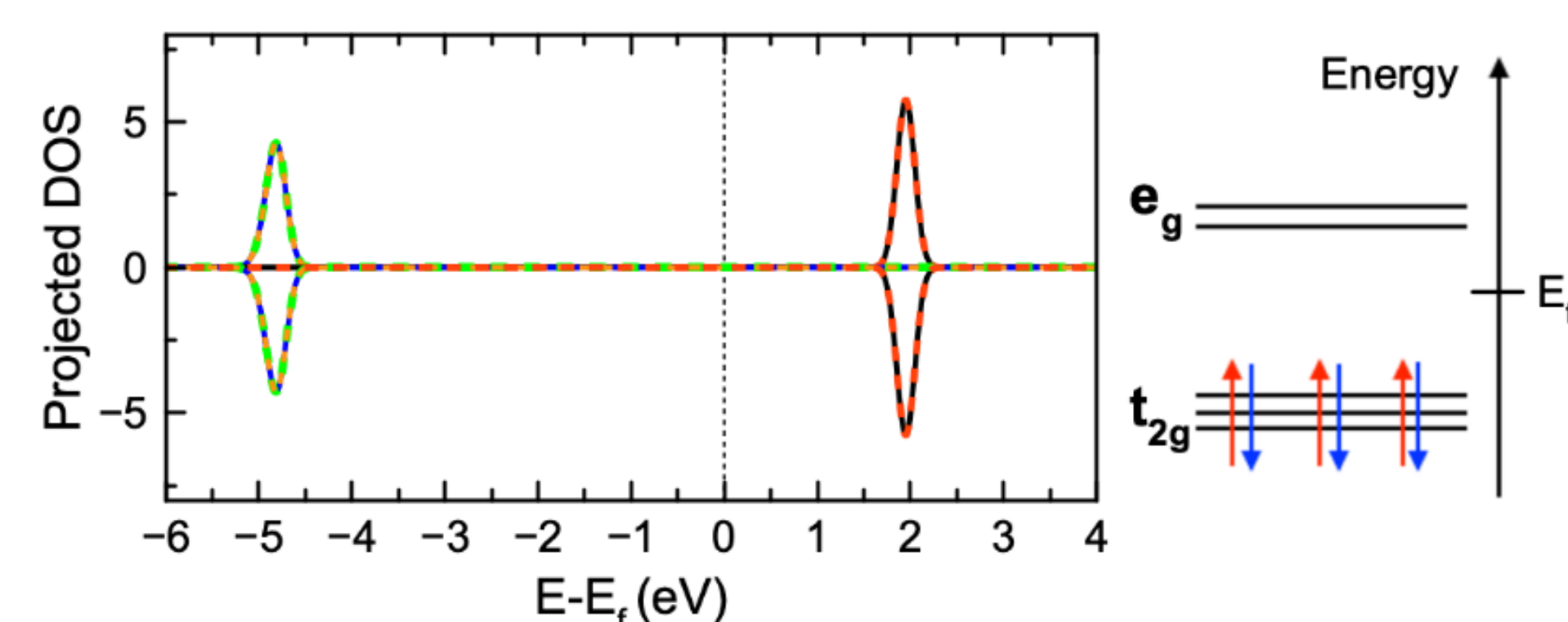
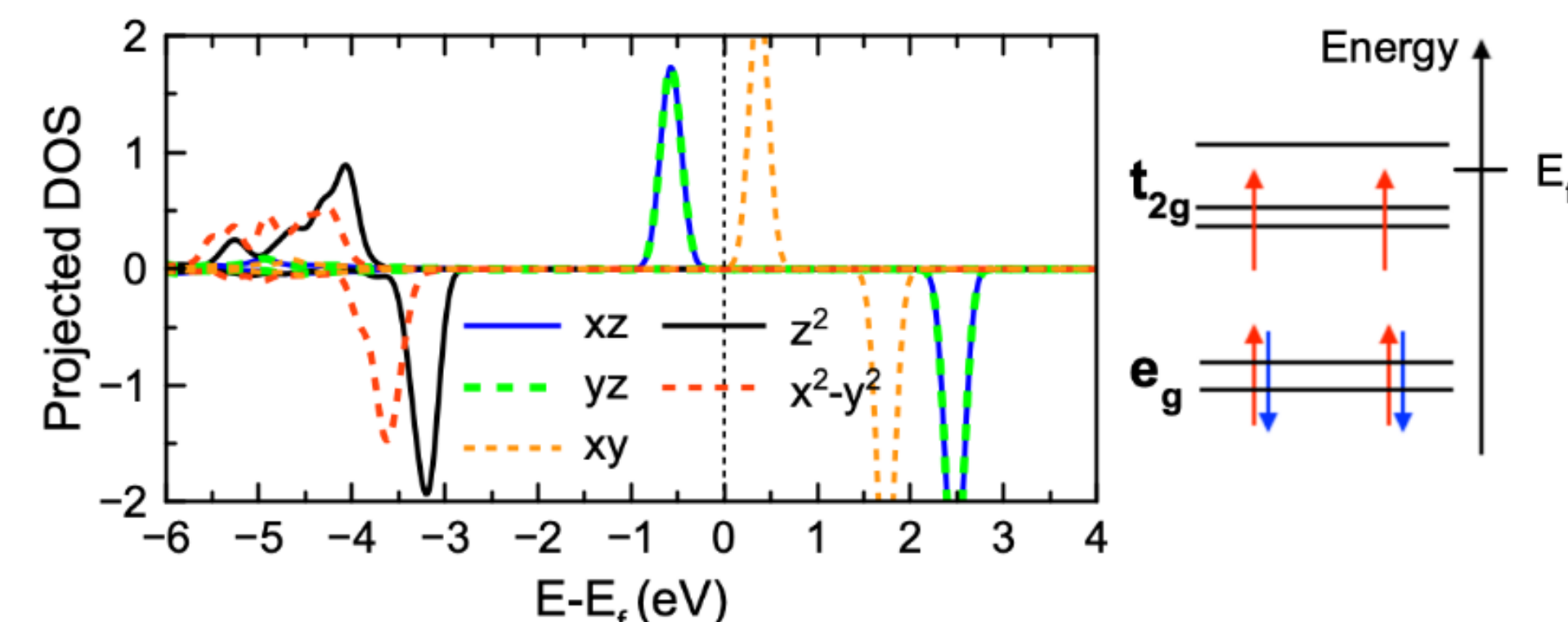
• For the face-centered cubic phase, B1 phase, we constructed a 2 × 2 × 2 supercell with 64 atoms with one iron atom corresponding to the iron concentrations X_{Fe}=0.03125 (fp3). Similarly, a 2√2 × 2√2 × 4 supercell has been constructed for B2 phase, which is a body-centered cubic phase. Ferrous iron is the form of iron in both B1 and B2 phase.

STATIC RESULTS

• In the B1 structure, the t_{2g} orbitals have lower energy than e_g orbital. However, in the B2 structure, e_g orbitals have lower energy than t_{2g} orbitals. The lower energy of e_g orbitals in B2 is due to the change of the polyhedron surrounding ferrous iron (Fe²⁺).

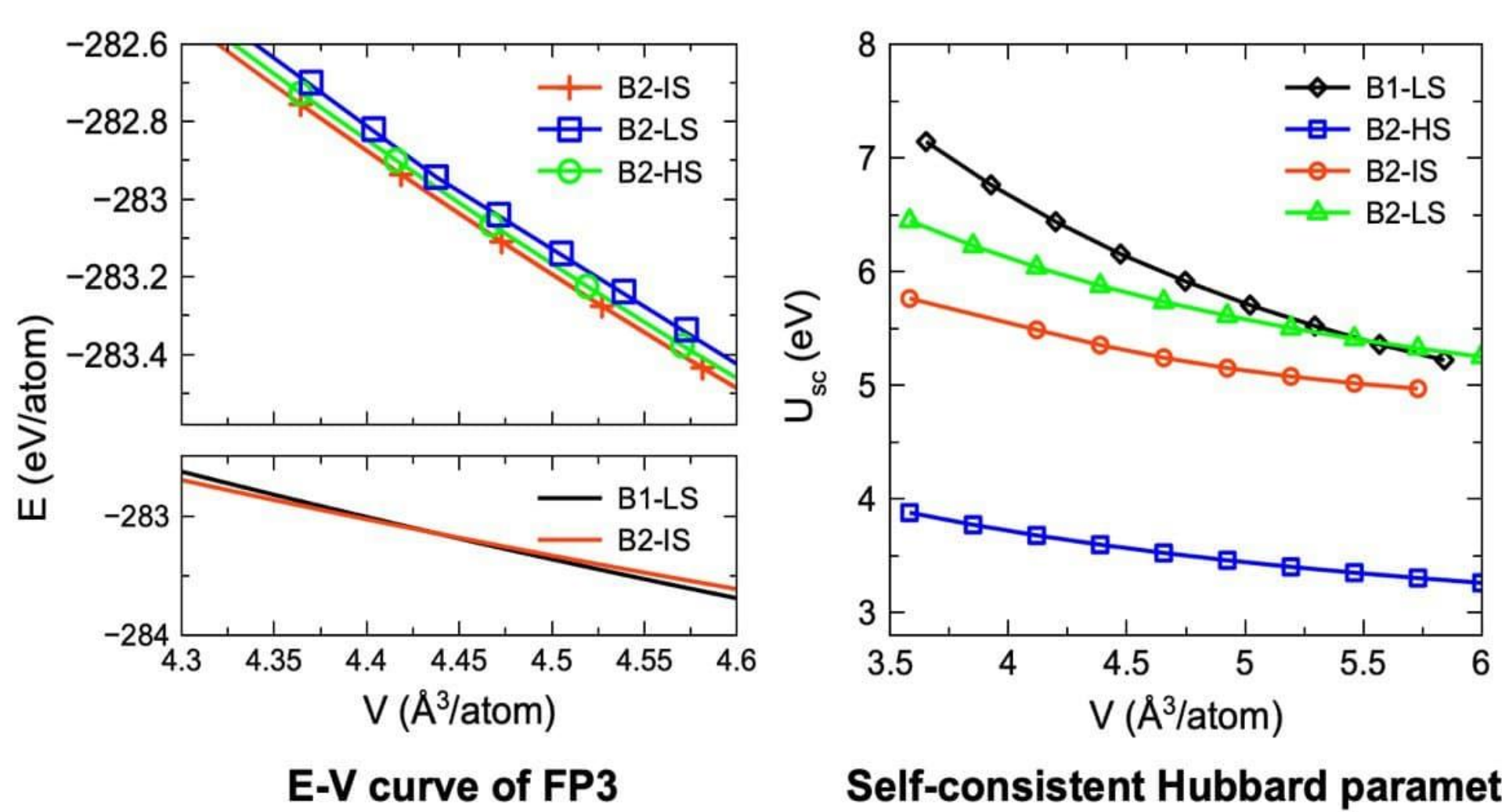


• In the B2 structure, four of the six d-electrons of Fe²⁺ occupy the e_g orbital with spin up and spin down. The remaining two electrons occupy two of the three t_{2g} orbitals. Such an occupancy leads to an intermediate-spin state, with S=1.

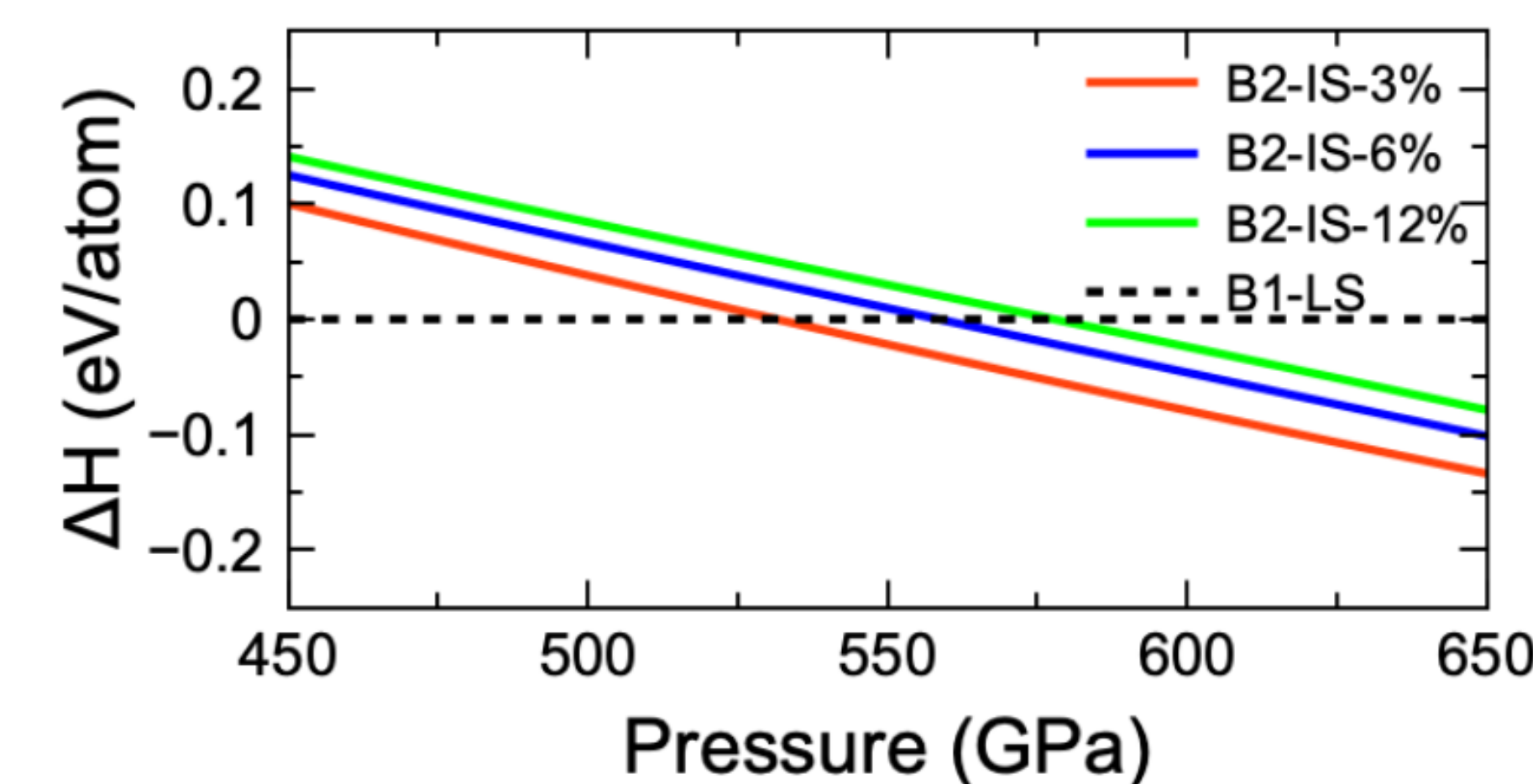


• The corresponding self-consistent Hubbard parameters display a strong dependence on volume, structure, and spin states.

• The B2-IS state has lower energy than the B2-HS and B2-LS states at all pressures in static calculations. Furthermore, there is a structural transition between B1-LS and B2-IS in fp3.



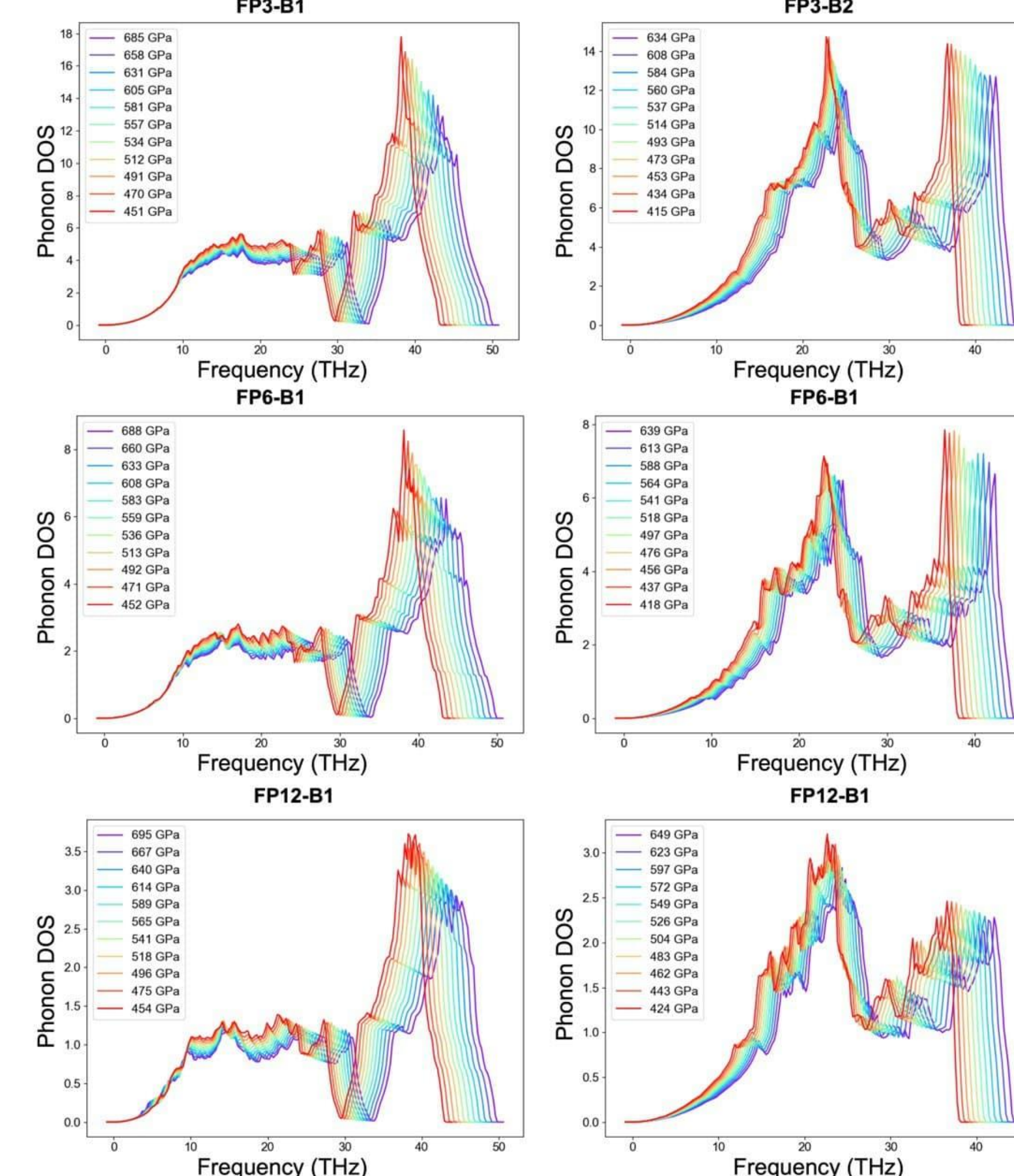
• The current LDA+U_{sc} calculations produce concentration dependent B1-LS to B2-IS transition pressures: 526 GPa, 568 GPa, and 576 GPa in fp3, fp6, and fp12, respectively.



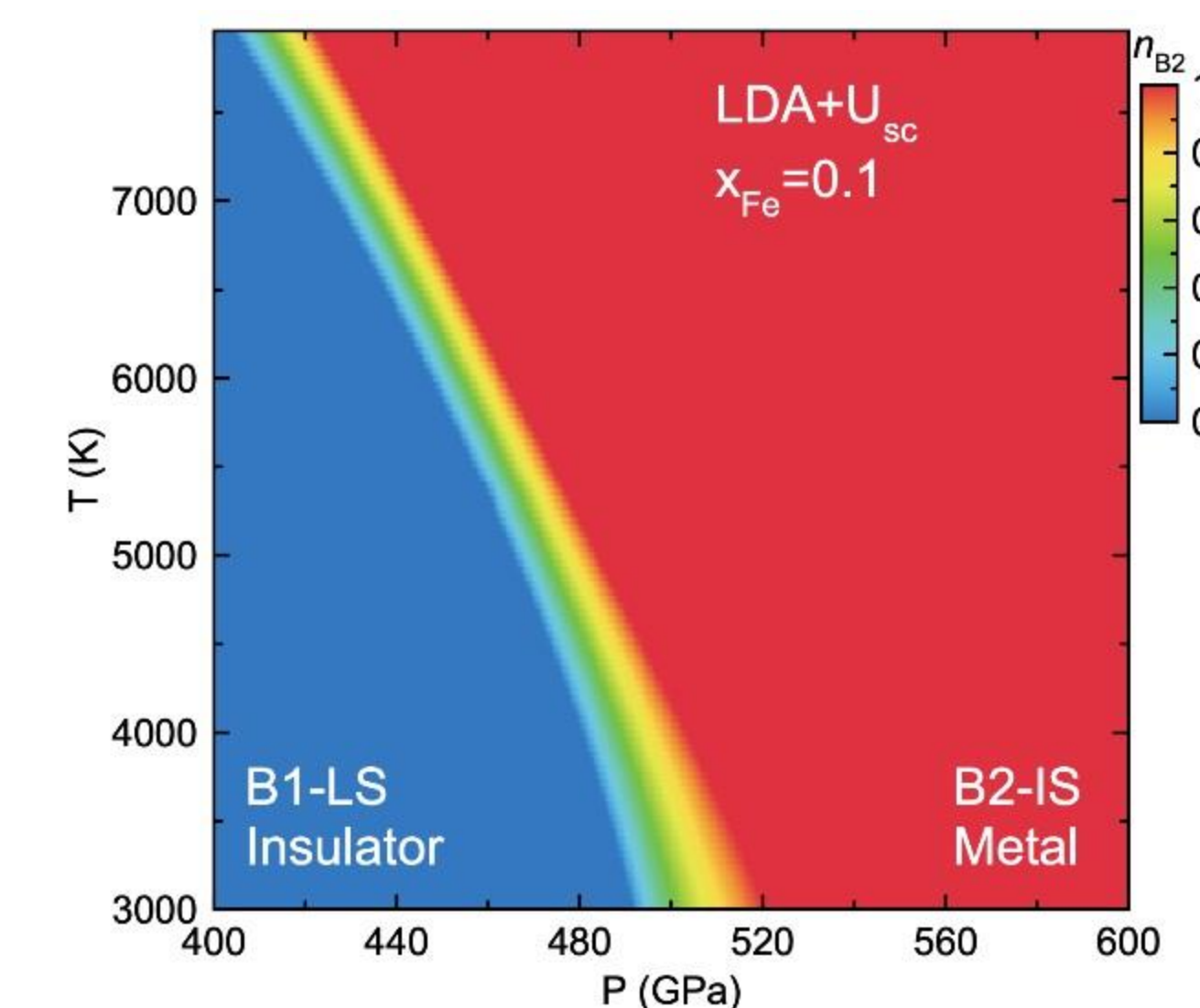
PHONON RESULTS

• Phonon calculations are performed with LDA+U_{sc} at several volumes in both B2-IS and B1-LS states for fp3, fp6, and fp12.

• No imaginary frequency is found in either B2-IS states or B1-LS states within the chosen pressure range. Therefore, both B2-IS and B1-LS states of fp with up to 12.5% iron are dynamically stable.



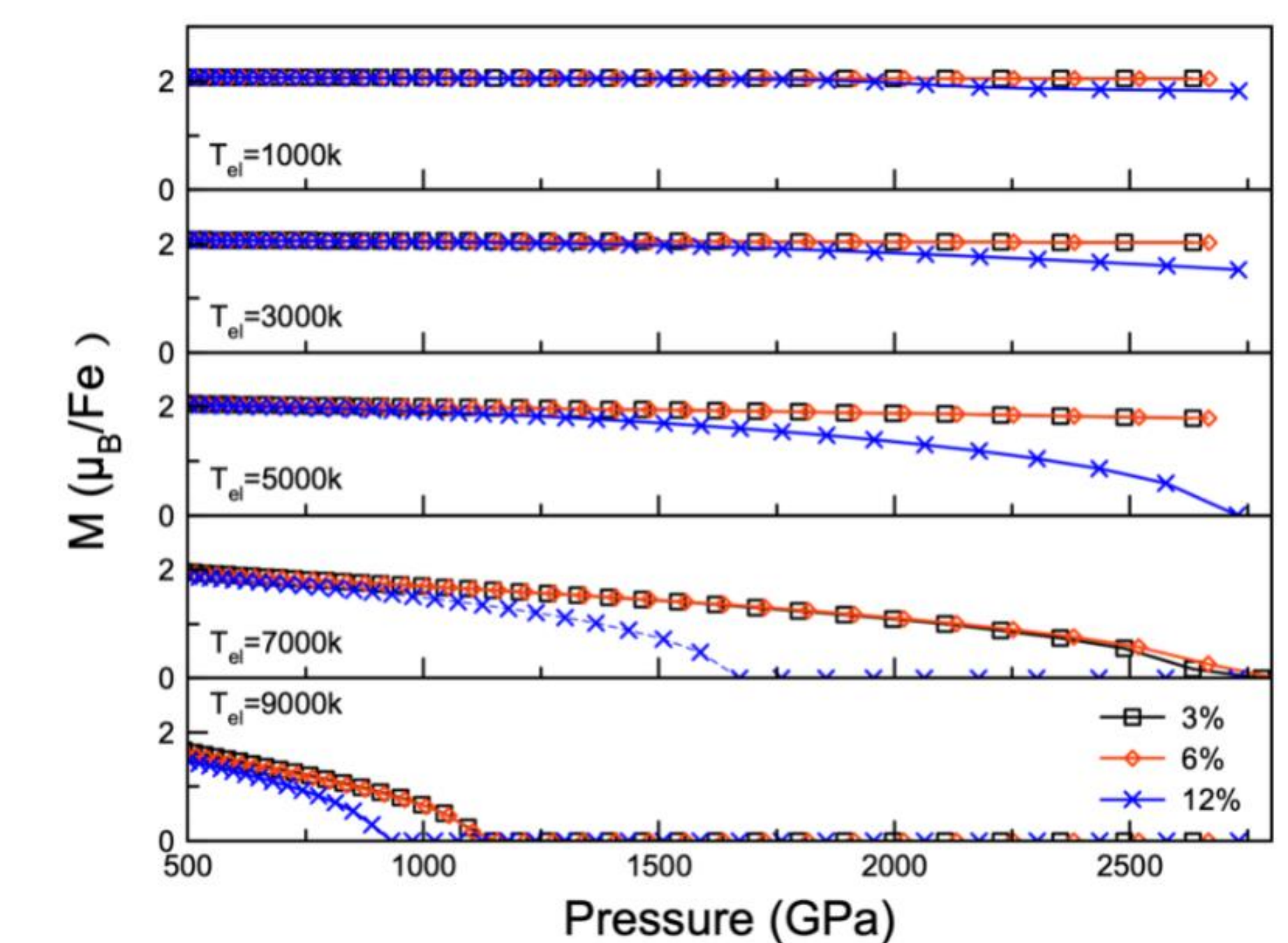
• To obtain the phase boundary at finite temperatures, we further included the vibrational entropy S_{vib} and electronic entropy S_{elec} described by the Mermin functional.



• The B2-IS phase is stable up to 2.5 TPa with T_{el}=1000K.

• With increasing electronic temperature, the electronic entropy destroys magnetization.

• At T_{el}=5000K, there are signs of a transition between B2-IS to B2-LS for X_{Fe}=12%. With higher electronic temperatures and higher Fe concentrations, the IS-LS transition pressure decreases.



SUMMARY AND ACKNOWLEDGMENT

• The intermediate-spin state is the ground state of fp in the B2 structure.

• The self-consistent Hubbard parameters U obtained from LDA+U_{sc} calculations depends strongly on pressure, structure, and spin state.

• There is a possible transition from B2-IS to B2-LS in the fp system, which depends on the electronic temperature.

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